- 1 **OPTiMAL:** A new machine learning approach for GDGT-based palaeothermometry
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16 Abstract

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18 In the modern oceans, the relative abundances of Glycerol dialkyl glycerol tetraether (GDGTs) compounds 19 produced by marine archaeal communities show a significant dependence on the local sea surface 20 temperature at the site of deposition. When preserved in ancient marine sediments, the measured 21 abundances of these fossil lipid biomarkers thus have the potential to provide a geological record of long-22 term variability in planetary surface temperatures. Several empirical calibrations have been made between 23 observed GDGT relative abundances in late Holocene core top sediments and modern upper ocean 24 temperatures. These calibrations form the basis of the widely used TEX_{86} palaeothermometer. There are, 25 however, two outstanding problems with this approach, first the appropriate assignment of uncertainty to 26 estimates of ancient sea surface temperatures based on the relationship of the ancient GDGT assemblage to 27 the modern calibration data set; and second, the problem of making temperature estimates beyond the range 28 of the modern empirical calibrations (>30 °C). Here we apply modern machine-learning tools, including 29 Gaussian Process Emulators and forward modelling, to develop a new mathematical approach we call 30 OPTiMAL (Optimised Palaeothermometry from Tetraethers via MAchine Learning) to improve 31 temperature estimation and the representation of uncertainty based on the relationship between ancient 32 GDGT assemblage data and the structure of the modern calibration data set. We reduce the root mean 33 square uncertainty on temperature predictions (validated using the modern data set) from ~± 6 °C using 34 TEX₈₆ based estimators to \pm 3.6 °C using Gaussian Process estimators for temperatures below 30 °C. We 35 also provide a new quantitative measure of the distance between an ancient GDGT assemblage and the 36 nearest neighbour within the modern calibration dataset, as a test for significant non-analogue behaviour.

37 Finally, we advocate caution in the use of temperature estimates beyond the range of the modern empirical

calibration dataset, given the lack of a robust predictive biological model or extensive and reproducible
mesocosm experimental data in this elevated temperature range.

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41 1. Introduction

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43 Glycerol dibyphytanyl glycerol tetraethers (GDGTs) are membrane lipids consisting of isoprenoid carbon 44 skeletons ether-bound to glycerol (Schouten et al., 2013). In marine systems they are primarily produced by ammonia oxidising marine Thaumarchaeota (Schouten et al., 2013). In modern marine core top 45 46 sediments, the relative abundance of GDGT compounds with more ring structures increases with the mean 47 annual sea surface temperature (SST) of the overlying waters (Schouten et al., 2002). This trend is most 48 likely driven by the need for increased cell membrane stability and rigidity at higher temperatures 49 (Sinninghe Damsté et al., 2002). On this basis, the TEX_{86} (tetraether index of tetraethers containing 86 50 carbon atoms) ratio was derived to provide an index to represent the extent of cyclisation (Eq. 1; where 51 GDGT-x represents the fractional abundance of GDGT-x determined by liquid chromatography mass 52 spectrometery (LC-MS) peak area, and cren' is the peak area of the isomer of crenarchaeol) (Schouten et 53 al., 2002; Liu et al. 2018) and was shown to be positively correlated with mean annual SSTs:

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55 $TEX_{86} = (GDGT-2 + GDGT-3 + cren^2)/(GDGT-1 + GDGT-2 + GDGT-3 + cren^2)$ (Eq. 1)

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57 Early applications of TEX₈₆ to reconstruct ancient SSTs were promising, especially in providing 58 temperature estimates in environments where standard carbonate-based proxies are hampered by poor 59 preservation (Schouten et al., 2003; Herfort et al., 2006; Schouten et al., 2007; Huguet et al., 2006; Sluijs 60 et al., 2006; Brinkhuis et al., 2006; Pearson et al., 2007; Slujis et al., 2009). The TEX₈₆ approach also extended beyond the range of the widely used alkenone-based $U^{k'_{37}}$ thermometer, in both temperature space, 61 62 where $U^{k'_{37}}$ saturates at ~28°C (Brassell, 2014; Zhang et al., 2017), and back into the early Cenozoic (Bijl 63 et al., 2009; Hollis et al., 2009; Bijl et al., 2013; Inglis et al., 2015) and Mesozoic (Schouten et al., 2002; 64 Jenkyns et al., 2012; O'Brien et al., 2017) where haptophyte-derived alkenones are typically absent from 65 marine sediments (Brassell, 2014). Initially, TEX₈₆ was converted to SSTs using the core-top calibration 66 (Schouten et al. 2002) (Eq. 2):

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68 $TEX_{86} = 0.015*SST+0.287$ (Eq. 2)

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70 However as the number and range of applications of TEX₈₆ palaeothermometry grew, concerns arose about 71 proxy behaviour at both the high (Liu et al., 2009) and low (Kim et al., 2008) temperature ends of the 72 modern calibration. In response to these observations, a new expanded modern core top dataset (Kim et al., 73 2010) was used to generate two new indices – TEX_{86}^{L} (Eq. 3), an exponential function that does not include 74 the crenarchaeol regio-isomer and was recommended for use across the entire temperature range of the new core top data (-3 to 30 °C, particularly when SSTs are lower than 15 °C), and TEX^H₈₆ (Eq. 4), also 75 exponential, and recommended for use when SSTs exceeded 15 °C (Kim et al., 2010). TEX^L₈₆ also excludes 76 77 GDGT abundance data from the high-temperature regimes of the Red Sea, which are somewhat anomalous 78 and likely related to salinity effects on community composition in this region (Trommer et al., 2009, Kim 79 et al. 2010).

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$$TEX_{86}^{L} = log\left(\frac{[GDGT2]}{[GDGT1] + [GDGT2] + [GDGT3]}\right)$$
 Eq. 3

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$$TEX_{86}^{H} = log\left(\frac{[GDGT2] + [GDGT3] + [Cren']}{[GDGT1] + [GDGT2] + [GDGT3] + [Cren']}\right)$$
 Eq. 4

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Despite the recommendations of Kim et al. (2010), both TEX_{86}^{H} and TEX_{86}^{L} were widely used and tested 86 87 across a range of temperatures and palaeoenvironments, including comparisons against other 88 palaeotemperature proxy systems (Hollis et al. 2012; Lunt 2012 Dunkley Jones et al. 2013; Zhang et al., 89 2014; Seki et al., 2014; Douglas et al., 2014; Linnert et al., 2014; Hertzberg et al., 2016). The rationale was that both TEX_{86}^{L} and TEX_{86}^{H} were calibrated across a full temperature range, with the exception of the 90 91 inclusion or exclusion of Red Sea core-top data. The difference in model fit between the two proxy 92 formulations to the calibration dataset was also minor (Kim et al. 2010). In certain environments, however, TEX_{86}^{L} was subject to significant variability in derived temperatures that were not apparent in TEX_{86}^{H} 93 94 (Taylor et al., 2013). This was mostly due to changing GDGT2 to GDGT3 ratios, which strongly influence 95 TEX_{86}^{L} , and may be related to local non-thermal environmental conditions at the site of GDGT production, and deep-water lipid production, (Taylor et al., 2013). As a result, TEX_{86}^{L} is no longer regarded as an 96 97 appropriate tool for palaeotemperature reconstructions, except in limited Polar conditions (Kim et al., 2010; 98 Tierney, 2012).

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100 Three fundamental issues have troubled the TEX_{86} proxy. The first is a concern about undetected non-101 analogue palaeo-GDGT assemblages, for which the modern calibration data set is inadequate to provide a 102 robust temperature estimation. Although various screening protocols, with independent indices and

103 thresholds, have been proposed to test for an excessive influence of terrestrial lipids (Branched and 104 Isoprenoid Tetraether, BIT index; Hopmans et al., 2004), within sediment methanogenesis (Methane Index, 105 'MI'; Zhang et al., 2011) and non-thermal effects such as nutrient levels and archaeal community structure 106 to impact the weighted average of cyclopentane moieties (Ring Index, 'RI;' Zhang et al., 2016), these do 107 not provide a fundamental measure of the proximity between GDGT abundance distributions in the modern, 108 and ancient GDGT abundance distributions recorded in sediment samples. The fundamental question 109 remains – are measured ancient assemblages of GDGT compounds anything like the modern assemblages, 110 from which palaeotemperatures are being estimated? Understanding this question cannot easily be 111 addressed with the use of indices – TEX₈₆ itself, or BIT and MI – that collapse the dimensionality of GDGT 112 abundance relationships onto a single axis of variation.

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114 Second, from the earliest applications of the TEX_{86} proxy to deep-time warm climate states (Schouten et 115 al., 2003) it was recognized that reconstructed temperatures beyond the range of the modern calibration 116 (>30 °C), were highly sensitive to model choice within the modern calibration range. Thus, Schouten et al. (2003) restricted their calibration data for deep-time temperature estimates to core-top data in the modern 117 118 with mean annual SSTs over 20 °C. However, this problem of model choice, and its impact on temperature 119 estimation beyond the modern calibration range, persists (Hollis et al. 2019), with current arguments 120 focused on whether there is an exponential (e.g. Cramwinckel et al., 2018) or linear (Tierney & Tingley, 121 2015) dependency of TEX₈₆ on SSTs, and the effect of these models on temperature estimates over 30 $^{\circ}$ C. 122

123 Culture and mesocosm studies are sometimes cited in support of extrapolations beyond the modern 124 calibration range when reconstructing ancient SSTs (Kim et al., 2010, Hollis et al., 2019). While there is a 125 basic underlying trend for more rings within GDGT structures at higher temperatures (Zhang et al. 2015; 126 Qin et al., 2015), the lack of a uniform response to archaeal GDGT production in response to increasing 127 growth temperatures (e.g., Elling et al., 2015; Qin et al., 2015) suggests that this does not easily translate 128 into a simple linear model at the community scale (i.e. the core top calibration dataset). Wuchter et al. 129 (2004) and Schouten et al. (2007) show a compiled linear calibration of TEX₈₆ against incubation 130 temperature (up to 40°C in the case of Schouten et al., 2007) based on strains that were enriched from 131 surface seawater collected from the North Sea and Indian Ocean respectively. Like Qin et al. (2015), we 132 note the *non*-linear nature of the individual experiments in Wuchter et al. (2004; see Fig. 5). Moreover, the 133 relatively lower Cren' in these studies yield a very different intercept and slope compared to core-top 134 calibrations (e.g. Kim et al. 2010) making direct comparisons problematic.

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137 More recently, Elling et al. (2015) studied three different strains (N. maritimus, NAOA6, NAOA2) isolated 138 from open ocean surface waters (South Atlantic) whilst Qin et al., (2015) studied a culture of N. maritimus 139 and three N. maritimus-like strains isolated from Puget Sound. All strains are of marine, mesophilic, 140 Thaumarchaeota within Marine Group 1 (equivalent to Crenarchaeota Group 1). Both of these papers 141 clearly demonstrate distinctly different responses of membrane lipid composition to temperature in these 142 strains, whilst Qin et al. (2015) additionally show that oxygen concentration is at least as important as 143 temperature in controlling TEX₈₆ values in culture. The impact of Thaumarchaeota community change on 144 TEX₈₆ in palaeoclimate studies is further suggested by the downcore study of Polik et al (2019). All of these 145 culture studies, made on marine, mesophilic archaea demonstrate how community composition may have 146 a significant impact on measured environmental TEX_{86} signatures. In these cases (e.g., Zhang et al. 2015; 147 Qin et al., 2015; Elling et al., 2015) cultured strains of Thaumarcheota were obtained from surface waters 148 which overlie the epi-continental or continental shelf regions of the North Sea, Indian Ocean, South Atlantic 149 and North Pacific - in addition to the pure culture strain N. maritimus in Qin et al. (2015) and Elling et al. 150 (2015). As such, these are collectively more representative of the community production contributing to 151 samples in the global core-top TEX₈₆ calibrations of Kim et al., (2010) and BAYSPAR (Tierney & Tingley, 152 2014), which predominantly sample continental margin environments, rather than deep ocean / pelagic 153 environments.

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155 It is clear from the above discussion that there is evidence for more complex responses in GDGT-production 156 to growth temperature in some instances, and across distinct strains of archaea (Elling et al., 2015). More 157 fundamentally, in natural systems, it is likely that aggregated GDGT abundance variations in response to 158 growth temperatures result from changing compositions of archaeal populations as well as the physiological 159 response of individual strains to growth temperature (Elling et al. 2015). For instance, a multiproxy study 160 of Mediterranean Pliocene-Pleistocene sapropels indicates that specific distributions of archaeal lipids 161 might be reflective of temporal changes in thaumarchaeael communities rather than temperature alone 162 (Polik et al., 2018). Indeed, the potential influence of community switching on GDGT composition can be 163 seen in mesocosm studies, with different species preferentially thriving at different growth temperatures 164 (e.g., Schouten et al., 2007). To use the responses of single, selected archaeal strains in culture to validate 165 a particular model of community-level responses to growth temperature is problematic even in the modern 166 system (Elling et al., 2015). For deep time applications it is even more difficult, where there is no 167 independent constraint on the archaeal strains dominating production or their evolution through time (Elling 168 et al. 2015). What is notable, however, is that the Ring Index (RI) - calculated using all commonly measured 169 GDGTs (Zhang et al., 2016) – has a more robust relationship with culture temperature between archaeal 170 strains than TEX₈₆, indicating a potential loss of information within the TEX₈₆ index (Elling et al. 2015).

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172 Finally, the original uses of the TEX₈₆ proxy had a relatively poor representation of the true uncertainty 173 associated with palaeotemperature estimates, as they included no assessment of non-analogue behavior 174 relative to the modern core-top data. Instead, uncertainty was typically based on the residuals on the modern 175 calibration, with no reference to the relationship between GDGT distributions of an ancient sample and the 176 modern calibration data. An improved Bayesian uncertainty model "BAYSPAR" is now in widespread use 177 for SST estimation, which models TEX₈₆ to SSTs regression parameters, and associated uncertainty, as 178 spatially varying functions (Tierney and Tingley, 2015). The Bayesian approach, as with all approaches 179 based on the TEX₈₆ index, however, still does not include an uncertainty that reflects how well modelled 180 ancient GDGT assemblages are by the modern calibration -i.e. the degree to which they are non-analogue 181 - as it still functions on one-dimensional TEX₈₆ index values.

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183 All empirical calibrations of GDGT-based proxies assume that mean annual SST is the master variable on 184 GDGT assemblages both today and in the past. Mean annual SST, however, is strongly correlated with 185 many other environmental variables (e.g., seasonality, pH, mixed layer depth, and productivity). In the 186 modern calibration dataset, mean annual SST shows the strongest correlation with TEX₈₆ index (Schouten 187 et al., 2002), but this does not preclude an important (but undetectable) influence of these other 188 environmental variables. The use of empirical GDGT calibrations to infer ancient sea surface temperatures 189 thus implicitly assumes that the relationships between mean annual SST and all other GDGT-influencing 190 variables are invariant through time. This assumption is inescapable until, and unless, a more complete 191 biological mechanistic model of GDGT production emerges.

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193 Here, we return to the primary modern core-top GDGT assemblage data (Tierney and Tingley, 2015), and 194 systematically explore the relationships between the modern GDGT distributions and surface ocean 195 temperatures using powerful mathematical tools. These tools can investigate correlations without prior 196 assumptions on the best form of relationship or a priori selection of GDGT compounds to be used. This 197 analysis is then extended through the exploration of the relationships between the modern core top GDGT 198 distributions and two compilations of ancient GDGT datasets, one from the Eocene (Inglis et al. 2015) and 199 one from the Cretaceous (O'Brien et al. 2017). We explore simple metrics to answer the fundamental 200 question – are modern core-top GDGT distributions good analogues for ancient distributions? We propose 201 the first robust methodology to answer this question, and so screen for significantly non-analogue palaeo-202 assemblages. From this, we go on to derive a new machine learning approach 'OPTiMAL' (Optimised 203 Palaeothermometry from Tetraethers via MAchine Learning) for reconstructing SSTs from GDGT

datasets, which outperforms previous GDGT palaeothermometers and includes robust error estimates that,for the first time, accounts for model uncertainty.

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207 2. Models for GDGT-based Temperature Reconstruction

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209 Our new analyses use the modern core-top data compilation, and satellite-derived estimates of SSTs, of 210 Tierney and Tingley (2015) as well as compilations of Eocene (Inglis et al. 2015) and Cretaceous (O'Brien 211 et al. 2017) GDGT assemblages. Within these fossil assemblages, only data points with full characterisation 212 of individual GDGT relative abundances were used. We also note that, in the first instance, all available 213 fossil assemblage data were included, although later comparisons between BAYSPAR and our new 214 temperature predictor excludes fossil data that was regarded as unreliable based on standard pre-screening 215 indices, as noted within the original compilations (Inglis et al. 2015; O'Brien et al. 2017). All data used in 216 this study are tabulated in the supplementary information.

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In order to enable meaningful comparison between new and existing temperature predictors, we use the following consistent procedure for evaluating all predictors throughout this paper. We divide the modern core-top data set of 854 data points into 85 validation data points (chosen randomly) and 769 calibration points (as we require fractional abundances for all 6 commonly measured GDGTs, we excluded those data points for which these values were not reported). We calibrate the predictor on the calibration points, and then judge its performance on the validation points using the root mean square error:

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$$\delta T = \sqrt{\frac{1}{N_v - 1} \sum_{k=1}^{N_v} (\hat{T}(x_k) - T(x_k))^2}$$
226 (Eq. 5)

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where the sum is taken over each of $N_v = 85$ validation points, T is the known measured temperature (which we refer to as the true temperature) and \hat{T} is the predicted temperature. For conciseness, we refer to δT as the predictor standard error. It is useful to compare the accuracy of the predictor to the standard deviation of all temperatures in the data set σT , which corresponds to using the mean temperature as the predictor in Equation 1; for the modern data set, $\sigma T = 10.0$ °C. The coefficient of determination, R^2 , provides a measure of the fraction of the fluctuation in the temperature explained by the predictor. To facilitate performance comparisons between different methods of predicting temperature, we use the same subset of validation points for all analyses. To avoid sensitivity to the choice of validation points, we repeat the calibration-validation procedure for 10 random choices from the validation dataset.

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238 2.1 Nearest neighbours

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240 We begin with an agnostic approach to using some combination of the proportions of each of the six 241 observables - GDGT-0, GDGT-1, GDGT-2, GDGT-3, crenarchaeol and cren', which we will jointly refer 242 to as GDGTs - to predict sea surface temperatures. Whatever functional form the predictor might take, it 243 can only provide accurate temperature predictions if nearby points in the six-dimensional observable space 244 - i.e. the distribution of all of the six commonly reported GDGTs - can be translated to nearby points in 245 temperature space. Conversely, if nearby points in the observable space correspond to vastly different 246 temperatures, then no predictor, regardless of which combination of GDGTs are used, will be able to 247 provide a useful temperature estimate. In other words, the structuring of GDGT distributions within multi-248 dimensional space, must have some correspondence to the temperatures of formation (or rather the mean 249 annual SSTs used for standard calibrations).

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251 We therefore consider the prediction offered by the temperature at the nearest point in the GDGT parameter 252 space. Of course, nearness depends on the choice of the distance metric. For example, it may be that sea 253 surface temperatures are very sensitive to one observable, so even a small change in that observable 254 corresponds to a significant distance, and rather insensitive to another, meaning that even with a large 255 difference in the nominal value of that observable the distance is insignificant. In the first instance, we use 256 a very simple Euclidian distance estimate $D_{x,y}$ where the distance along each observable is normalised by 257 the total spread in that observable across the entire data set. This normalisation ensures that a dimensionless 258 distance estimate can be produced even when observables have very different dynamical ranges, or even 259 different units. Thus, the normalised distance D between parameter data points x and y is

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$$D_{x,y}^{2} \equiv \sum_{i=0}^{6} \frac{GDGT_{i}(x) - (GDGT_{i}(y))^{2}}{var(GDGT_{i})}$$

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We show the distribution of nearest distances of points in the modern data set, excluding the sample itself,
in (Fig. 1).

267 The nearest-sample temperature predictor is $\hat{T}_{\text{nearest}}(x) = T(y)$ where y is the nearest point to x over the 268 calibration data set, i.e., one that minimises $D_{x,y}$. Fig. 2 shows the scatter in the predicted temperature when

(Eq. 7)

269 using the temperature of the nearest data point to make the prediction. Overall, the failure of the nearest-270 neighbour predictor to provide accurate temperature estimates even when the normalised distance to the 271 nearest point is small, $D_{xy} \leq 0.5$, casts doubt on the possibility of designing an accurate predictor for 272 temperature based on GDGT observations. This is most likely due to additional environmental controls on 273 GDGT abundance distributions in natural systems, in particular the water depth (Zhang and Liu, 2018), 274 nutrient availability (Hurley et al., 2016; Polik et al., 2018; Park et al., 2018), seasonality, growth rate 275 (Elling et al., 2014; Hurley et al., 2016) and ecosystem composition (Polik et al., 2018), that obscure a 276 predominant relationship to mean annual SSTs.

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278 On the other hand, the standard error for the nearest-neighbour temperature predictor is $\delta T_{\text{nearest}} = 4.5 \text{ °C}$. 279 This is less than half of the standard deviation σT in the temperature values across the modern data set. 280 Thus, the temperatures corresponding to nearby points in GDGT observable space also cluster in 281 temperature space. Consequently, there is hope that we can make some useful, if imperfect, temperature 282 predictions. The value of $\delta T_{\text{nearest}}$ will also serve as a useful benchmark in this design: while we may hope 283 to do better by, say, suitably averaging over multiple nearby calibration points rather than adopting the 284 temperature at one nearest point as a predictor, any method that performs worse than the nearest-neighbour 285 predictor is clearly suboptimal.

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287 *2.2 TEX*₈₆ and Bayesian applications

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289 The TEX₈₆ index reduces the six-dimensional observable GDGT space to a single number. While this has 290 the advantage of convenience for manipulation and the derivation of simple analytic formulae for 291 predictors, as illustrated below, this approach has one critical disadvantage: it wastes significant information embedded in the hard-earned GDGT distribution data. Fig. 3 illustrates both the advantage and 292 293 disadvantage of TEX_{86} . On the one hand, there is a clear correlation between TEX_{86} and temperature (top 294 panel of Fig. 3), with a correlation coefficient of 0.81 corresponding to an overwhelming statistical 295 significance of 10⁻¹⁹⁸. On the other hand, very similar TEX₈₆ values can correspond to very different 296 temperatures. We can apply the nearest-neighbour temperature prediction approach to the TEX₈₆ value 297 alone rather than the full GDGT parameter space; this predictor yields a large standard error of $\delta T_{\text{nearestTEX86}}$ 298 = 8.0 °C (bottom panel of Fig. 3). While smaller than σT , this is significantly larger than $\delta T_{\text{nearest}}$ (Fig. 2), 299 consistent with the loss of information in TEX₈₆. We therefore do not expect other predictors based on 300 TEX₈₆ to perform as well as those based on the full available data set.

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Indeed, this is what we find when we consider predictors of the form $\hat{T}_{1/\text{TEX}} = a + b/\text{TEX}_{86}$ and $\hat{T}_{\text{TEXH}} = c$ 302 303 + $d \log_{\text{TEX86}}$ (Liu et al., 2009; Kim et al., 2010), i.e., the established relationships between GDGT 304 distributions and SST. We fit the free parameters a, b, c, and d by minimising the sum of squares of the 305 residuals over the calibration data sets (least squares regression). We find that $\delta T_{I/\text{TEX}} = 6.1 \text{ °C}$ (note that this is slightly better than using the fixed values of a and b from (Kim et al., 2010), which yield $\delta T_{I/\text{TEX}}$ = 306 6.2 °C). We note that the corresponding R^2 value associated with these TEX₈₆ based predictors is 0.64, 307 308 which is lower than the R^2 values in Kim et al. (2010). We attribute this to the fact that we are using a larger 309 dataset based on Tierney and Tingley (2015), including data from the Red Sea (Kim et al. 2010).

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311 Tierney and Tingley (2014) proposed a more sophisticated approach to obtaining the transfer function from 312 TEX₈₆ to temperature, continuing to use simple linear regression, but with the addition of Gaussian 313 processes to model spatial variability in the temperature-TEX₈₆ relationship and working with a forward 314 model which is subsequently inverted to produce temperature predictions. This forward model 315 'BAYSPAR' is capable of generating an infinite number of calibration curves relating TEX₈₆ to sea surface 316 temperatures (Tierney and Tingley, 2014). In order to derive a calibration for a specific dataset, the user 317 edits a range of parameters which vary depending on whether the dataset in question is from the relatively 318 recent past or deep time (Tierney and Tingley, 2014). For deep time applications, the authors propose a 319 modern analogue-type approach, in which they search the modern data for 20° x 20° grid boxes containing 320 'nearby' TEX₈₆ measurements and subsequently apply linear regression models calibrated on the analogous 321 samples for making predictions.

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323 However, along with the simpler TEX₈₆-based models described above, this approach still suffers from the 324 reduction of a six-dimensional data set to a single number. Therefore, it is not surprising that even the 325 simplest nearest-neighbour predictor (such as the one described above) that makes use of the full six-326 dimensional dataset outperforms single-dimensional forward modelling approaches. Additionally, 327 uncertainty estimates do not account for the fact that TEX_{86} is, fundamentally, an empirical proxy, and so 328 its validity outside the range of the modern calibration is not guaranteed. This is a fundamental issue for 329 attempts to reconstruct surface temperatures during Greenhouse climate states, when tropical and sub-330 tropical SSTs were likely hotter than those observed in the modern oceans.

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332 2.3 Machine learning Approaches – Random Forests

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There are a number of options to improve on nearest-neighbour predictions using machine learningtechniques such as artificial neural networks and random forests. These flexible, non-parametric models

336 would ideally be based on the underlying processes driving the GDGT response to temperature, but since 337 these processes remain unconstrained at present, we choose to deploy models which can reasonably reflect 338 predictive uncertainty and will be sufficiently adaptable in future (as new information regarding controls 339 on GDGTs emerge). These machine learning approaches are all based on the idea of training a predictor by 340 fitting a set of coefficients in a sufficiently complex multi-layer model in order to minimise residuals on 341 the calibration data set. As an example of the power of this approach, we train a random forest of decision 342 trees with 100 learning cycles using a least-squares boosting to fit the regression ensemble. Figure 4 shows 343 the prediction accuracy for this random forest implementation. This machine learning predictor yields δT 344 = 4.1 °C degrees, outperforming the naive nearest-neighbour predictor by effectively applying a suitable 345 weighted average over multiple near neighbours. This corresponds to a very respectable $R^2 = 0.83$, meaning 346 that 83% of the variation in the observed temperature is successfully explained by our GDGT-based model.

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348 2.4 Gaussian Process Regression

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350 One downside of the random forest predictor is the difficulty of accurately estimating the uncertainty on 351 the prediction (Mentch and Hooker, 2016), although this is possible with, e.g., a bootstrapping approach 352 (Coulston et al., 2016). Fortunately, Gaussian process (GP) regression provides a robust alternative. For 353 full details on GP regression refer to Williams and Rasmussen (2006) and Rasmussen and Nickisch (2010). 354 Loosely, the objective here is to search among a large space of smoothly varying functions of GDGT 355 compositions for those functions which adequately describe temperature variability. This, essentially, is a 356 way of combining information from all calibration data points, not just the nearest neighbours, assigning 357 different weights to different calibration points depending on their utility in predicting the temperature at 358 the input of interest. The trained Gaussian process learns the best choice of weights to fit the data. Typically, 359 the GP will give greater weight to closer points, but, as we discuss below, it will learn the appropriate 360 distance metric on the multi-dimensional GDGT input space.

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362 The weighting coefficients learned by the GP emulator represent a covariance matrix on the GDGT 363 parameter space. We can use this as a distance metric to provide meaningfully normalised distances 364 between points, removing the arbitrariness from the nearest neighbour distance $(D_{x,y})$ definition used 365 earlier. If the temperature is insensitive to a particular GDGT input coordinate (i.e., the value of that input 366 has a minimal effect on the temperature) then points within GDGT space that have large differences in 367 absolute input values in that coordinate are still near. We find that Cren has very limited predictive power, 368 and so points with large Cren differences are close in term of the normalised distance. Conversely, if the 369 temperature is sensitive to small changes in a particular GDGT variant, then points with relatively nearby

370 absolute input values in that coordinate are still distant. We find that most GDGT parameters other than 371 Cren are comparably useful in predicting temperature, with GDGT-0 and GDGT-3 marginally the most 372 informative. We considered whether interdependency of percentage GDGT data could influence our 373 calculations. Our analysis suggests that there are only five free parameters. Machine learning tools should 374 be able to pick up this correlation and effectively ignore one of the parameters (or one parameter 375 combination). For example, we do find that the GP emulator has a very broad kernel in at least one 376 dimension, signaling this. In principle, we could have considered only five of six parameters. The smaller 377 scale of some of the parameters is automatically accounted for by the trained kernel size in GP regression, 378 or by normalising to the appropriate dynamical range in our initial investigation.

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380 We use a Gaussian process model with a squared exponential kernel with automatic relevance 381 determination (ARD) to allow for a separate length scale for each GDGT predictor. We fit the GP 382 parameters with an optimiser based on quasi-Newton approximation to the Hessian. Prediction accuracy is shown in Figure 5, and we find that $\delta T = 3.72$ °C, which is a substantial improvement over the existing 383 384 indices, at least on the modern data. As mentioned, the GP framework provides a natural quantification of 385 predictive uncertainty, which includes uncertainty about the learned function. This is in contrast to, for 386 example, the TEX₈₆ proxy, whereby the uncertainty associated with the selection of the particular functional 387 form used for predictions is ignored. While Tierney & Tingley (2014) also use Gaussian processes to model 388 uncertainty, they model spatial variability in the TEX_{86} -temperature relationship with a Gaussian process 389 prior. While this is a valuable approach to understand regional effects in the TEX_{86} -temperature 390 relationship, it does not deal with the `non-analogue' situations we are concerned with in this paper.

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392 2.5 Data Structure

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394 The random forest (Section 2.3) and GPR approaches (Section 2.4) are agnostic about any underlying bio-395 physical model that might impart the observed temperature-dependence on GDGT relative abundances 396 produced by archaea. They are essentially optimized interpolation tools for mapping correlations between 397 temperature and GDGT abundances within the range of the modern calibration data set; they can make no 398 sensible inference about the behavior of this relationship outside of the range of this training data. To move 399 from interpolation within, to extrapolation beyond, the modern calibration requires an understanding of, 400 and model for, the temperature-dependence of GDGT production. To explore these relationships and the 401 extent to which the ancient and modern data reside in a coherent relationship within GDGT space, we 402 employed two forms of dimensionality reduction to enable visualisation of the data in two or three 403 dimensions. The fundamental point is that if temperature is the dominant control, all of the data should lie

404 approximately on a one-dimensional curve in GDGT space, and the arclength along this curve should405 correspond to temperature; we will revisit this point below.

406

407 We first employed a version of principal component analysis (PCA) tailored to compositional data 408 (Aitcheson, 1982, 1983; Aitcheston and Greenacre, 2002; Filzmoser et al., 2009a; Filzmoser et al., 2009b; 409 Filzmoser et al., 2012). Taking into account the compositional nature of the data is important because the 410 sum-to-one constraint induces correlations between variables which are not accounted for by classical PCA. 411 Furthermore, apparently nonlinear structure in Euclidean space often corresponds to linearity in the simplex 412 (i.e. the restricted space in which all elements sum to one) (Egozcue et al., 2003). Figure 6 shows the 413 modern. Eocene and Cretaceous data projected onto the first two principal components. Aside from the 414 obvious outlying cluster of Cretaceous data, characterised by GDGT-3 fractions above 0.6, the bulk of the 415 data occupy a two-dimensional point cloud with a small amount of curvature. The large majority of the 416 Cretaceous data has more positive PC1 values relative to the modern data.

417

418 We also explored the data using diffusion maps (Coifman et al., 2005; Haghverdi et al., 2015), a nonlinear 419 dimensionality reduction tool designed to extract the dominant modes of variability in the data. Such 420 diffusion maps have been successfully used to infer latent variables that can explain patterns of gene 421 expression. In the case of biological organisms, this latent variable is commonly developmental age (called 422 pseudo-time) (Haghverdi et al., 2016). In our case, the assumption would be that this latent variable 423 corresponds to temperature. Inspection of the eigenvalues of the diffusion map transition matrix suggests 424 that four diffusion components are adequate to represent the data; we plot the second, third and fourth of 425 these components in Figure 7 for the modern and ancient data. The separate clusters marked `A' are the 426 outlying Cretaceous points with high GDGT-3 values. The bulk of the modern data lies on the branch 427 marked 'B', while the bulk of the Cretaceous data lies on the branch marked 'C'. Notably, the majority of 428 the modern points lying on branch C are from the Red Sea, which suggests that the Red Sea data is essential 429 for understanding ancient climates (particularly Cretaceous climates).

430

The relationship between the first diffusion component and TEX_{86} for all data is shown in Figure 8. There is a clear correlation, despite the presence of some outlying Cretaceous points, some of which are not shown because they lie so far outside the majority data range within this projection. This suggests that TEX_{86} is, in one sense, a natural one-dimensional representation of the data. We also plot the first diffusion component for the modern data as a function of temperature (Figure 9). We see a similar pattern emerging to that displayed by TEX_{86} - there is little sensitivity to temperature below 15 °C, and between ~20 and 25 °C. An interesting avenue for future research might be to explore the temperature-GDGT system from a 438 dynamical systems perspective, i.e. use simple mechanistic mathematical models to explore the 439 temperature-dependence of steady-state GDGT distributions. It may be that such models suggest that only 440 a few steady-states exist, and that temperature is a bifurcation parameter, i.e. it controls the switch between 441 the steady states. Note also the downward slope in the residual pattern in Figure 4 between 0 and 15-17 442 degrees celsius, and again at higher temperatures. This pattern is consistent with predictions that are biased 443 towards the centre of each `cluster', i.e. a system which is not very sensitive to temperature, but can 444 distinguish between high and low temperatures reasonably well. This observation also links to recent culture 445 studies (Elling et al., 2015) and Pliocene-Pleistocene sapropel data (Polik et al., 2018), which support the 446 existence of discrete populations with unique GDGT-temperature relationships and that temporal changes 447 in population over time can drive changes in TEX_{86} .

448

449 2.6 Forward Modelling

450

451 Based on the analysis of the combined modern and ancient data structure outlined above, there appears to 452 be some consistency to underlying trends in the overall variance of GDGT relative abundances. These 453 trends provide some hope that models of this variance, and its relationship to sea surface temperature, within 454 the modern dataset could be developed to predict ancient SSTs. TEX_{86} and BAYSPAR are such models, 455 but they are limited by, first, the reduction of six-dimensional GDGT space to a one-dimensional index; 456 and second, by an *ad hoc* model choice – linear, exponential – that does not account for uncertainty in 457 model fit to the modern calibration data, and the resultant uncertainty in the estimation of ancient SSTs 458 relating to model choice. To overcome these issues, we develop a forward model based on a multi-output 459 Gaussian Process (Alvarez et al., 2012), which models GDGT compositions as functions of temperature, 460 accounting for correlations between GDGT measurements. This model is then inverted to obtain 461 temperatures which are compatible with a measured GDGT composition. In simple terms, we posit that a 462 measured GDGT composition is generated by some unknown function of temperature and corrupted by 463 noise, which may be due to measurement error or some unmodelled particularity of the environment in 464 which the sample was generated. We proceed by defining a large (in this case infinite) set of functions of 465 temperature to explore and compare them to the available data, throwing away those functions which do 466 not adequately fit the data. This means, of course, that the behaviour of the functions we accept is allowed 467 to vary more widely outside the range of the modern data than within it. With no mechanistic underpinning, 468 choosing only one function (such as the inverse of TEX₈₆) based on how well it fits the modern data grossly 469 underestimates our uncertainty about temperature where no modern analogue is available.

470

471 The forward modelling approach is similar to that of Haslett et al. (2006), who argue that it is preferable to 472 model measured compositions as functions of climate, before probabilistically inverting the model to infer 473 plausible climates given a composition. The cost of modelling the data in this more natural way is the loss 474 of degrees of freedom -- we are now attempting to fit a one-dimensional line through a multidimensional 475 point cloud rather than fit a multidimensional surface to the GDGT data, which means that the predictive 476 power of the model suffers, at least on the modern data. The existing BAYSPAR calibration also specifies 477 the model in the forward direction, however while BAYSPAR does model spatial variability, it does not 478 account for the systematic uncertainty in the model when extrapolated beyond the calibration range. As 479 with all GP models, the choice of kernel has a substantial impact on predictions (and their associated 480 uncertainty) outside the range of the modern data, where predictions revert to the prior implied by the 481 kernel. Given that we have no mechanistic model for the data generating process, we recommend the use 482 of kernels which do not impose strong prior assumptions on the form of the GDGT-temperature relationship 483 (e.g. kernels with a linear component) and thus reasonably represent model uncertainty outside the range 484 of the modern data. We choose a zero-mean Matern 3/2 kernel for the applications below. Note, however, 485 that since we are working in ilr-transformed coordinates, this corresponds to a prior assumption of uniform 486 compositions at all temperatures, i.e. all components are equally abundant.

487

The residuals for the forward model are shown in Figure 10. The clear pattern in the residuals does not necessarily indicate model misspecification, since no explicit noise model is specified for temperatures. Predictive distributions are to be interpreted in the Bayesian sense, in that they represent a 'degree of belief' in temperatures given the model and the modern data. The residual pattern is similar to that of the random forest (Figure 4) with two clear downward slopes, suggesting again that the data are clustered into temperatures above and below 16-17 degrees celsius, and that predictions tend towards temperatures at the centres of these clusters.

495

496 An advantage of the forward modelling approach is that the inversion can incorporate substantive prior 497 information about temperatures for individual data points. In particular, other proxy systems can be used to 498 elicit prior distributions over temperatures to constrain GDGT-based predictions, particularly when 499 attempting to reconstruct ancient climates with no modern analogue in GDGT-space. We emphasise that 500 outside the range of the modern data, the utility of the models is almost solely due to the prior information 501 included in the reconstruction. At present, the only priors being used in the forward model prescribe a 502 reasonable upper limit and lower limit on temperatures (see Supplementary Information). The only way to 503 improve these reconstructions will be for future iterations to incorporate prior information from other 504 proxies. It is worth noting that the predictive uncertainty, while reasonably well-described by the standard

deviation in cases where ancient data lie quite close to the modern data in GDGT space, can be highly multimodal (Fig. 11). This is the case when estimates are significantly outside of the modern calibration dataset, such as low latitude data in the Cretaceous, or where there is considerable scatter in the modern calibration data, for example in the low temperature range (<5 °C).</p>

509

510 **3. Non-analogue behavior and Extrapolation**

511

512 In principle, the predictors described above can be applied directly to ancient data, such as data from the 513 Eocene or Cretaceous (Inglis et al., 2015; O'Brien et al., 2017). In practice, one should be careful with 514 using models outside their domain of applicability. The machine learning tools described above, which are 515 ultimately based on the analysis of nearby calibration data in GDGT space, are fundamentally designed for 516 interpolation. To the extent that ancient data occupy a very different region in GDGT space, extrapolation 517 is required, which the models do not adequately account for. The divergence between modern calibration 518 data and ancient data is evident from Fig. 12, which shows histograms of minimum normalised distances 519 between 'high quality' Eocene/Cretaceous data points (those that passed the screening tests applied by 520 O'Brien et al., 2017 and Inglis et al., 2015) and the nearest point in the full modern data set. We strongly 521 recommend the use of the nearest neighbor distance metric (D_{nearest}) as a screening method to determine 522 whether the modern core top GDGT assemblage data is an appropriate basis for ancient SST estimation on 523 a case-by-case basis. Note that this distance measure is weighted by the scale length of the relevant 524 parameter as estimated by the Gaussian process emulator in order to quantify the relative position of ancient 525 GDGT assemblages to the modern core-top data. By using the GP-estimated covariance as the distance 526 metric, we account for the sensitivity of different GDGT components to temperature. Our inference is that 527 samples with $D_{nearest} > 0.5$, regardless of the calibration model or approach applied, are unlikely to generate 528 temperature estimates that are much better than informed guesswork. In these instances, in both our GPR 529 and Fwd models, the constraints provided by the modern calibration data set are so weak that estimates of 530 temperature have large uncertainty bands that are dictated by model priors; i.e. are unconstrained by the 531 calibration data (e.g., Figure 13 and Figure 14). This uncertainty is not apparent from estimates generated 532 by BAYSPAR or TEX_{86}^{H} models, although the underlying and fundamental lack of constraints are the same. 533 While 93% of validation data points in the modern data have $D_{nearest} < 0.5$, this is the case for only 33% of 534 Eocene samples and 3% for Cretaceous samples.

535

536 Where ancient GDGT distributions lie far from the modern calibration data set ($D_{nearest} > 0.5$), we argue that 537 there is no suitable set of modern analogue GDGT distributions from which to infer growth temperatures

538 for this ancient GDGT distribution. Both the GPR and Fwd models revert to imposed priors once the

539 distance from the modern calibration dataset increases. We propose that this is more rigorous and justified 540 model behavior than extrapolation of TEX₈₆ or BAYSPAR predictors to non-analogue samples far from 541 the modern calibration data. As a result, the predictive models can only be applied to a subset of the Eocene 542 and Cretaceous data. We also note that there are two broad, non-mutually-exclusive categories of samples 543 that lie far from the modern calibration dataset ($D_{nearest} > 0.5$), the first are samples that seem to lie 'beyond' 544 the temperature-GDGT calibration relationship, likely with (unconstrained) GDGT formation temperatures 545 higher than the modern core-top calibrations; the second are samples with anomalous GDGT distributions 546 lying on the margins of, or far away from the main GDGT clustering in 6-dimensional space (see outliers 547 in Fig. 8).

548

549 Given the (current) limit on natural mean annual surface ocean temperatures of ~ 30 °C, extending the 550 GDGT-temperature calibration might be possible through, 1) integration of full GDGT abundance 551 distributions produced in high temperature culture, mesocosm or artificially warmed sea surface 552 conditions into the models; followed by, 2) validation through robust inter-comparisons of any new 553 GDGT palaeothermometer for high temperatures conditions with other temperature proxies from past 554 warm climate states. As discussed in the introduction, the first approach is limited by the ability of culture 555 or mesocosm experiments to accurately represent the true diversity and growth environments and 556 dynamics of natural microbial populations. Such studies clearly indicate a more complex, community-557 scale control on changing GDGT relative abundances to growth temperatures (e.g., Elling et al., 2015). 558 Community-scale temperature dependency can be modelled relatively well with analyses of natural 559 production preserved in core-top sediments, especially with more sophisticated model fitting, including 560 the GPR and Fwd model presented here. Above $\sim 30^{\circ}$ C, however, the behavior of even single strains of 561 mesophilic archaea are not well-constrained by culture experiments, and the natural community-level 562 responses above this temperature are, so far, completely unknown. While there is evidence for the 563 temperature-sensitivity of GDGT production by thermophilic and acidophilic archaea in older papers (de 564 Rosa et al., 1980; Gliozzi et al., 1983), recent work, characterised by more precise phylogenetic and 565 culturing techniques show a more complex relationship between GDGT production and temperature. 566 Elling et al., (2017) highlight that there is no correlation between TEX_{86} and growth temperature in a 567 range of phylogenetically different thaumarchaeal cultures - including thermophilic species. Bale et al. 568 (2019) recently cultured Candidatus nitrosotenuis uzonensis from the moderately thermophilic order 569 Nitrosopumilales (that contains many mesophilic marine strains). They found no correlation between 570 TEX₈₆ calibrations (either the Kim et al., core-top or Wuchter et al. 2004 and Schouten et al., 2008 571 mesocosm calibrations) with membrane lipid composition at different growth temperatures (37°C, 46°C, 572 and 50°C) and found that phylogeny generally seems to have a stronger influence on GDGT distribution

573 than temperature. In view of these existing data, we see no robust justification at present for the

574 extrapolation of modern core-top calibration data sets into the unknown above 30 °C, although the

- 575 coherent patterns apparent across GDGT space, between modern, Eocene and Cretaceous data (Figures
- 576 7), do provide some grounds for hope that the extension of GDGT palaeothermometry beyond 30°C might
- 577 be possible in future.
- 578

579 4. OPTiMAL and D_{nearest}: A more robust method for GDGT-based paleothermometry

580

581 A more robust framework for GDGT-based palaeothermometry, could be achieved with a flexible 582 predictive model that uses the full range of six GDGT relative abundances, and has transparent and robust 583 estimates of the prediction uncertainty. In this context, the Gaussian Process Regression model (GPR; 584 Section 2.4) outperforms the Forward model (Fwd; Section 2.6) within the modern calibration dataset and 585 we recommend standard use of the GPR model, henceforth called OPTiMAL, over the Fwd model. Model 586 code for the calculation of D_{nearest} values and OPTiMAL SST estimates (Matlab script) and the Fwd Model 587 SST estimates (R script) are archived in the GITHUB repository, 588 https://github.com/carbonatefan/OPTiMAL.

589

590 To investigate the behaviour of the new OPTiMAL model, we compare temperature predictions including 591 uncertainties for the Eocene and Cretaceous datasets, made by OPTiMAL and the BAYSPAR methodology 592 of Tierney and Tingley (2014) (Figures 13 and 14), using the default priors specified in the model code for 593 the BAYSPAR estimation. The OPTiMAL model systematically estimates slightly cooler temperatures 594 than BAYSPAR, with the biggest offsets below ~ 15 °C (Figure 13). We suggest that this is driven by our 595 inclusion of all data present in our modern calibration dataset, including data north of 70°N, which is 596 excluded from the BAYSPAR model (Tierney and Tingley, 2015). Fossil GDGT assemblages that fail the 597 D_{nearest} test are shown in grey, which clearly illustrate the regression to the mean in the OPTiMAL model, 598 whereas BAYSPAR continues to make SST predictions up to and exceeding 40 °C for these "non-analogue" 599 samples due to the fact that BAYSPAR assumes that higher TEX86 values equate to higher temperatures 600 as part of the functional form of the model, whereas the GPR model is agnostic on this. A comparison of 601 error estimation between OPTiMAL and BAYSPAR is shown in Figure 14. For most of the predictive 602 range below the D_{nearest} cut-off of 0.5, OPTiMAL has smaller errors than BAYSPAR, especially in the lower 603 temperature range. As D_{nearest} increases, i.e. as the fossil GDGT assemblage moves further from the 604 constraints of the modern calibration dataset, the error on OPTiMAL increases, until it reaches the standard 605 deviation of the modern calibration dataset (i.e., is completely unconstrained). In other words, OPTiMAL 606 generates maximum likelihood SSTs with robust confidence intervals, which appropriately reflect the

607 relative position of an ancient sample used for SST estimation and the structure of the modern calibration 608 data set. Where there are strong constraints from near analogues in the modern data, uncertainties will be 609 small, where there are weak constraints, uncertainty increases. In contrast, BAYSPAR, because it is 610 fundamentally based on a *parametric* linear model and therefore does not account for model uncertainty, 611 assigns similar uncertainty intervals as to the rest of the data, despite there being no way of reasonably

testing whether the linear model is an appropriate description of the data far from the modern dataset.

- 612
- 613

614 We further provide a first assessment of the inter-relationship between standard screening indices and 615 D_{nearest}, with an additional figure (Figure 15) showing the relationship between D_{nearest}, BIT, and MI for the 616 Eocene and Cretaceous compilations (where these data are available). These plots show little relationship 617 between the BIT and MI screening indices and D_{nearest} values. Whilst in the Eocene, samples with the highest 618 D_{nearest} values (>3) also show very elevated BIT values (>0.8), in the Cretaceous the exceptionally 619 anomalous assemblages (D_{nearest} values >100) are not anomalous in either BIT or MI. Conversely, in the 620 Eccene there are many samples with relatively high BIT (>0.3) that are below the D_{nearest} threshold of 0.5. The behaviour of these systems needs to be examined in detail in future studies, but a conservative approach 621 would be to apply all three screening indices (BIT, MI and Dnearest) to have the most confidence in resulting 622 623 temperature estimates. To investigate these behaviours requires the publication of the full range GDGT 624 abundance data. Whilst key compilations of Eocene and Cretaceous GDGT data have strongly encouraged 625 the release of such datasets (Lunt et al. 2012; Dunkley Jones et al. 2013; Inglis et al. 2015; O'Brien et al. 626 2017), most Neogene studies only publish TEX₈₆ values. Without full GDGT assemblage data neither 627 OPTiMAL nor other detailed assessments of GDGT behaviour and type can be made, and we would 628 strongly encourage authors, reviewers and editors to ensure the publication of full GDGT assemblages in 629 future

630 Finally, we provide two example time series from the Neogene to modern, where full GDGT assemblage data were made available, and there are comparison alkenone-based Uk'37 data from the same sampling 631 632 location - ODP 806 and ODP 850, respectively in the West and Eastern Equatorial Pacific (Figure 16; Zhang et al. 2014). Where U^{k'}₃₇ temperatures are not at the limit of alkenone saturation in ODP 806, 633 OPTiMAL and $U^{k'_{37}}$ agree well in the Plio-Pleistocene. In ODP 850, there is a strong agreement in the 634 reproduction of a long-term late Miocene to Recent cooling trend in both $U^{k'}_{37}$ and OPTiMAL of ~5°C. 635 There is, however a consistent $\sim 2^{\circ}$ offset between cooler OPTiMAL and warmer U^{k'}₃₇ temperatures at this 636 location. This offset is very similar in magnitude and direction as that between TEX_{86}^{H} and $U^{k'}_{37}$ used in 637 638 the original study. and is more likely due to an inherent feature (seasonality or depth) of archaeal versus 639 eukaryotic production at this site (Zhang et al. 2014).

640

641 5. Conclusions

642

643 Although the fundamental issue of non-analogue behaviour is a key problem for GDGT-temperature 644 estimation, it has an undue impact on the community's general confidence in this method. In part, this is 645 because these issues have not been clearly stated and circumscribed - rather they have been allowed to erode 646 confidence in the GDGT-based methodology through the use of GDGT-based palaeothermometry far 647 outside the modern constraints on the behavior of this system. The use of GDGT abundances to estimate 648 temperatures in clearly non-analogue conditions is, at present, problematic on the basis of the available 649 calibration constraints or a good understanding of underlying biophysical models. We hope that this study 650 prompts further investigations that will improve these constraints for the use of GDGTs in deep-time 651 paleoclimate studies, where they clearly have substantial potential as temperature proxies. Temperature 652 estimates based on fossil GDGT assemblages that are within range of, or similar to, modern GDGT 653 calibration data, do, however, rest on a strong, underlying temperature-dependence observed in the 654 empirical data. With no effective means of separating the "good from the bad" can lead to either false 655 confidence and inappropriate inferences in non-analogue conditions, or a false pessimism when ancient 656 samples are actually well constrained by modern core-top assemblages.

657

658 In this study, we apply modern machine-learning tools, including Gaussian Process Emulators and forward 659 modelling, to improve temperature estimation and the representation of uncertainty in GDGT-based SST 660 reconstructions. Using our new nearest neighbour test, we demonstrate that >60% of Eocene, and >90% of 661 Cretaceous, fossil GDGT distribution patterns differ so significantly from modern as to call into question 662 SSTs derived from these assemblages. For data that does show sufficient similarity to modern, we present 663 OPTiMAL, a new multi-dimensional Gaussian Process Regression tool which uses all six GDGTs (GDGT-664 0, -1, -2, -3, Cren and Cren') to generate an SST estimate with associated uncertainty. The key advantages 665 of the OPTiMAL approach are: 1) that these uncertainty estimates are intrinsically linked to the strength of 666 the relationship between the fossil GDGT distributions and the modern calibration data set, and 2) by 667 considering all GDGT compounds in a multi-dimensional regression model it avoids the dimensionality 668 reduction and loss of information that takes place when calibrating single parameters (TEX₈₆) to 669 temperature. The methods presented above make very few assumptions about the data. We argue that such 670 methods are appropriate with the current absence of any reasonable mechanistic model for the data 671 generating process, in that they reflect model uncertainty in a natural way. Finally, we note the potential 672 for multi-proxy machine learning approaches, synthesising data from other palaeothermeters with 673 independent uncertainties and biases, to improve calibration of ancient GDGT-derived SST reconstructions. 674

675	
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683	
684	
685	Figure Captions:
686 687	Figure 1 . A histogram of the normalised distance to the nearest neighbour in GDGT space $(D_{x,yt})$ for all
688	samples in the modern calibration dataset of Tierney and Tingley (2015).
689	samples in the modern canoration dataset of Themey and Tingley (2015).
690	Figure 2. The error of the nearest-neighbour temperature $(D_{x,y})$ predictor, for modern core-top data, as a
691	function of the distance to the nearest calibration sample.
692	1
693	Figure 3. Top: The temperature of the modern data set as a function of the TEX ₈₆ value, showing a clear
694	linear correlation between the two, but also significant scatter. Bottom: the error of the predictor based on
695	the nearest TEX ₈₆ calibration point.
696	
697 698 699 700 701	Figure 4. The error of a random forest predictor as a function of the true temperature (see Section 2.3). This machine learning based predictor yields δT 4.1 °C degrees, by applying a suitable weighted average over multiple near neighbours. R2 = 0.83, meaning that 83% of the variation in the observed temperature is successfully explained by our GDGT-based model.
702	Figure 5. The error of the GPR (Gaussian Process regression) predictor as a function of the true
703	temperature.
704	
705	Figure 6. Modern and ancient data projected onto the first two compositional principal components. Black:
706	Modern; Blue: Eocene (Inglis et al., 2015); Red: Cretaceous (O'Brien et al., 2017).
707	
708	Figure 7. Diffusion map projection of the modern and ancient data. Black: Modern; Blue: Eocene (Inglis
709	et al., 2015); Red: Cretaceous (O'Brien et al., 2017). separate clusters marked 'A' are the outlying

710 711 712	Cretaceous points with high GDGT-3 values. Branch 'B' is dominated by modern data points; branch 'C' by Cretaceous data.
713 714 715 716	Figure 8. The first diffusion component as a function of TEX ₈₆ . Some outlying points have been excluded from the plot for the purposes of visualisation. Black: Modern; Blue: Eocene (Inglis et al., 2015); Red: Cretaceous (O'Brien et al., 2017).
717 718	Figure 9. The first diffusion component as a function of temperature (modern data only).
719 720	Figure 10. Temperature residuals for the forward model.
721	Figure 11. The posterior distributions over temperature from the forward model for selected examples of
722	high and low temperature, Eocene and Cretaceous, data points. The Gaussian error envelope from the GPR
723	model is shown for comparison.
724	
725	Figure 12. A histogram of normalised distances to the nearest sample in the modern data set for Eocene
726	and Cretaceous data, excluding samples that had been screened out in previous compilations using BIT, MI
727	and RI following the approach of (Inglis et al., 2015; O'Brien et al., 2017).
728	
729	Figure 13. Comparison of temperature estimates for the BAYSPAR and the OPTiMAL GPR model, greyed
730	out data fails the $D_{nearest}$ test (>0.5), and the colour scaling reflects $D_{nearest}$ values for those datapoints that
731	pass. Note that outside of the constraints of the modern calibration (training) dataset, ($D_{nearest}$ test >0.5) the
732	GPR model temperature estimates revert to the mean value of the calibration dataset, with an uncertainty
733	that reverts to the standard deviation of the training data.
734	
735	Figure 14. Inter-comparison of temperature estimates and errors (y-axis) for compiled Eocene and
736	Cretaceous data calculated using OPTiMAL (top) and BAYSPAR (bottom). Greyed out data fails the
737	$D_{nearest}$ test (>0.5), and the colour scaling reflects $D_{nearest}$ values for those datapoints that pass. The black
738	dashed line shows the $D_{nearest}$ threshold (>0.5).
739 740 741 742	Figure 15. Comparison of $D_{nearest}$ threshold (>0.5), BIT and MI index for the Eocene (Inglis et al., 2015) and Cretaceous (O'Brien et al., 2017) datasets.
743	Figure 16. GDGT-derived OPTiMAL palaeotemperatures, for the late Miocene to Recent, from two sites
744	in the Eastern (ODP Site 850) and Western (ODP Site 806) Equatorial Pacific; uncertainty envelopes are

one standard deviation each side of the maximum likelihood temperature estimator. Also shown for comparison are $U^{k'_{37}}$ data from the same sites and modern mean annual SSTs.

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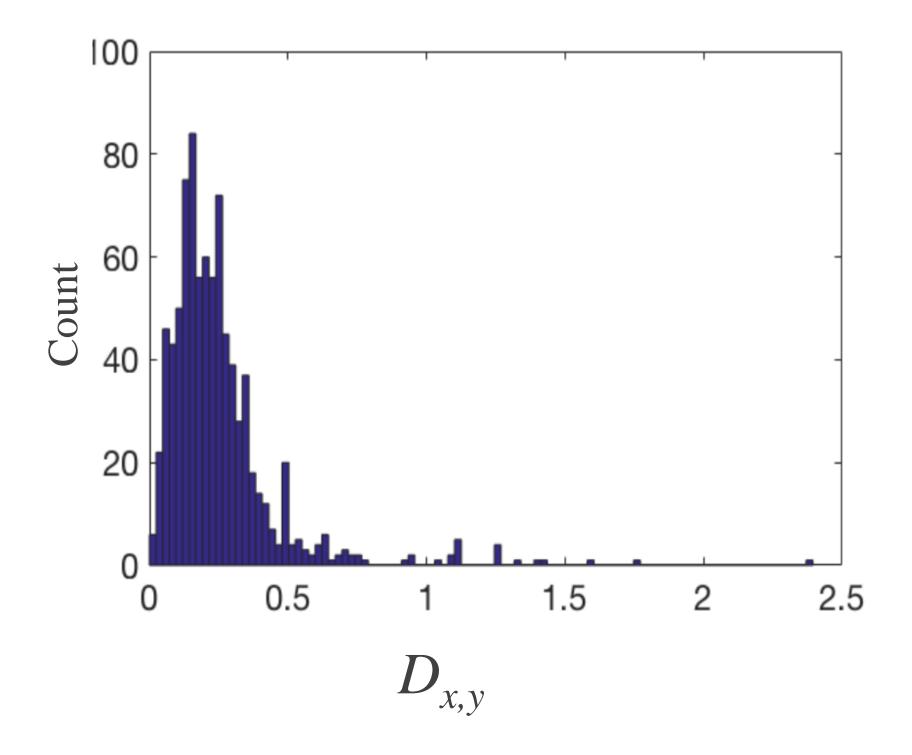
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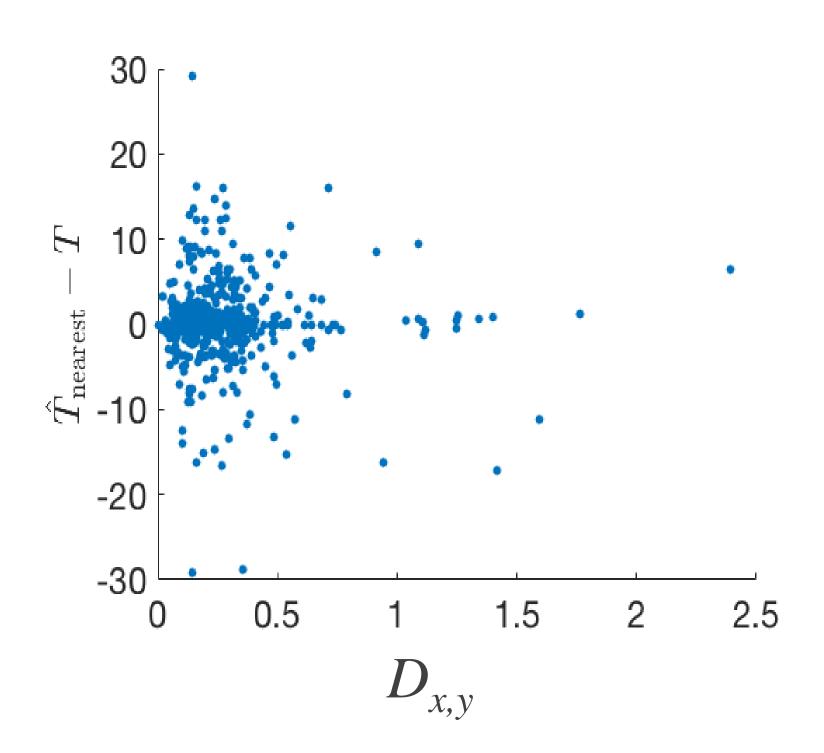
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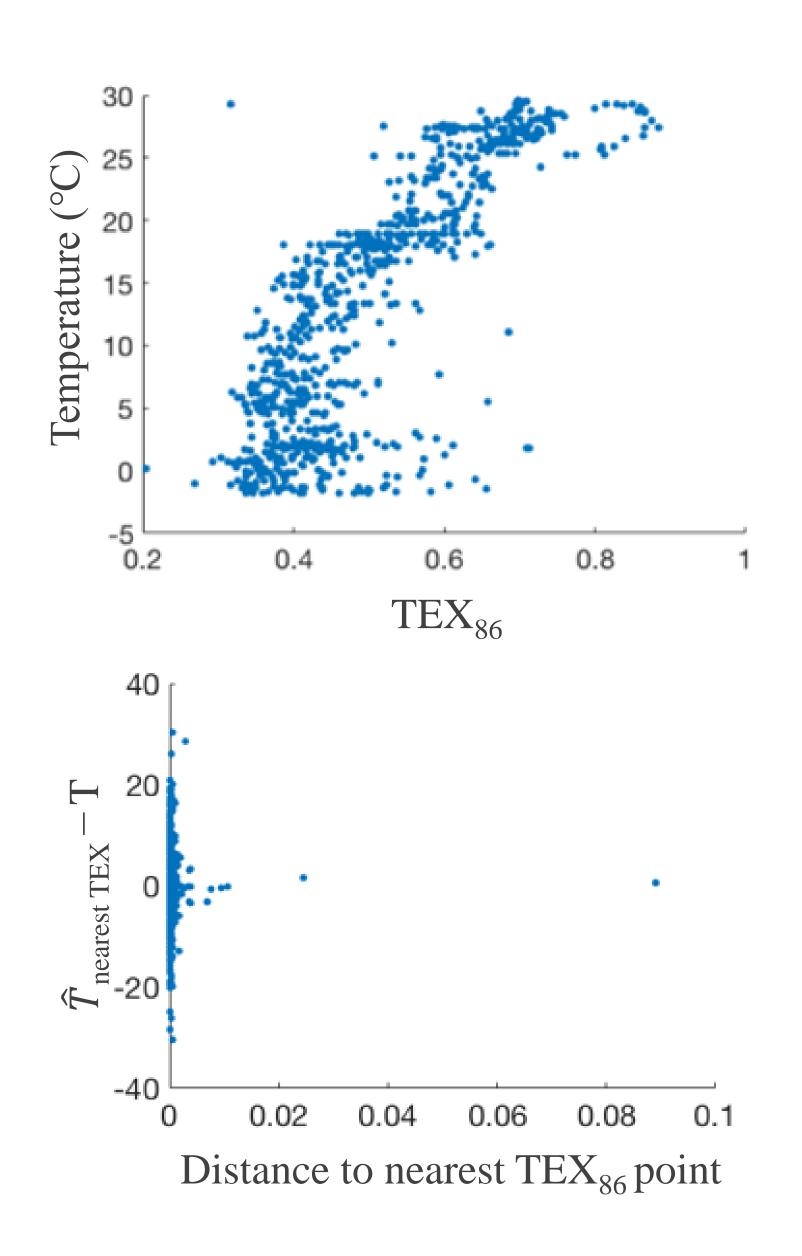
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Figure 1

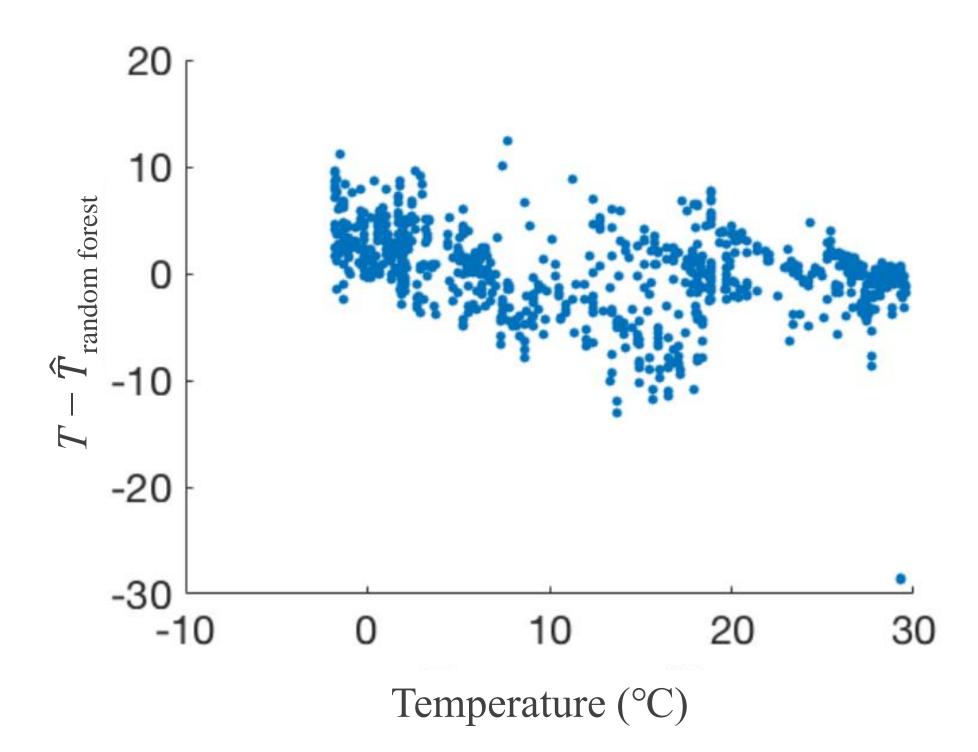


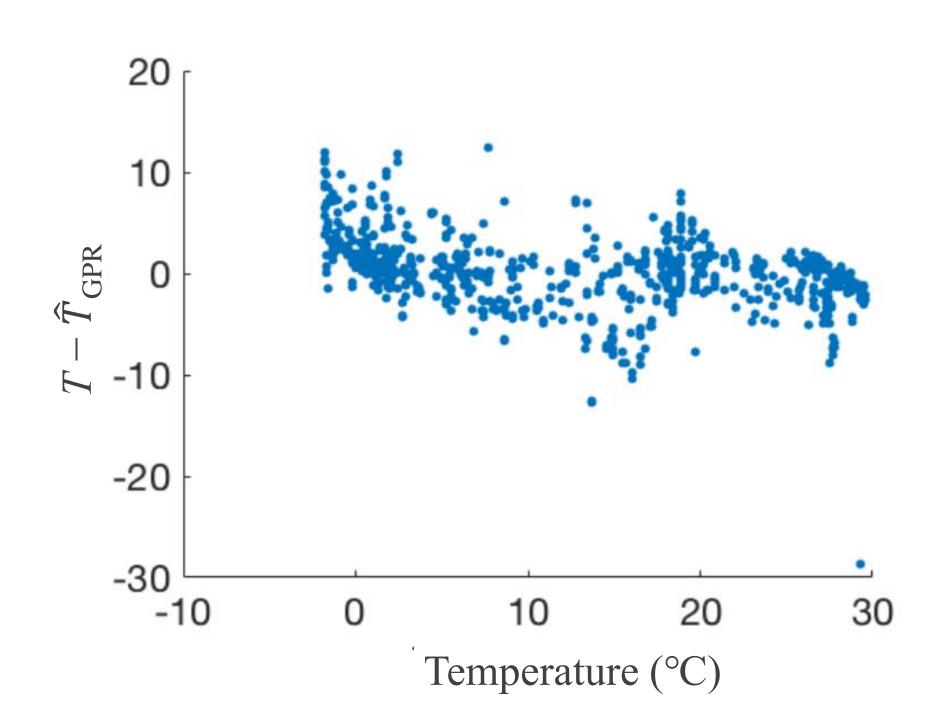


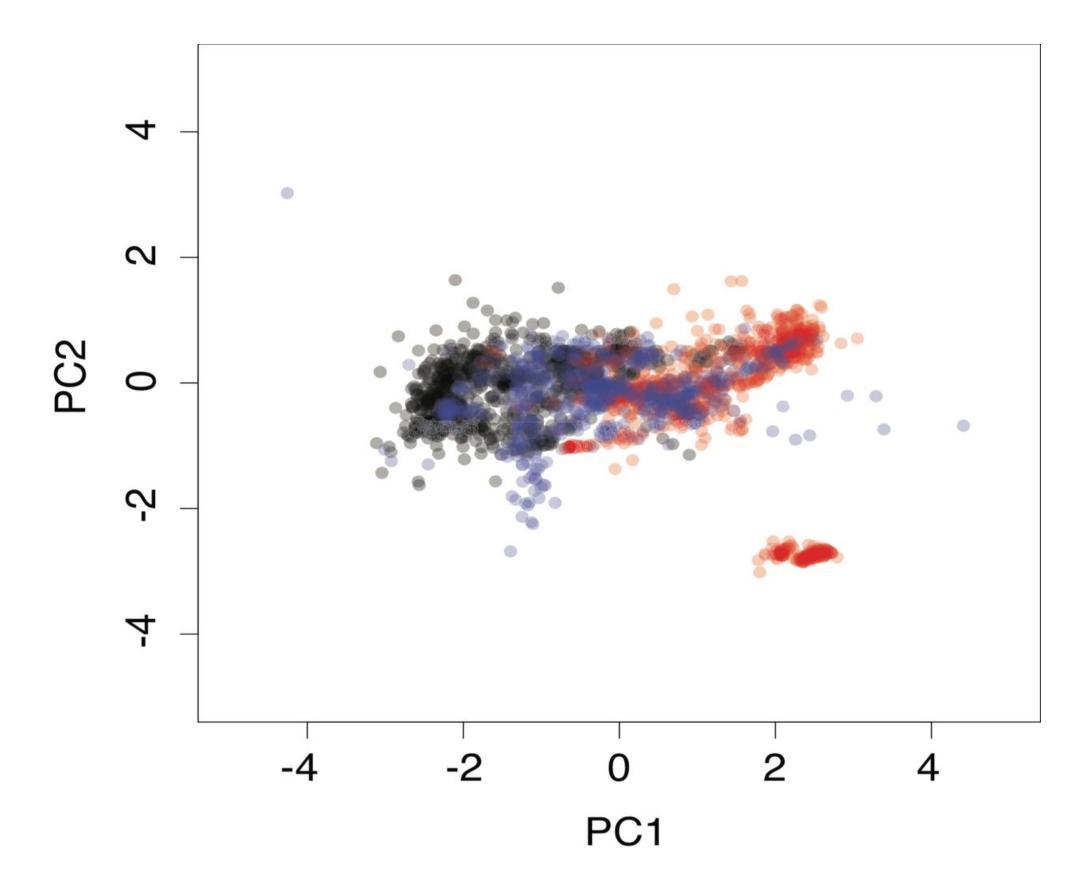


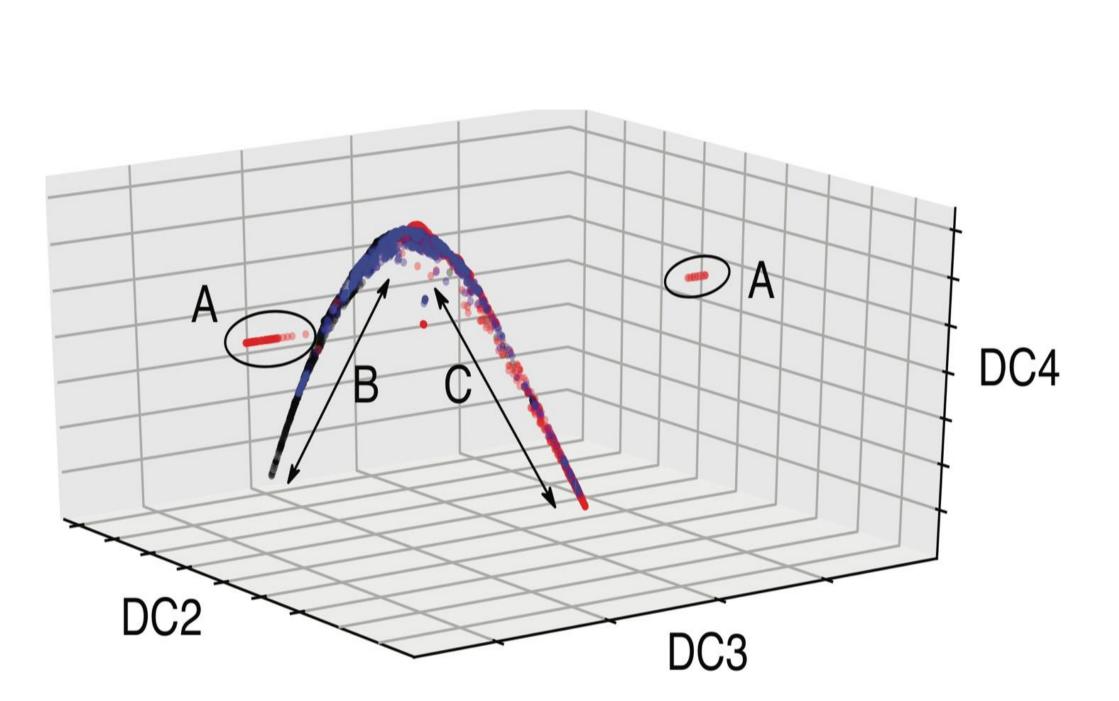


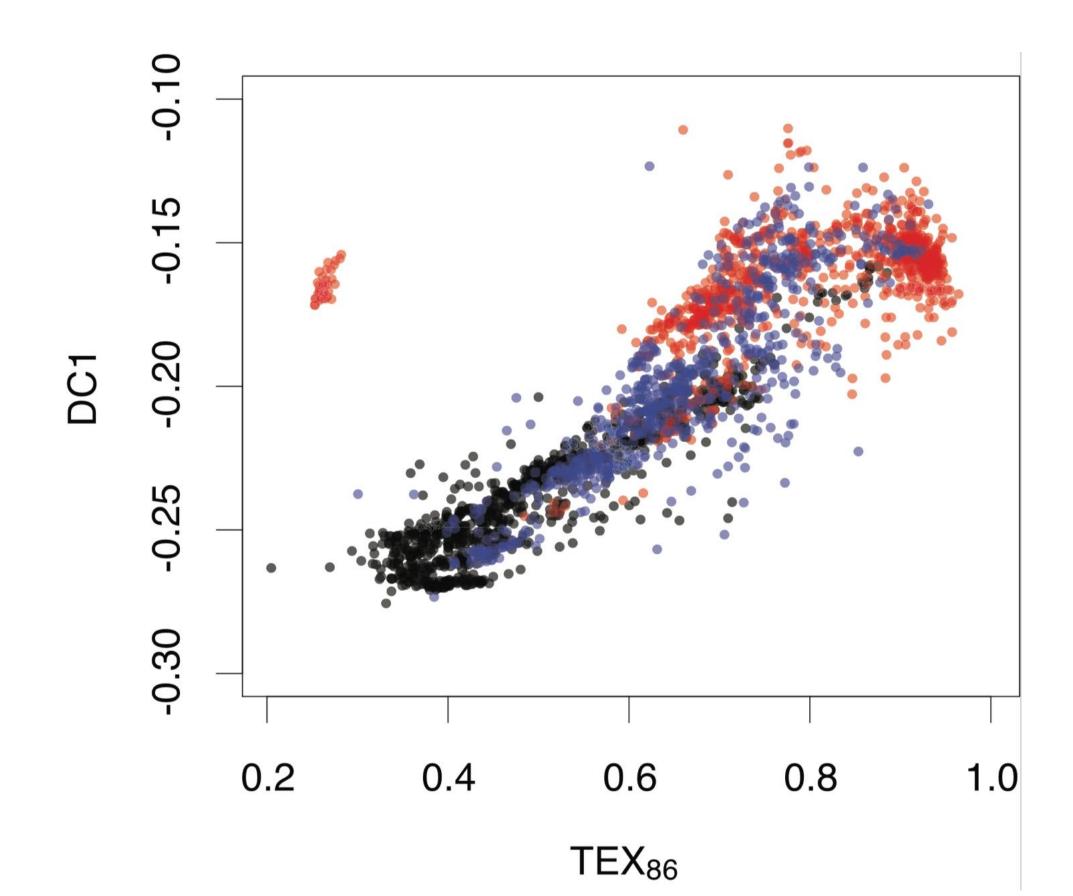


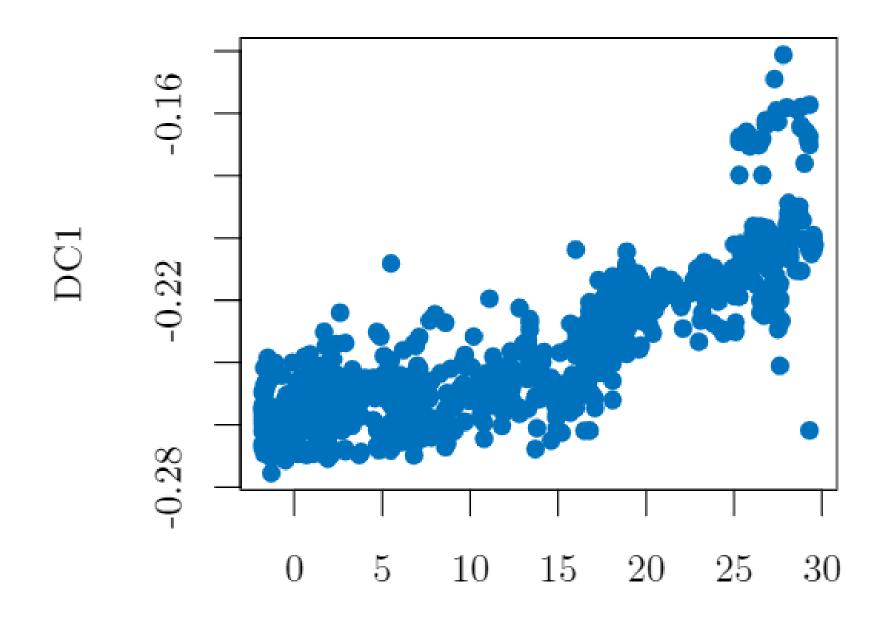




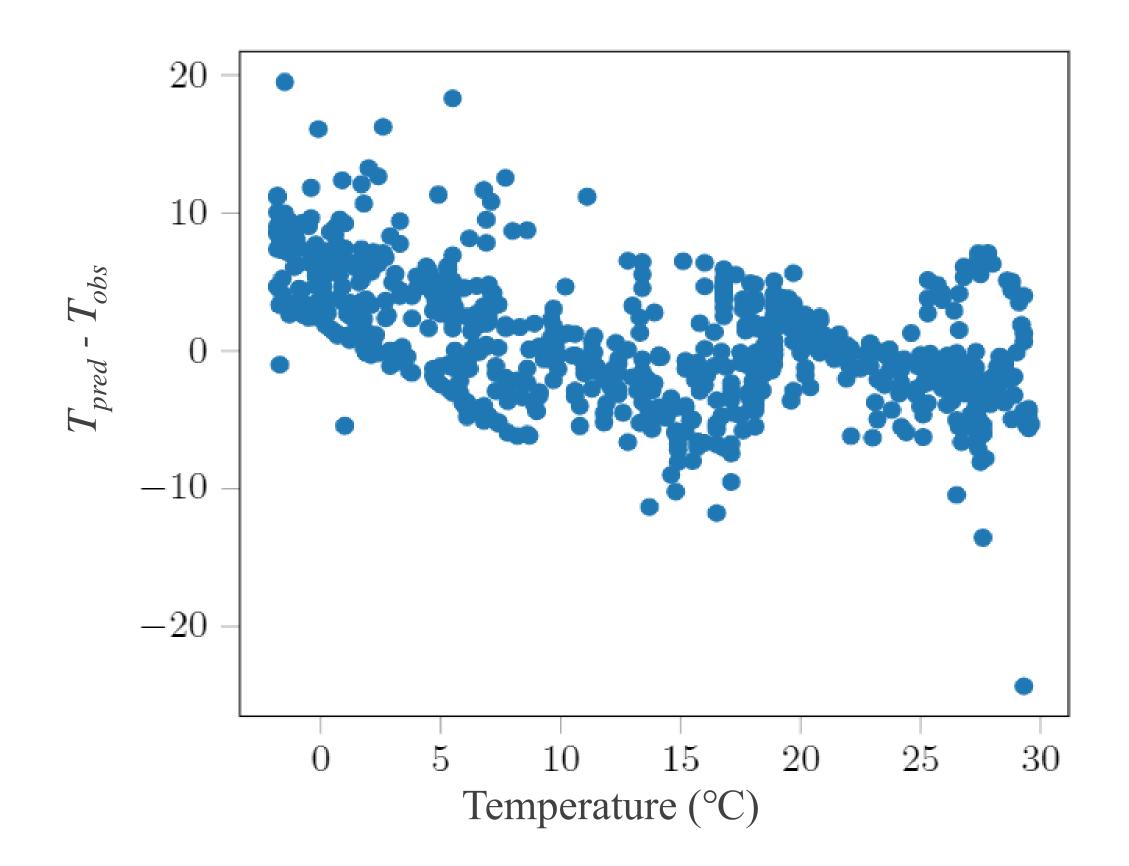


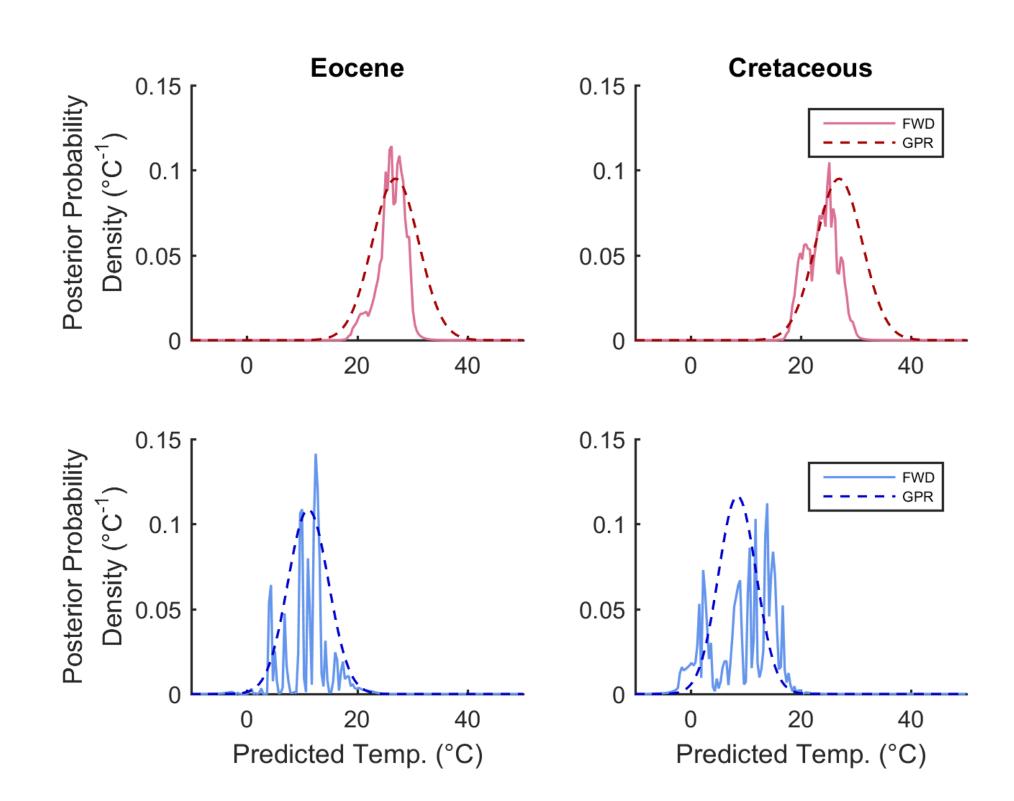


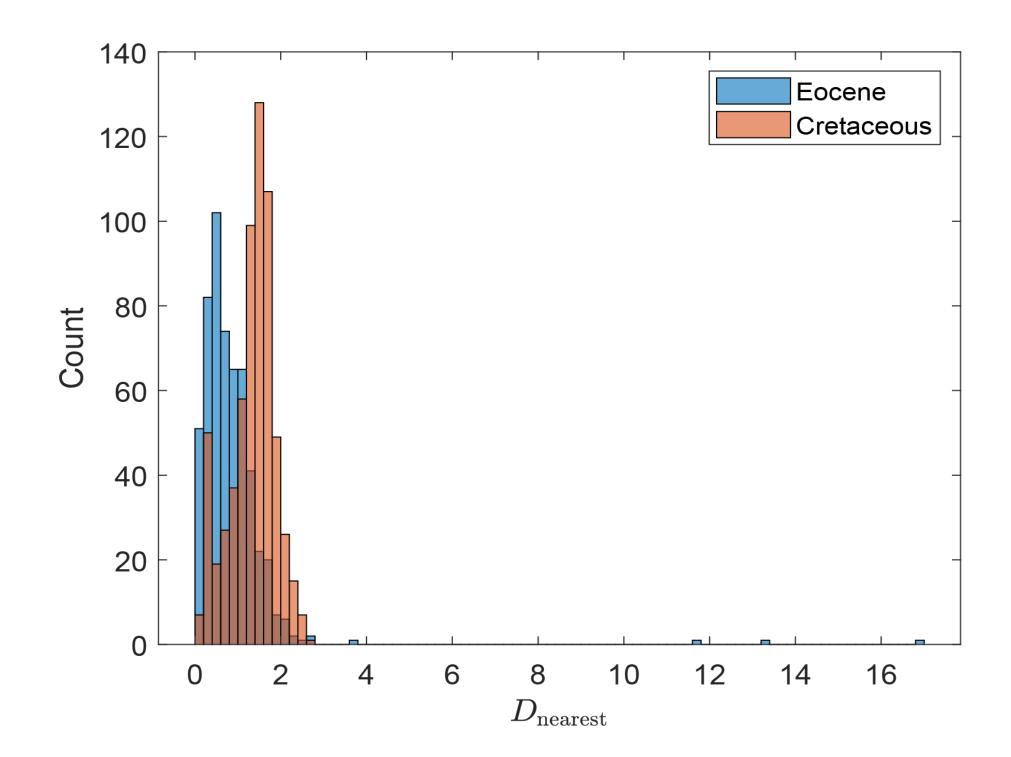


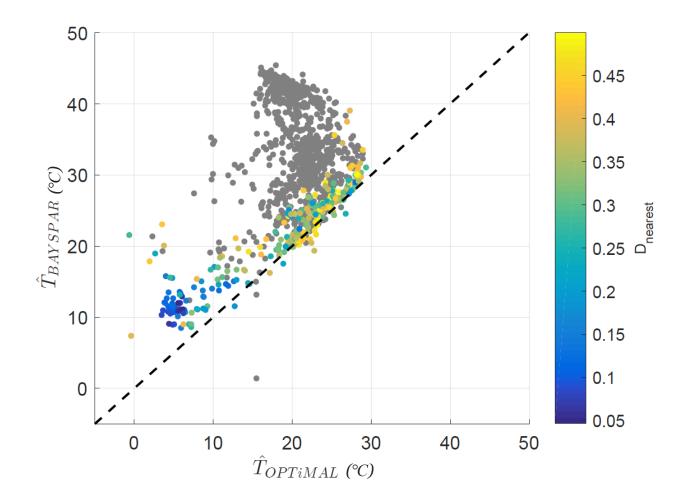


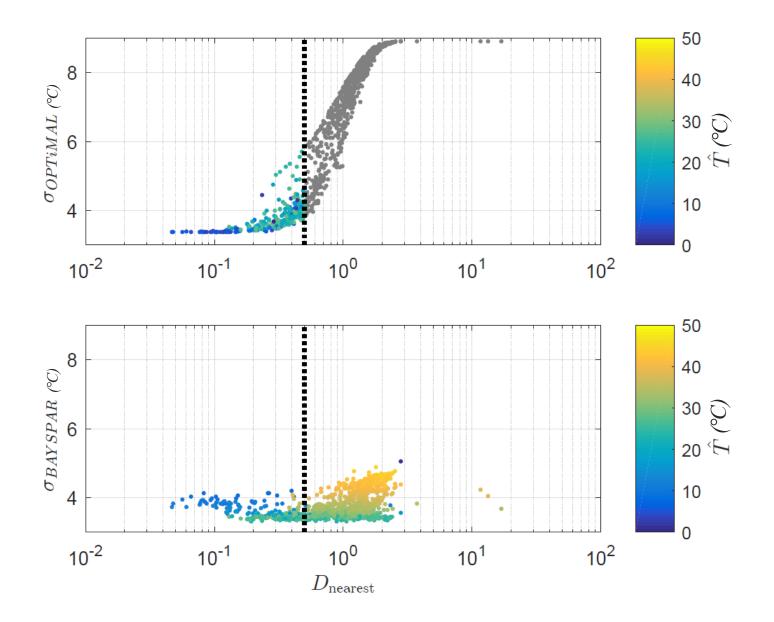
Temperature (°C)



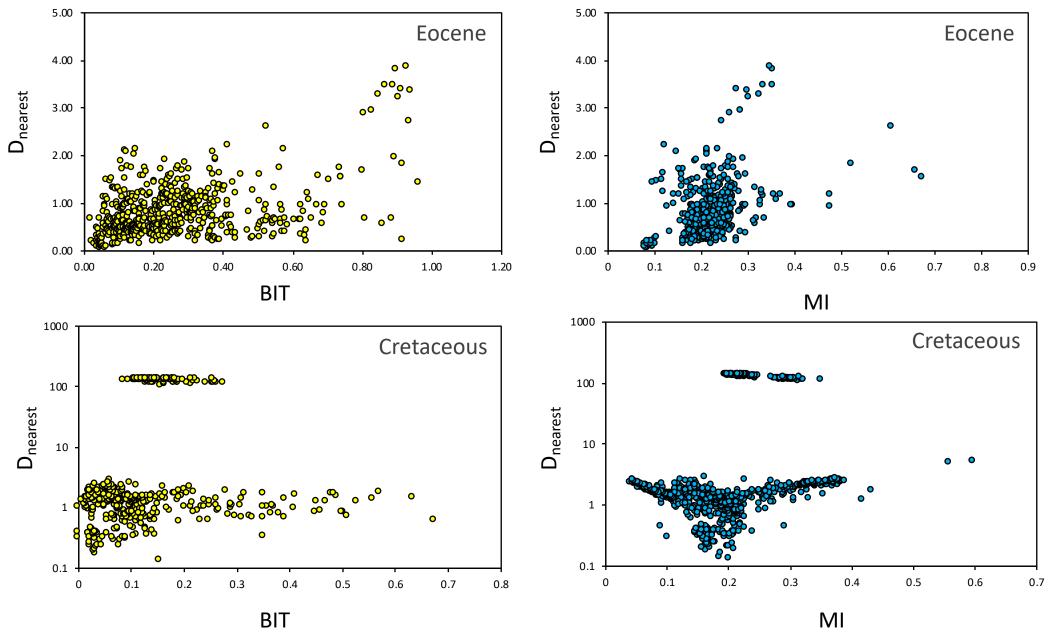












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