## SUPPLEMENTARY MATERIAL

## Miocene Antarctic ice sheet area responds significantly faster than volume to CO<sub>2</sub>-induced climate changes

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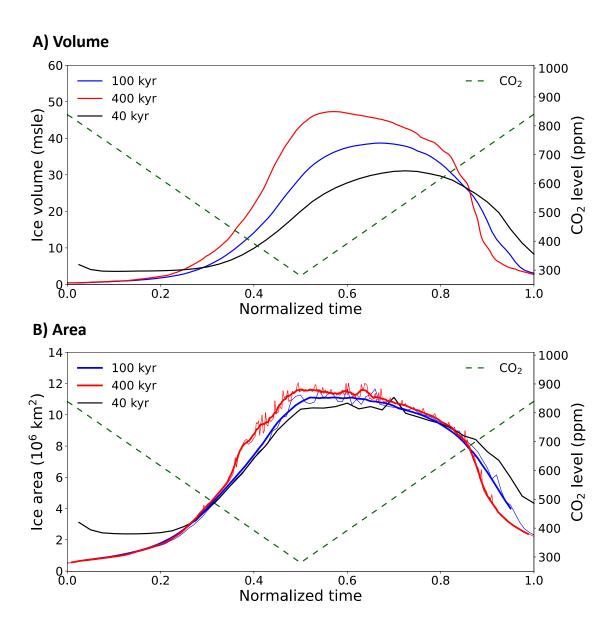
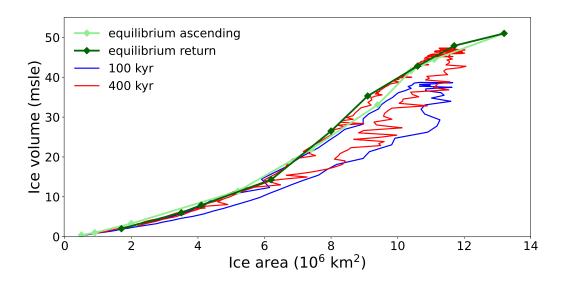
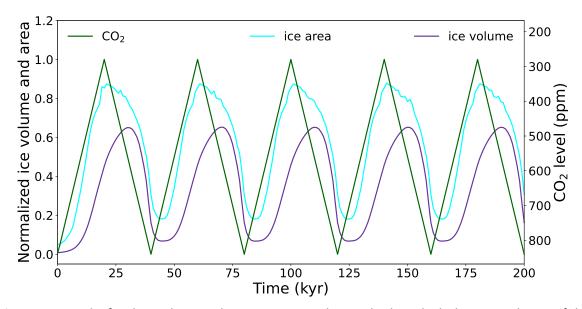


Figure S1. (A) Transient evolution of the forcing  $CO_2$  level (green dashed) and the resulting ice volume over time, normalized with respect to the maximum integration time, for the 100-kyr (blue), 400-kyr (red) simulations, and the final cycle of the 40-kyr simulation (black).

(B) Same for CO<sub>2</sub> and ice area. For the 100-kyr and 400-kyr simulations, we show the 10-kyr moving average (thick lines) in addition to the 1-kyr output (thin lines).



**Figure S2.** Ice volume plotted against ice area, for the 100-kyr (blue) and 400-kyr (red) simulations. The progression direction is counterclockwise. The connected symbols indicate the ascending branch (lightgreen) and return branch (darkgreen) equilibrium ice volume and area.



**Figure S3.** Results for the 40-kyr simulation using an index method in which the interpolation of the climate forcing is solely based on the  $CO_2$  level (NOFEEDB experiment in Stap et al., 2022). Transient evolution over time of ice area (cyan) and ice volume (purple) relative to their maximum sizes as obtained from the 280-ppm equilibrium simulation, 14.4 x  $10^6$  km² and 60.1 msle respectively. The green line shows the forcing  $CO_2$  level. The right y-axis is reversed because  $CO_2$  is generally negatively related to the benthic  $\delta^{18}O$  signal.

## Section S1

We perform an additional experiment using a model set-up representative for Pleistocene glacial-interglacial variability of the North American ice sheet, that is described in detail in Scherrenberg et al. (2023). Briefly, we deploy the updated version 2.0 of IMAU-ICE. This version uses the DIVA approach - which is slightly different from the hybrid SIA/SSA approach - to calculate the dynamics of grounded and floating ice (Berends et al., 2022). The grid covers the North American continent on a 40x40-km resolution. We carry out an equilibrium and a transient simulation like those for the Miocene Antarctic ice sheet. An equilibrium simulation is conducted at a  $CO_2$  level of 190 ppm. In the transient simulation, the  $CO_2$  level is linearly decreased from 280 to 190 ppm, and then increased back to 190 ppm. In Fig. S4, we show the forcing  $CO_2$  level and the resulting ice area and volume.

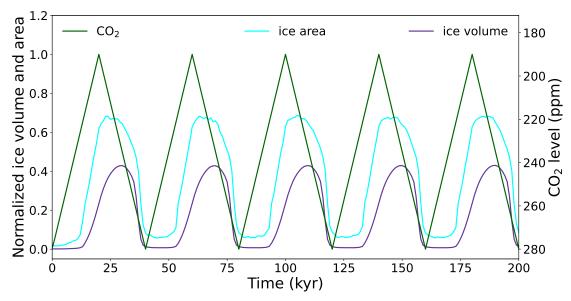


Figure S4. Results for the 40-kyr simulation of the North American ice sheet in settings representative for Pleistocene glacial-interglacial variability. Transient evolution over time of ice area (cyan) and ice volume (purple) relative to their maximum sizes as obtained from the 190-ppm equilibrium simulation,  $15.5 \times 10^6 \text{ km}^2$  and 98.9 msle respectively. The green line shows the forcing  $\text{CO}_2$  level. The right y-axis is reversed because  $\text{CO}_2$  is generally negatively related to the benthic  $\delta^{18}\text{O}$  signal.

## <u>REFERENCES</u>

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