

This is a nice result of one particular ocean model that shows only a slightly stronger LGM AMOC than present day, but more shoaled, using a stronger calculated LGM tidal mixing. Ferrari 2014, suggested that a shallower interface between North Atlantic Deep Water (NADW) and Antarctic Bottom Water (AABW), as observed for the LGM, reduced mixing between the two water masses, and in turn increased deep carbon. So this study can help test our understanding of biogeochemical cycles during deglaciation in further studies that come along. The impact of the strong LGM forcing on the mechanical forcing of the AMOC is novel. It would have been nice to see further theoretical analysis on how the mixing does not impact the AMOC in the upper ocean (e.g. meridional transport based upon zonal density gradients etc.). Also I find there isn't much effort put into describing the ocean model here and giving a more detailed description or illustration of how the ocean model actually performs against modern observations, in particular how the water masses compare and how the stratification compares in modern (see below).

We thank the reviewer for their positive and constructive feedback on our manuscript. Below are our detailed, point-by-point responses:

L47-50: Add some more text here that there is more dissipation in the interior instead of the shelves at LGM. Removing the shelves reduces the damping of the tides and leads to increase in tidal amplitude.

**Authors' Response:** Thank you for your valuable feedback. We will include a brief explanation on lines 47-50 to clarify that during the LGM, the reduction of the continental shelves led to decreased tidal damping and consequently enhanced tides.

L92: You might mention here that the use of ICE-6G instead of ICE-5G is suggested to reduce internal vertical mixing and would therefore suggest a further weakened AMOC (Wilmes et al 2021).

**Authors' Response:** Thank you for your valuable suggestions. Yes, the choice of LGM bathymetry databases can influence the tidal dissipation obtained in the tidal model. The tidal dissipation derived using ICE-6G is indeed weaker than that obtained using ICE-5G (Wilmes et al., 2019; Wilmes et al., 2021). We will add a corresponding explanation in the manuscript. Our choice to use ICE-5G is to demonstrate that even under conditions of strong tidal dissipation, the tides alone are insufficient to alter the shallower geometry of the AMOC during the LGM. We will include the corresponding explanations in the revised manuscript.

In Figure 3 (left column) I would like to see instead a vertical profile of horizontally averaged  $N^2$  and the mean values. What mean values are used in the tide model  $D_{IT}$  (internal wave drag)? Are they taken from the PD and LGM simulations?

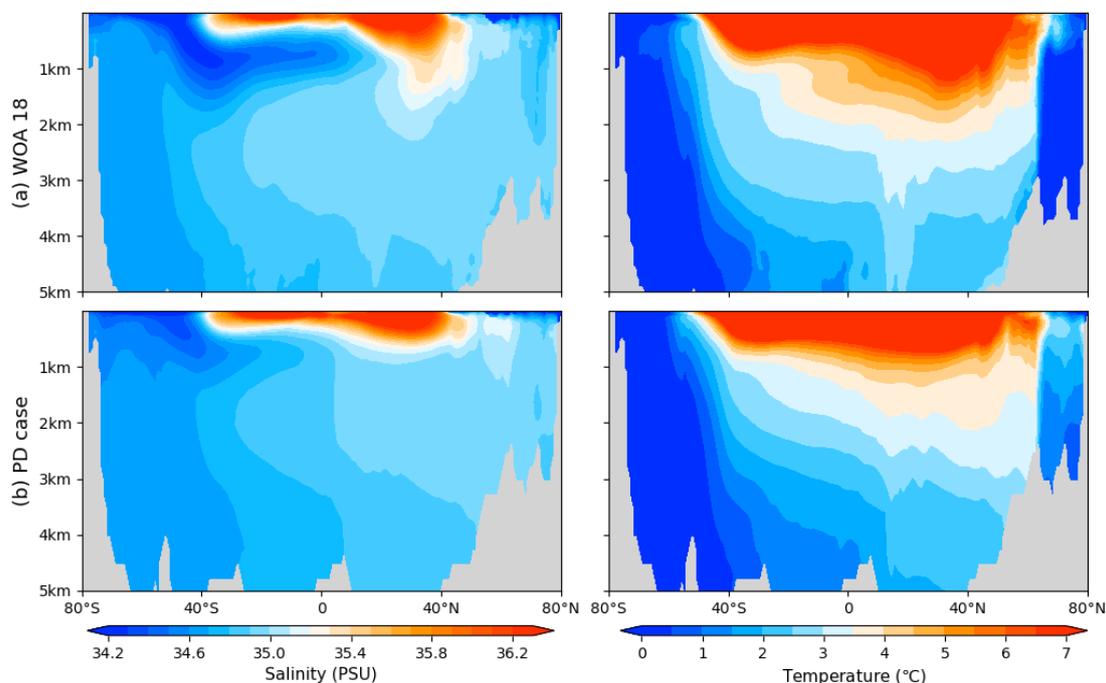
**Authors' Response:** Thank you for your feedback. Yes, the  $N^2$  values used in the tidal model are derived from the PD and LGM simulations. We have provided a global depth-averaged distribution of  $N^2$  in response to your comment regarding L135-136.

Section on Ocean Model: I would like to see more information about the ocean model described here. What is the resolution? In addition to "Figure S1 presents the horizontal resolution of the meshes for PD and LGM", please describe it here. How does it perform with respect to the present day? Isn't the

AMOC a little weak compared with the RAPID array or other observations? How is the modern ocean forced? Does it use COREv2 AMIP type forcing? I want a better description of how the stratification compares with modern day observations. Maybe a T-S density showing different water masses in the ocean compared with modern observations (say ARGO). We don't get a good feel from this document on how the model actually performs against modern observations, which is the most important part of the paper.

**Authors' Response:** Thank you for your valuable comments. We will include Figure S1 in the main text and add relevant information regarding the resolution of the meshes. For the PD cases, we employed atmospheric forcing derived from the Reanalysis dataset (JRA55-do 1.4.0) spanning the period from 1958 to 2020.

Yes, the simulated AMOC is slightly weaker compared to observations. However, what is more crucial in our simulations is the ability to reproduce the geometry of the AMOC for both PD and LGM periods, as well as the ocean characteristics of these periods, and study the effects of tides on this basis. We have included a comparison of the temperature and salinity in the Atlantic Ocean from our PD case with the WOA (World Ocean Atlas) 2018 data, as shown in the Figure R1 below. The results indicate that our model effectively reproduces the temperature and salinity structures of the modern ocean. Based on this foundation, we accurately replicated the ocean characteristics during the LGM period as indicated by proxy data (Adkins et al., 2002; Knorr et al., 2021): strong vertical stratification caused by elevated salinity of the deep sea and the rapid temperature decrease in the ocean's upper layers. This was not achieved in previous studies (Schmittner et al., 2015; Wilmes et al., 2019), which is why they concluded that tides would significantly enhance the AMOC during the LGM.



**Figure R1.** Comparison of salinity and temperature between WOA 18 data and PD simulation in the Atlantic Ocean.

Line 115: In ocean models “ $k_{bg}$  is employed to manage the effects of various background mixing mechanisms”. However, the tidal mixing parameterization considers the locally dissipated energy over topography (1/3 of the total energy dissipation). The other 2/3 is dissipated in the far-field in which the background diffusivity is used to represent this. Is this correct interpretation? If so, wouldn’t this tend to underestimate the effect of the increased tidal mixing.

Therefore, there is a constant internal energy dissipation due to internal wave breaking in the far field of something of the order of  $\int (\Gamma^{-1} * \rho * N^2 k_{bg}) dV$ . Do you know how large this value is?

**Authors’ Response:** Thank you for your suggestions. The tidal mixing parameterization indeed only considers the locally dissipated energy. Therefore, we calculated the far-field dissipation due to  $k_{bg}$  and the local tidal dissipation for each simulation using Osborn (1980) formula:

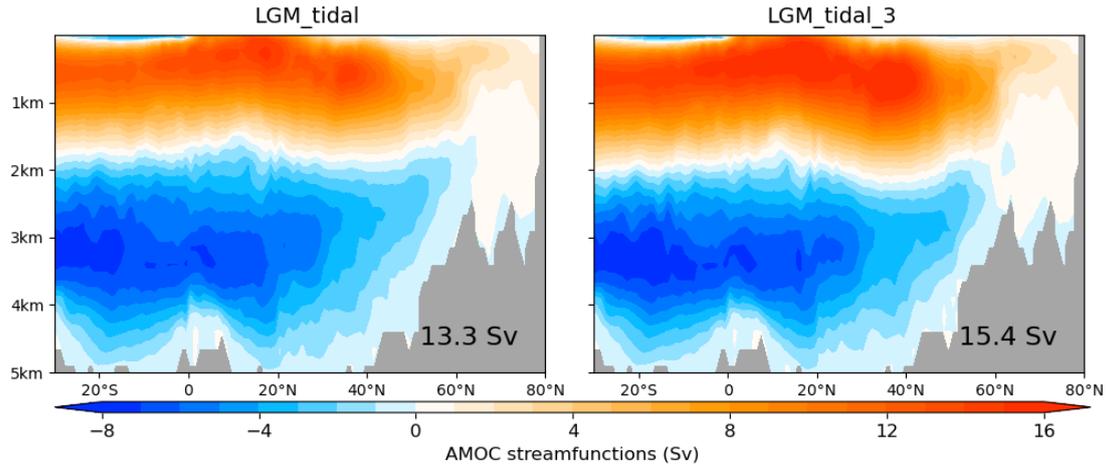
$$P = \int \rho \epsilon dV = \frac{1}{\Gamma} \int \rho k N^2 dV$$

The results are shown in the table R1 below. Additionally, we conducted a new experiment, LGM\_tidal\_3, where we increased  $k_{bg}$  from  $1*10^{-5} \text{ m}^2\text{s}^{-1}$  to  $3*10^{-5} \text{ m}^2\text{s}^{-1}$  for comparison. The results in the table indicate that the LGM\_tidal experiment indeed underestimated the energy provided by tides, while the total energy in LGM\_tidal\_3 reached 3.92 TW.

We compared the AMOC geometry in LGM\_tidal and LGM\_tidal\_3, as shown in the figure below. The geometry of the AMOC in LGM\_tidal\_3 does not show significant changes and remains relatively shallow, further supporting the conclusions of our study. The only notable change is in the AMOC strength, which increased from 13.3 Sv to 15.4 Sv. We will add this discussion to the revised manuscript. We believe that these additions emphasize not only the necessity of employing tidal mixing parameterization but also the importance of appropriately adjusting the background diffusivity  $k_{bg}$ .

**Table R1.** Summary of energy consumption due to diapycnal mixing

Simulation	$k_{bg}$ ( $1*10^{-5} \text{ m}^2\text{s}^{-1}$ )	$k_{bg}$ contribution (TW)	Tidal contribution (TW)	Total (TW)
PD	1	0.79	0	0.79
PD_tidal	1	0.78	0.38	1.16
LGM	1	1.05	0	1.05
LGM_tidal	1	1.02	1.03	2.05
LGM_tidal_3	3	2.86	1.06	3.92

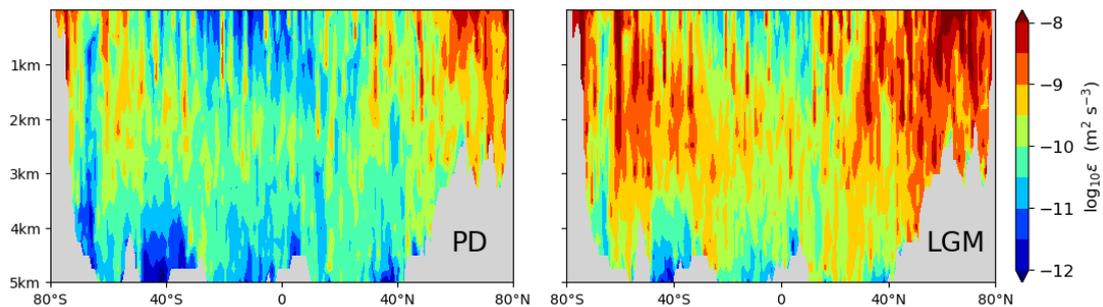


**Figure R2.** AMOC streamfunctions (Sv) between LGM\_tidal and LGM\_tidal\_3.

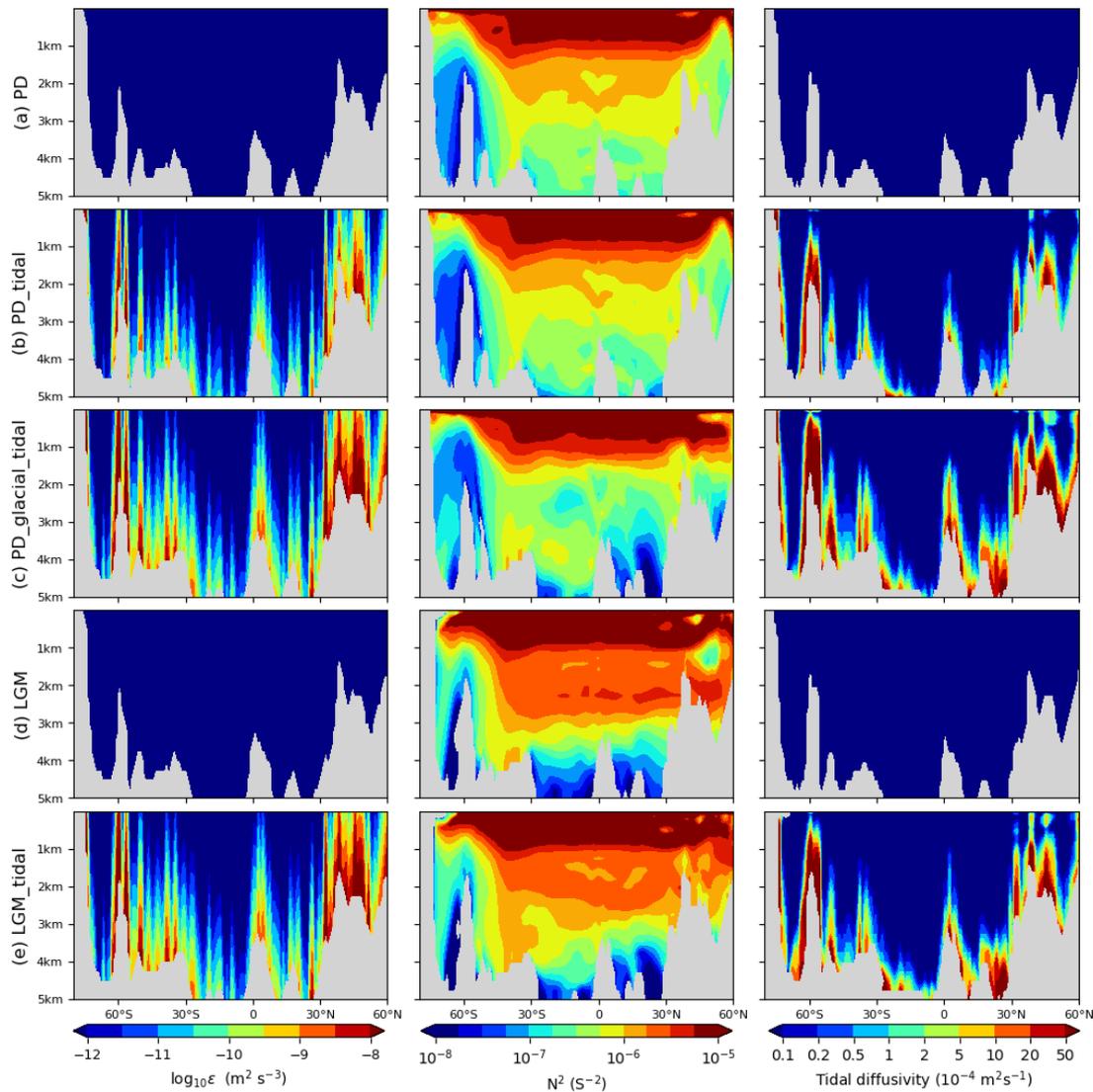
Line 121:  $K_{v\_tidal}$  is dependent on  $N^2$  and the internal tide dissipation energy, epsilon. Epsilon is increasing at LGM, but the stratification is also increasing. I would like to see a quantitative comparison of the results produced in Figure 2 (right column) due to each component, the internal tide energy dissipation and the stratification.

**Authors' Response:** The change in tidal dissipation has specific figures, increasing from 1.31 TW during the PD to 3.41 TW during the LGM. For  $N^2$ , we will give the percentage increase both globally and in the Atlantic Ocean, comparing the changes between these two parameters.

It is worth noting that there is significant spatial distribution variability between them. Therefore, we further plotted the vertical distribution of the rate of tidal dissipation. Figure R3 presents the zonally averaged vertical distributions of the rate of tidal dissipation in the Atlantic Ocean. However, due to the spatial variability of dissipation (as shown in Figure 1 of the manuscript) and changes in water depth, the dissipation rate in Figure R3 shows considerable variation and does not clearly reflect its decrease from the seafloor upwards. Therefore, in Figure R4, we provide the rate of tidal dissipation (left), the squared buoyancy frequency (middle), and tidal diffusivity (right) along the 27°W section.



**Figure R3.** Zonally averaged vertical distributions of the rate of tidal dissipation for PD and LGM in the Atlantic Ocean.



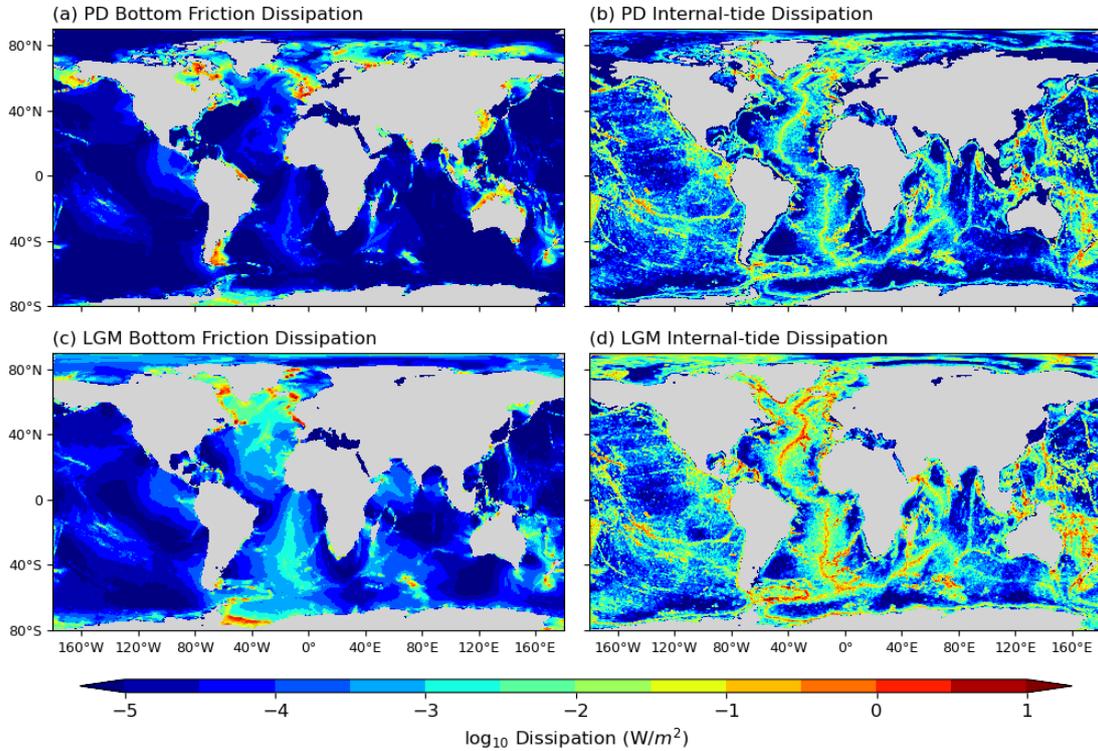
**Figure R4.** The rate of tidal dissipation (left), the squared buoyancy frequency (middle), and tidal diffusivity (right) along 27°W section.

L125: One of the biggest problems I have is with these Jayne et al 2009 type parameterizations is the vertical decay function  $F$  using this universal e-folding factor of 500m. Would this not tend to overestimate the internal tide mixing energy in shallow seas? But if your hypothesis is true, then the LGM surface forcing overcomes these inadequacies in the parameterization.

**Authors' Response:** Regarding the issues with the tidal mixing parameterization, I would like to address this based on my understanding. In the barotropic tidal model, tidal energy is dissipated in two forms: the bottom friction term (equation 2 in the manuscript) and the internal-wave drag term (equation 3 in the manuscript). The dissipation of  $D_{BL}$  caused by the former primarily occurs in shallow seas, while  $D_{IT}$  caused by the latter mainly occurs in deep seas. The global distribution is shown in Figure R5. The proportion of  $D_{IT}$  used in tidal mixing parameterization in regions shallower than 500 meters is very small, as indicated in Table R1.

**Table R1.** Global and Sub-500m Distribution of  $D_{IT}$  and  $D_{BL}$  during PD and LGM.

Time	$D_{IT}$	$D_{IT} (<500 \text{ m})$	$D_{BL}$	$D_{BL} (<500 \text{ m})$
PD	1.31	0.21	1.69	1.65
LGM	3.41	0.36	1.17	0.99



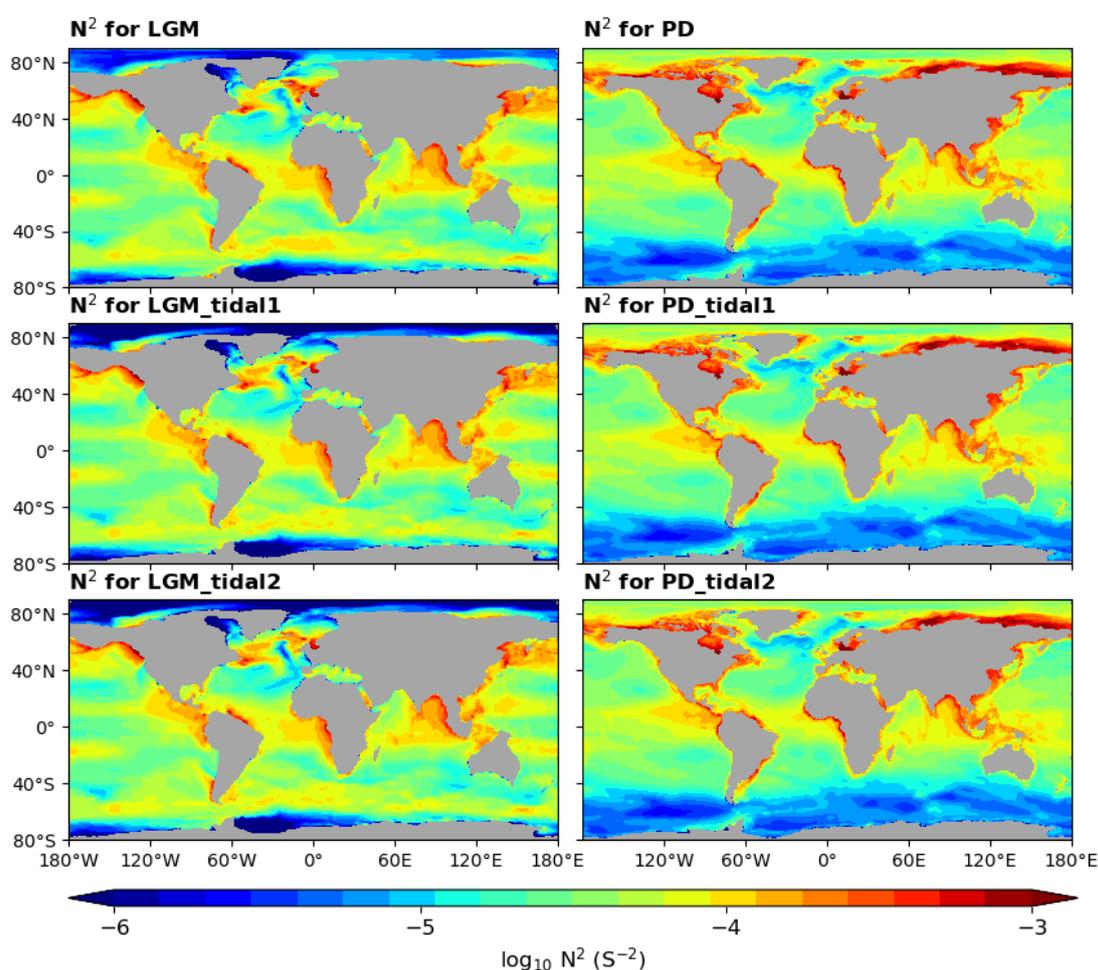
**Figure R5.** Global distributions of bottom friction dissipation ( $D_{BL}$ ) and internal-tide dissipation ( $D_{IT}$ ) during PD and LGM.

L133: “which resonates with the North Atlantic basin”. Do you mean that the predominant contributor, the M2 tide, has increased resonance in the North Atlantic at LGM. Isn’t this due predominantly because of the removal of the shelves at LGM and the increases of tidal mixing in the deep North Atlantic Ocean at LGM?

**Authors’ Response:** Thank you for your feedback. Actually, 12.66 hours is one of the natural resonant periods of the present-day Atlantic Ocean (Muller, 2008), which is very close to the 12.42 hours period of the M2 tide. In this resonant situation, the removal of the shelves during the LGM led to decreased damping, resulting in a significant increase in the M2 tide. I will include this explanation in the revised manuscript.

L135-136: So the horizontal variations of  $D_{IT}$  are put into FESOM in a one off setting. I assume the variations in the Brunt Vaisala frequency are taken from an LGM simulation then used to calculate the LGM tides and then the ocean model is run with these. There would presumably be some feedback between the stratification and the tide model if this were done in a proper interactive way and that the results might be different if this were done. This should be mentioned here.

**Authors' Response:** Thank you for your comment. In fact, we used an iterative approach to address the interaction between  $D_{IT}$  and ocean simulations for the PD\_tidal and LGM\_tidal experiments. The iterative process is as follows: Taking the LGM simulations as examples, we first input the  $N^2$  obtained from the LGM case (no tidal mixing) into the tidal model, then input the resulting tidal dissipation back into the OGCM, obtaining the experimental result LGM\_tidal1. Next, we input the  $N^2$  from LGM\_tidal1 back into the tidal model to obtain a new tidal dissipation, and run the OGCM again to obtain LGM\_tidal2. The LGM\_tidal shown in our manuscript is actually LGM\_tidal2. Figure R6 illustrates the changes in depth-averaged vertical  $N^2$  during the iterations for both the PD and LGM. It can be seen that during the simulation of LGM, the change from LGM to LGM\_tidal1 primarily involves a decrease in  $N^2$  in the Arctic. From LGM\_tidal1 to LGM\_tidal2, there is almost no change. For the PD simulations, there were no significant changes in  $N^2$  throughout. Thus, we have nearly eliminated the mutual influences between  $N^2$  in the tidal model and the OGCM through one iteration.



**Figure R6.** Changes in depth-averaged vertical  $N^2$  Across Iterations for LGM and PD Simulations.

L142 expand on “we apply five cycles”

**Authors' Response:** Thank you for your inquiry. For the PD cases, our surface (atmospheric) forcing is derived from the Reanalysis dataset (JRA55-do 1.4.0), covering the period from 1958 to 2020. We repeatedly drove each PD case with data from this time span five times to achieve simulation stability. We will include this description in the revised manuscript.

L147 Also the atmospheric forcing is held fixed. A reduced AMOC would have reduced heat transport to the North Atlantic which would favour sea ice growth to some degree, even though the atmosphere tends to compensate for the lack of ocean heat transport. This would presumably affect deep water formation and stratification. The same would happen around Antarctica. This limitation should be discussed or mentioned somewhere.

This atmospheric forcing aspect is, however, mentioned briefly in the conclusions.

**Authors' Response:** Thank you for pointing out this important aspect. You are correct that holding the atmospheric forcing fixed could limit the representation of feedbacks between the AMOC, heat transport, and sea ice growth. We acknowledge this limitation and will include it in the revised manuscript.

L160: See comments in L121 above.

**Authors' Response:** As mentioned in the response to L21, we will provide a quantitative comparison.

L170: In PD scenarios integrating the tidal mixing...

**Authors' Response:** Apologies for the ambiguity. I will revise this sentence to: In the PD\_tidal experiment, incorporating tidal mixing parameterization does not alter the geometry of the AMOC.

L172 Mention Table S1 here.

Thank you for your suggestion. We will mention Table S1.

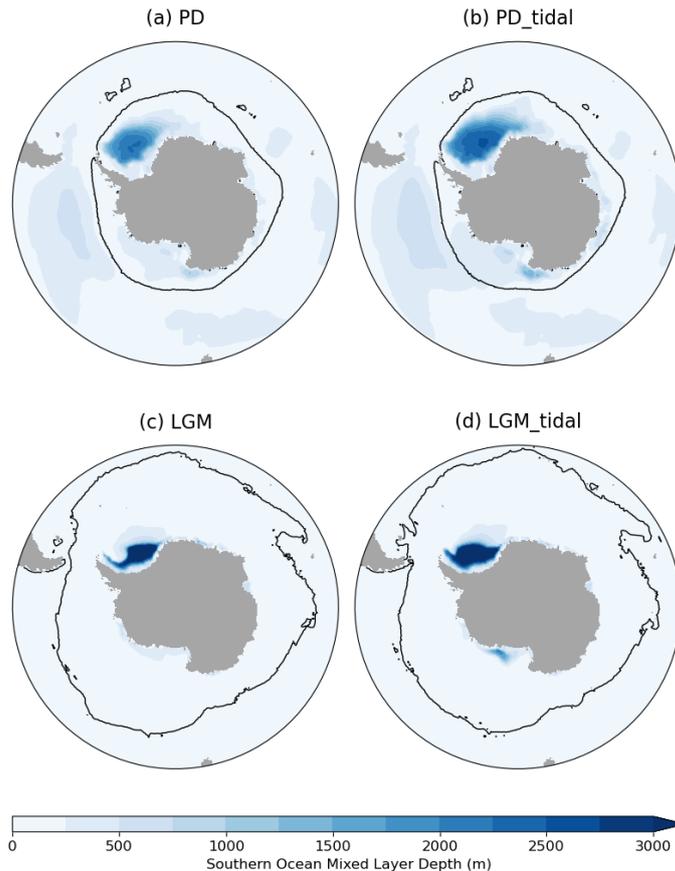
Discussions:

This is a nice result and this paper should be added to the literature on the subject. In particular as the discussions conclude, the study suggests that stronger stratification significantly reduces the impact of tidal dissipation. However, in the abyssal ocean with relatively weak stratification, the pronounced tidal dissipation during the LGM notably enhances the formation of AABW.

In paleoclimate settings, increased AABW production is often associated with a colder Antarctica and increased sea ice. From Table S1, some of the increase appears to be due to the atmospheric forcing. Maybe add a comment that since the LGM atmospheric forcing is fixed, it separates out possible effects that would occur due interactions of Southern Ocean sea ice growth on AABW formation.

Thank you for the positive evaluation. Yes, one of the important reasons for the increase in AABW during the LGM is indeed the colder background climate, which has been discussed in many papers. Therefore, we did not elaborate on this point in detail. The Figure R7 below shows the sea ice extent and MLD in the Southern Ocean for several cases in this study. It is evident that the background climate or the LGM atmospheric forcing predominantly results in a larger sea ice extent, which further facilitated the formation of AABW. At the same time, the strong tides during the LGM significantly further promoted the formation of AABW under this background.

We will add a statement in the manuscript to address the limitations of our ocean-only simulations, specifically noting that the interactions of Southern Ocean sea ice growth and AABW formation might be overlooked due to the fixed LGM atmospheric forcing.



**Figure R7.** Southern Ocean Mixed Layer Depth (MLD) and 50% sea ice concentration contour line (black) for different experiments.

***Cited literature:***

- Adkins, J. F., McIntyre, K., and Schrag, D. P.: The salinity, temperature, and delta O-18 of the glacial deep ocean, *Science*, 298, 1769-73, DOI 10.1126/science.1076252, 2002.
- Knorr, G., Barker, S., Zhang, X., Lohmann, G., Gong, X., Gierz, P., Stepanek, C., and Stap, L. B.: A salty deep ocean as a prerequisite for glacial termination, *Nat Geosci*, 14, 930+, 10.1038/s41561-021-00857-3, 2021.
- Muller, M.: Synthesis of forced oscillations, Part I: Tidal dynamics and the influence of the loading and self-attraction effect, *Ocean Modelling*, 20, 207-22, 10.1016/j.ocemod.2007.09.001, 2008.
- Osborn, T. R.: Estimates of the Local-Rate of Vertical Diffusion from Dissipation Measurements, *J Phys Oceanogr*, 10, 83-9, Doi 10.1175/1520-0485(1980)010<0083:Eotlro>2.0.Co;2, 1980.
- Schmittner, A., Green, J. A. M., and Wilmes, S. B.: Glacial ocean overturning intensified by tidal mixing in a global circulation model, *Geophys Res Lett*, 42, 4014-22, 10.1002/2015gl063561, 2015.
- Wilmes, S. B., Green, J. A. M., and Schmittner, A.: Enhanced vertical mixing in the glacial ocean inferred from sedimentary carbon isotopes, *Commun Earth Environ*, 2, ARTN 166 10.1038/s43247-021-00239-y, 2021.
- Wilmes, S. B., Schmittner, A., and Green, J. A. M.: Glacial Ice Sheet Extent Effects on Modeled Tidal Mixing and the Global Overturning Circulation, *Paleoceanography and Paleoclimatology*, 34, 1437-54, 10.1029/2019pa003644, 2019.