## Supplementary figures



**Fig. S1.** The calcareous nannofossil total number (CNTN) and the relative abundances of main species of core MD77-176 over the last 26 kyr. The main coccolith species are *F. profunda*, *Emiliania huxleyi*, *Gephyrocapsa oceanica* and small *Gephyrocapsa* (*Gephyrocapsa* spp. <3μm). A few subtropical specimens can be observed and include Oolithotus spp., Pontosphaera spp., *Rhabdosphaera* spp., *Umbellosphaera* spp., *Calciosolenia* spp. and *Scyphosphaera* spp. Other species such as *Ceraolithus* spp. and *Calcidiscus* spp. are very rare (thus not shown here).



**Fig. S2.** (a) Relative abundance of *F. profunda* at site MD77-176; (b) Calcualted primary productivity based on the Indian Ocean equation (PP-IO\_HA) (red line) and the global equation (PP-G\_HA) (blue line) of Hernández-Almeida et al., (2019); and based on the Arabian Sea equation (PP-AS\_LB) (green line) of Beaufort et al., (1997). The black dash line marks the modern value of averaged PP in the region surrounding core MD77-176 (see Fig. 1).



**Fig. S3.** Differences of climatic and oceanic parameters between the experiments LGMc and LGMf, and between the experiments MH and CTRL run with IPSL-CM5A-LR. ANN=annual mean, JJA= mean of summer months (from July to Auguest).



**Fig. S4.** Differences of climatic and oceanic parameters between the MH and LH in the TraCE, and between the MH and LH in the ORB.



**Fig. S5.** Differences of climatic and oceanic parameters between the LGM in the TraCE simulation and the HS1 in the MWF, and between the LGM and HS1 in the TraCE.



**Fig. S6.** Differences of climatic and oceanic parameters between the B-A and HS1 in the TraCE, and between the B-A and HS1 in the MWF.



**Fig. S7.** Analyzed area for modeling. The bathymetric map was created by the Ocean Data View software (©Reiner Schlitzer, Alfred Wegener Institute) with its built-in global high resolution bathymetric data (GlobHR). Blue crosses mark the studied grids of oceanic outputs of TraCE-21 (Fig. 5, Fig. S8). Pink crosses mark the grids of the results shown by Fig. 7 and 8. The red dot marks the core MD77-176.



**Fig. S8.** Annual SSS (a) and annual potential density difference between 200 and 5 m ( $\Delta$ PD) in TraCE-21 simulation (ALL) and single forcing experiments. The single forcing experiments are with other forcing fixed at their values at 19 kyr BP and forced by changing orbital insolation (ORB), green-house gas concentration (GHG), meltwater flux (MWF) and ice sheet (ICE).