

Reply to reviewer #1:

We thank reviewer #1 for the report. Hereafter we address the questions and comments mentioned by the reviewer. Reviewer comments are given in *italic letters* whereas our replies are given in normal letters.

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It needs to be made clear, right at the beginning, that d15N by itself is not sufficient to provide a temperature record. There must be a highly accurate independent accumulation rate record in addition. It is only the COMBINATION of d15N data and accumulation data that gives temperature, in the method that is described in the manuscript. The reason is very simple. A doubling of accumulation rate can cause a change in firn thickness and hence d15N, with no temperature change whatsoever.

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The same is true for d40Ar data, when it is used as the sole gas measurement.

15 We fully agree with reviewer #1 that highly-accurate accumulation-rate data are needed to reconstruct surface-temperature histories from $\delta^{15}\text{N}$ and $\delta^{40}\text{Ar}$ data. We added this fact already in the first sentence of the abstract by saying:

20 “Greenland past temperature history can be reconstructed by forcing the output of a firn-densification and heat-diffusion model to fit multiple gas-isotope data ($\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$ or $\delta^{15}\text{N}_{\text{excess}}$) extracted from ancient air in Greenland ice-cores using published accumulation-rate (ACC) data sets.”

Additionally, the abstract was changed for the dependencies of the reconstructed temperature by adding the accumulation explicitly, i.e. $T(\delta^{15}\text{N}, \text{Acc})$. It reads now:

25 “We solve the inverse problem $T(\delta^{15}\text{N}, \text{Acc})$ by using a combination of a Monte-Carlo-based iterative approach and the analysis of remaining mismatches between modelled and target data, based on cubic-spline-filtering of random numbers as well as the laboratory-determined temperature-sensitivity for nitrogen isotopes.”

In the original text we already mentioned the necessity of the accumulation several times in chapter 2.

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Highly accurate d15N_{excess} data, however, can provide a temperature record without any associated accumulation record. This distinction needs to be made clearer. In its present form the reader could be seriously misled by the manuscript. It borders on scientific dishonesty to persist in making this misleading presentation of the facts.

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We agree with the reviewer in part. Indeed the $\delta^{15}\text{N}_{\text{excess}}$ removes the gravitational signal and therefore temperature gradients, ΔT , along the firn column can be directly estimated. However, we do not agree with the statement that no accumulation rate is necessary to reconstruct surface or bottom temperature because accumulation-rate changes initiate heat-diffusion changes. Therefore, firn models are needed as they describe the changes of the firn column due to temperature and accumulation-rate variability and more important the associated heat diffusion through the firn to extract the related surface-temperature time-series (Landais, 2012). That means, also for $\delta^{15}\text{N}_{\text{excess}}$ -based temperature reconstructions, highly accurate accumulation-rate data are needed. For instance, in the recent published study from Kobashi et al. (2017) where a $\delta^{15}\text{N}_{\text{excess}}$ -based approach was chosen to reconstruct past temperature, the Goujon-firn-model (Goujon et al., 2003) was used for the integration of $\Delta T(t)$ and even if it is not explicitly mentioned in the paper, accumulation-rate data were needed to run the firn model.

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In contrast to this, Grachev and Severinghaus (2005) relates the $\Delta T(t)$ variability one to one to past surface-temperature changes with additionally applying a heat-model-based transfer correction of 2 K. In Landais (2012) it is argued that the use of a firn-densification and heat-diffusion model instead of the heat transfer correction would probably lead to more accurate results. We support this statement.

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page 4 line 16 units for mass difference should be "kg per mol"

We corrected for that and changed the new sentence to:

55 “g is the gravitational acceleration, Δm the molar mass-difference between the heavy and light isotopes (equals 10^{-3} kg per mol for nitrogen) and R the ideal gas-constant.”

page 4 line 27 the language here is confusing. As I understand it, the Leuenberger, Boersma-Klein, and DeVries results were not the ones used in the current manuscript, so there is no place for them in the sentence describing the given equation. Please cut the mention of Leuenberger and Boersma-Klein and DeVries, as it makes it hard for the reader to know which measurement result is being presented in the given equation. There should be no ambiguity here, and there is indeed no excuse for creating ambiguity in a scientific paper. This issue was already raised by one of the reviewers in the first round of review, and the authors have apparently chosen to ignore that reviewer. This is unacceptable and unprofessional behavior and the authors are hereby warned that continuing to ignore the reviewers will result in rejection of the manuscript.

10 We deleted the corresponding reference.

References:

- 15 Goujon, C., Barnola, J.-M. and Ritz, C.: Modeling the densification of polar firn including heat diffusion: Application to close-off characteristics and gas isotopic fractionation for Antarctica and Greenland sites, *J. Geophys. Res. Atmos.*, 108(D24), n/a-n/a, doi:10.1029/2002JD003319, 2003.
- Grachev, A. M. and Severinghaus, J. P.: A revised $+10\pm 4^\circ\text{C}$ magnitude of the abrupt change in Greenland temperature at the Younger Dryas termination using published GISP2 gas isotope data and air thermal diffusion constants, *Quat. Sci. Rev.*, 24(5–6), 513–519, doi:10.1016/j.quascirev.2004.10.016, 2005.
- 20 Kobashi, T., Menviel, L., Jeltsch-Thömmes, A., Vinther, B. M., Box, J. E., Muscheler, R., Nakaegawa, T., Pfister, P. L., Döring, M., Leuenberger, M., Wanner, H. and Ohmura, A.: Volcanic influence on centennial to millennial Holocene Greenland temperature change, *Sci. Rep.*, 7(1), 1441, doi:10.1038/s41598-017-01451-7, 2017.
- 25 Landais, A.: Stable Isotopes of N and Ar as Tracers to Retrieve Past Air Temperature from Air Trapped in Ice Cores, in *Handbook of Environmental Isotope Geochemistry*, edited by M. Baskaran, pp. 865–886, Springer Berlin Heidelberg, Berlin, Heidelberg., 2012.

Reply to reviewer #3:

We thank reviewer #3 for the detailed and helpful report. Hereafter we reply to the questions and comments mentioned by the reviewer. Reviewer comments are given in *italic letters* whereas our replies are given in normal letters.

*Although the manuscript appears to have been significantly improved since the original submission, I still found the manuscript to be dense and difficult to read. The point of the manuscript is to introduce a method to infer past temperatures, but the description of the method is difficult to follow. I think the material is appropriate for publication in *Climate of the Past*, but the presentation of the material can still be improved to make it more accessible to a broader range of climate scientists. Reaching readers is, after all, a primary goal of publishing. Here are issues that I had with Section 2:*

- The authors want to describe a complicated procedure. The 4-point summary overview at the top of page 6 is a good start. However, in my view, too much detail is then provided before readers have been given a clear understanding of the whole process. Section 2.3 Reconstruction Approach actually contains many intermediate results, numerical values, and detailed discussion points, before the process is fully explained. When I see text like this, I really don't want to read it. I think the text would be easier to read if the authors were to restrict 2.3 to describing the fundamental concepts and assumptions of the approach. Then, e.g. in a subsequent Discussion section, they could explain how some of those results were developed or obtained, why they were needed, the numerical values that arose, and how they were used.*

- Illustrations integrated with the description of the method could help readers to "see" and understand the procedure. For example, a flow chart could be very useful to help readers as they follow Section 2.3. However, there are no figures in the main text to help here; instead, the text depends heavily on figures and tables in the Supplement. If material is needed to explain the main points of a paper, then that material should be in the main body of the paper. A Supplement should be limited to material that is nice to have in order to supplement the primary material. It should not contain primary material that is essential in order for readers to understand the main text.*

In order to make the manuscript more readable, we follow the suggestion mentioned by the reviewer. We rearranged the order of sections to start with the fundamentals of the new method which is now section 2.1. To provide a guideline for an easier understanding of the description of our inversion approach, we created a flow chart (Fig. 01) as suggested by the reviewer. The new Fig. 01 contains besides the schematic description of the whole algorithm also the used variables. Additionally, we added a new table (Table 01) listing and describing all variables and acronyms used in the manuscript, which can be used together with Fig. 01 to follow the explanations in sections 2.1ff. To further clarify our descriptions we rearranged the figure order in the main and supplementary documents. Additionally, we moved the explanation of the adaption of the accumulation rates to the GICC05 time scale to a new supplement section S1, as we think that is not important for the understanding of the inversion algorithm itself. For the same reason, we moved the sensitivity experiments on the accumulation-rate data (low-pass-filtering and variability) to a new supplement section S2. To shorten the manuscript, we moved a part of our discussion (section 4.2 "High frequency step and final correction") to the supplement section S3 and only summarise the results of the cross-correlation experiments in the main text. Furthermore, we wrote a short remark right at the start of section 2.1 to inform the readers that the problem we deal with is indeed an inverse problem. We hope that with these changes the manuscript is better understandable.

Reviewers of manuscripts are generally expected to identify two types of problems.

- The first is scientific failings, such as failure to correctly interpret and cite relevant background work, or omissions of key steps in descriptions or analysis, or errors in logical development of ideas or conclusions. I was pleased to see that many of the minor points raised by the two initial reviewers have been addressed.*

Thank you.

• The second type of problem that reviewers are asked to identify is communication failings. Is a manuscript organized in a way that readers who are not closely connected with the work can easily understand the approach and grasp the aspects that are novel? If points were unclear to the reviewers, they will probably also be unclear to many other readers. So, I am a bit concerned that more effort appears to have gone into explaining how the initial two reviewers misunderstood the manuscript (15 pages), than has gone into making the manuscript clearer on those points to other readers. Section 4.3 is new in response, but it is only 3 pages long, i.e. only 20% of the length of the argument to the reviewers. I am concerned that the authors may not fully appreciate the challenges that outsiders can have in attempting to read their work.

Yes, we got your point. Indeed, when re-reading our response it is obvious that we were very exhausting in describing what the reviewers potentially have misunderstood and not concentrating on improving why this is the case. We now rearranged sections; we added a new figure and table to follow our methodology as explained above.

• In most inverse problems, non-uniqueness of the inferred model parameters grows rapidly with increasing uncertainties in either the data or the model physics. Section 4.3 addresses the new uncertainties (suggested by Reviewer #2) that could be associated individually with each of the imperfectly known real-world data sets, and with unknowns in the model physics. However, it might be prudent to remind potential users of the procedure why a formal inverse approach is necessary.

Indeed this is a valid and important point. The problem that we deal with is an inverse problem, since the effect, observed as $\delta^{15}\text{N}$ variations, is dependent on its drivers, i.e. temperature and accumulation changes. Therefore, the temperature will be dependent on $\delta^{15}\text{N}$ and the accumulation-rate changes. The firm model is a non-linear transfer function of temperature and accumulation rate to firm states and relates then to $\delta^{15}\text{N}$ values. The fact that manual adjustments are time-consuming and yet not easy reproducible favours an automated inverse approach as implemented here. This last statement is already mentioned in the introduction and the main text.

But, we added the following short introduction to section 2.1:

“The problem that we deal with is an inverse problem, since the effect, observed as $\delta^{15}\text{N}$ variations, is dependent on its drivers, i.e. temperature and accumulation rate changes. Hence, the temperature that we would like to reconstruct depends on $\delta^{15}\text{N}$ and accumulation rate changes. To solve this inverse problem, the firm model, which is a non-linear transfer function of temperature and accumulation rate to firm states and relates to $\delta^{15}\text{N}$ values, is run iteratively to match the modelled and measured $\delta^{15}\text{N}$ values (or other gas species). The automated procedure is significantly more efficient and less time-consuming than a manual approach. The Holocene temperature-reconstruction is implemented by the following four steps (see Fig. 01):”

Page 1, Line 16 – Results may be reproducible, but are they correct?

Quite apart from uncertainties in the input data or in the model physics, are there biases built into the automated procedure? This was a question that Reviewer #2 posed, and it is unclear to me that it has been answered satisfactorily.

The first statement is indeed an interesting and valid comment. As it is shown in the paper, we are able to reconstruct the synthetic temperature targets by fitting the related $\delta^{15}\text{N}$ histories very accurately. This means that the methodology is working. Yet, another issue are the uncertainties in the input data or in the model physics. This, however, has not been the main goal of our investigation, but could be dealt with using our methodology with several different firn models. To our knowledge the presently available firn models (Goujon and Schwander model) are very well comparable. One first step to prove our methodology on real data has been done on data from two Daansgard-Oeschger events which demonstrated good agreement with previously determined reconstructed temperature and accumulation variations by Kindler et al. (2014).

Page 9, Equation (8) –

Why is an L1 norm used instead of an L2 norm?

During the development of the presented algorithm we investigated different minimization-criteria/cost-functions. As a result of these pre-examinations, no significant differences have been found between the use of a L1 or L2 norm for the fitting of Holocene gas-isotope data. The algorithm is implemented in such a way that the choice of the minimization-criterion can be done by the user in a very simple way by changing only one line of code in a sub-function. Also worthwhile mentioning is that for fitting of glacial $\delta^{15}\text{N}$ data we used a L2 norm weighted with the data uncertainties. To summarize: There is no special reason for the use of one norm instead of the other one. Both norms can be used in a sufficient way.

Page 9, Line 8 –

“If the mismatch decreases compared to the prior input, the new input is saved and used as new guess.”

5 *I thought that in most Monte Carlo applications, there was also a probability that a result would not be accepted, even if it had a lower mismatch. Why is that not done here?*

10 For the current version of the algorithm a new seed of the random generator is set each time before new random values are being generated. That means if the Monte-Carlo algorithm is used several times on the same target, the “way” to the final result is different for any case. This is done to prevent the algorithm for falling into the same local minimum during the minimization and leads to a certain band of solutions (not discussed in the paper). Further, the fact that we do select only the solutions that improve our criteria of minimization corresponds to a probability function.

15 *In their response to reviewers (page 13), the authors argue that their paper is appropriate for publication in CP, because another methods paper (Winstrup et al., 2012) was previously welcomed and published in CP. While the decision to publish or not resides with the editors, I personally think that it is obvious that Winstrup et al. is a methods paper, and the Winstrup et al. paper is much clearer and more accessible to readers than this manuscript in its current form. The editors must also consider these factors.*

20 We fully agree this was an unnecessary statement and of course the decision about an adequate manuscript is taken by the editor. Yet, we are convinced that our manuscript fits well into the Climate of the Past journal since it describes a method for investigating paleo proxy-records regarding temperature variations in the past.

Details

When acronyms are well established in the broad scientific literature, it is fine to use them. However, very little space is saved when authors introduce new acronyms for phrases that are relatively short and which are used relatively infrequently. Writing the phrase in full for clarity whenever it is used makes reading more efficient and produces happier readers, who don't need to search back through dense text to find the meaning. For example,

is using "cop" for "cut-off period" really necessary? I think the manuscript would benefit from a table of variables (and acronyms). If reader are going to need to frequently look up meanings of variables and acronyms, it would at least make it easier for them if there was one clearly identified place to go for that information.

We fully agree to the reviewer that used acronyms should be well established when used in a paper. For that reason we consequently changed the acronym "cop" to "cut-off-period" in the whole manuscript. Yet, we keep the abbreviation since it is used in Fig. 01 and Table 1.

Hyphens

The manuscript is nearly devoid of hyphens, although in many instances, correctly used hyphens would eliminate minor textual stumbling blocks that can slow readers' grasp of the material. For example – • Page 3, line 1 – "... argon-isotope-based temperature reconstructions."

Or better,

"... temperature reconstructions based on argon isotopes."

• Page 3, line 24 – "... Holocene-like data ..."

• Page 6, line 19 – "low-pass filtered:

• Page 8, line 30 – "first-guess temperature"

• Page 6, line 21 - "... accumulation-rate data ..."

• Page 16, line 14 – "gas-isotope-based temperature reconstructions ...", or better, "temperature reconstructions based on gas isotopes ...",

We changed all the points as it was suggested by the reviewer. Also we reformulate sentences and add hyphens in the text when it was necessary.

Data are plural

• Page 6, line 21 - "... data are linearly interpolated ..."

• Page 6, line 24 - "... data were linearly indeed reconstructed ..."

• Page 8, line 2 – "... data are filtered ..."

• Page 17, line 5 – "... gas-isotope data are calculated ..."

• Page 18, line 11 – "... data are used to run ..."

We corrected all the points as it was suggested by the reviewer. We also corrected the wrong grammar according to this in the rest of the manuscript.

Page 1, line 26 –

"This is shown by high quality fitting of NGRIP $\delta^{15}\text{N}$ data for two Dansgaard-Oeschger events using the presented approach, leading to results comparable to other studies."

"High quality" is wordy and can appear to be an attempt to prejudice how readers will view the results. It can often be more convincing to simply state that results were comparable, and let readers decide for themselves whether or not the fit was "high quality". If the authors want to retain "high-quality fitting", then it needs a hyphen.

We agree that the used phrase "high quality fitting..." may bias the reader and influence the judgement of the presented details. We changed the formulation of the sentence (p.1 l.26) to:

"This is shown by fitting of NGRIP $\delta^{15}\text{N}$ data for two Dansgaard-Oeschger events using the presented approach, leading to results comparable to other studies."

Page 17, line 23 – *The distance between GRIP and GISP3 is ~30 km, it is not “a few km”. The authors are correct that more cores closer together could be very useful.*

We corrected for that and reformulated the sentence to:

5 “For example, a $\delta^{15}\text{N}$ -based temperature reconstruction from the combination of data from the GISP2 ice core with the “sister ice core” GRIP drilled 30 kilometres apart is likely one of the best ways to overcome potential cm-scale variability.”

10 **Clarity**

• Page 1, line 15 – *“... parameter tuning leading to ...” I think there should be a comma after “tuning. Without a comma it is unclear whether the phrase “leading to reproducible temperature estimates” refers to the new automated approach or to the old manual approach. I think the former, but some readers may stumble on this point.*

15

We corrected for that and added the comma as suggested by the reviewer:

“The presented approach is completely automated and therefore minimizes the “subjective” impact of manual parameter-tuning, leading to reproducible temperature-estimates.”

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• Page 1, line 16 –

“... other ice core based temperature reconstruction methods ...”.

Please try to avoid long strings of adjectives especially if you don’t use hyphens to help readers understand the groupings. Better, with hyphens, “... other ice-core-based temperature-reconstruction methods ...” Or better yet, unpacked, “... other temperature-reconstruction methods based on ice cores ...”.

25

We changed the sentence according to the suggestion by the reviewer:

“In contrast to many other temperature-reconstruction methods based on ice cores, the presented approach is completely independent from ice-core stable-water-isotopes, providing the opportunity to validate water-isotope-based reconstructions or reconstructions where water isotopes are used together with $\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$.”

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• Page 2, line 3 - *What is intended by “partly even centennial ... variations”? This is not a English expression that I understand.*

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We corrected for that and changed the sentence to:

“Yet, high-resolution studies are still very sparse and therefore limit the investigation of decadal and even centennial climate variations over the course of the Holocene.”

40

• Page 2, line 14 – *There is no “Cuffey et al. (1997)” reference. The correct reference is “Cuffey and Clow (1997)”.*

We corrected the wrong reference:

45 “The studies of Cuffey et al. (1995), Cuffey and Clow (1997) and Dahl-Jensen et al. (1998) demonstrate the usefulness of inverting the measured borehole-temperature profile for surface-temperature-history estimates for the investigated drilling site using a coupled heat- and ice-flow model.”

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• Page 4 – *“g is the acceleration constant.” I think it is standard practice to mention “gravity” in this context.*

We changed the terminology here to:

“g is the gravitational acceleration, ...”

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• Page 8, line 8 – *“... which serve later on as ...” Delete “on”.*

We corrected for that and deleted the “on”:

60 “In order to develop and evaluate the presented algorithm, eight temperature scenarios were constructed and used to model synthetic $\delta^{15}\text{N}$ data, which serve later as targets for the reconstruction.”

• Page 8, line 31 – “... of about -29.60C”. Did you use -29.60C, or did you use something different? Why not just say “... of -29.6°C”?

We changed the sentence to:

5 “To construct the first-guess temperature-input $T_{g,0}(t)$, a constant temperature of -29.6 °C is used for the complete Holocene section, which corresponds to the last value of the temperature spin-up (Fig. 02b).”

Tables

10 In Table 01, I don’t see the point of saying that calculations ran over a weekend. Surely the days of the week are unimportant (are Saturdays really better than Wednesdays?). If the point is the execution time, then state “48 hours” or “N cpu cycles”, or whatever is the appropriate number.

15 We fully agree to the reviewer that the presented algorithm is independent from the exact date of use. We wanted to provide an explanation for the significant higher execution time for three runs. As it is not important for the description of the algorithm we deleted the line “Comments” of that table together with the statement, “3 runs were conducted over weekend, which leads to a higher number of iterations;”, in the description.

References

20 • Guillevic (2013). PhD thesis. More information would be helpful – title, university, accessibility.

25 Guillevic, M., Characterisation of rapid climate changes through isotope analyses of ice and entrapped air in the NEEM ice core, PhD thesis, University of Copenhagen, Université de Versailles Saint Quentin en Yvelines, 2013.

• Schwander et al. (1997) should have a hanging indent, not be fully indented.

30 We corrected for that.

• Severinghaus et al. (1998) should have hanging indent. “Sowers” and “Alley” are mis-spelled.

We corrected for that:

35 “Severinghaus, J. P., Sowers, T. and Alley, R. B.: Timing of abrupt climate change at the end of the Younger Dryas interval from thermally fractionated gases in polar ice, Nature, 39(January), 141–146, doi:10.1002/jqs.622, 1998.”

40 • Spahni (2003) Check how “CH 4” is presented in GRL.

We corrected for that:

45 “Spahni, R.: The attenuation of fast atmospheric CH₄ variations recorded in polar ice cores, Geophys. Res. Lett., 30(11), 1571, doi:10.1029/2003GL017093, 2003.”

• Steig et al. (1994). Only the first word in the title (“Seasonal”) should be capitalized.

We corrected for that:

50 “Steig, E. J., Grootes, P. M. and Stuiver, M.: Seasonal precipitation timing and ice core records, Science, 266(5192), 1885–1886, doi:10.1126/science.266.5192.1885, 1994.”

• Werner et al. (2001) Missing space in “... present and ...”

55 We corrected for that:

“Werner, M., Heimann, M. and Hoffmann, G.: Isotopic composition and origin of polar precipitation in present and glacial climate simulations, Tellus Ser. B Chem. Phys. Meteorol. B, 53(1), 53–71, doi:10.1034/j.1600-0889.2001.01154.x, 2001.”

Novel automated inversion algorithm for temperature reconstruction using gas isotopes from ice cores

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Keywords: temperature reconstruction, ice core, nitrogen isotope, argon isotope, inverse model, firm model, [accumulation rate](#)

10 **Abstract.** Greenland past temperature history can be reconstructed by forcing the output of a firn-densification and heat-diffusion model to fit multiple gas-isotope data ($\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$ or $\delta^{15}\text{N}_{\text{excess}}$) extracted from ancient air in Greenland ice cores- [using published accumulation-rate \(Acc\) data sets](#). We present here a novel methodology to solve this inverse problem, by designing a fully-automated algorithm. To demonstrate the performance of this novel approach, we begin by intentionally constructing synthetic temperature-histories and associated $\delta^{15}\text{N}$ datasets, mimicking real Holocene data that

15 we use as “true values” (targets) to be compared to the output of the algorithm. This allows us to quantify uncertainties originating from the algorithm itself. The presented approach is completely automated and therefore minimizes the “subjective” impact of manual parameter-tuning, leading to reproducible temperature-estimates. In contrast to many other ice-core-based temperature-reconstruction methods, the presented approach is completely independent from ice-core stable-water-isotopes, providing the opportunity to validate water-isotope-based reconstructions or reconstructions where

20 water isotopes are used together with $\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$. We solve the inverse problem $T(\delta^{15}\text{N}, \text{Acc})$ by using a combination of a Monte-Carlo-based iterative approach and the analysis of remaining mismatches between modelled and target data, based on cubic-spline-filtering of random numbers [as well as and](#) the laboratory-determined temperature-sensitivity for nitrogen isotopes. Additionally, the presented reconstruction approach was tested by fitting measured $\delta^{40}\text{Ar}$ and $\delta^{15}\text{N}_{\text{excess}}$ data, which leads as well to a robust agreement between modelled and measured data. The obtained final mismatches follow a symmetric

25 standard-distribution-function. For the [study on synthetic data-study](#), 95 % of the mismatches compared to the synthetic target-data are in an envelope between 3.0 permeg to 6.3 permeg for $\delta^{15}\text{N}$ and 0.23 K to 0.51 K for temperature (2σ , respectively). In addition to Holocene temperature-reconstructions, the fitting approach can also be used for glacial temperature-reconstructions. This is shown by [high quality](#) fitting of NGRIP $\delta^{15}\text{N}$ data for two Dansgaard-Oeschger events using the presented approach, leading to results comparable to other studies.

1 Introduction

Holocene climate variability is of key interest to our society, since it represents a time of moderate natural variations prior to anthropogenic disturbance, often referred to as a baseline for today's increasing greenhouse effect driven by mankind. Yet, high-resolution studies are still very sparse and therefore limit the investigation of decadal and partly even centennial climate variations over the course of the Holocene. One of the first studies about changes in the Holocene climate was conducted in the early 1970s by Denton and Karle'n (1973). The authors investigated rapid changes in glacier extents around the globe potentially resulting from variations of Holocene climatic conditions. Mayewski et al. (2004) used this data as the base of a multiproxy study identifying rapid climate changes (so-called RCCs) globally distributed over the whole Holocene time period. Although not all proxy data are showing an equal behaviour in timing and extent during the quasi-periodic RCC patterns, the authors found evidence for a highly variable Holocene climate controlled by multiple mechanisms, which significantly affects ecosystems (Pál et al., 2016; Beaulieu et al., 2017; Crausbay et al., 2017) and human societies (Holmgren et al., 2016; Lespez, L. et al., 2016). Precise high-resolution temperature estimates can contribute significantly to the understanding of these mechanisms. Ice-core proxy data offer multiple paths for reconstructing past climate and temperature variability. The studies of Cuffey et al. (1995; 1997) and Dahl-Jensen et al. (1998) demonstrate the usefulness of inverting the measured borehole temperature profile for surface temperature history estimates for the investigated drilling site using a coupled heat and ice flow model. Because of smoothing effects due to heat diffusion within an ice sheet, this method is unable to resolve fast temperature oscillations and leads to a rapid reduction of the time resolution towards the past. Another approach to reconstruct past temperature is based on the calibration of stable water isotopes of oxygen and hydrogen ($\delta^{18}\text{O}_{\text{ice}}$, $\delta\text{D}_{\text{ice}}$) from ice-core water samples assuming a constant (and mostly linear) relationship between temperature and water isotopic composition due to fractionation effects during ocean evaporation, cloud formation and snow and ice precipitation (Stuiver et al., 1995; Johnsen et al., 2001). This method provides a rather robust tool for reconstructing past temperature for times where large temperature excursions occur (Dansgaard-Oeschger events, Glacial-Interglacial transitions (Dansgaard et al., 1982; Johnsen et al., 1992)). However, in the Holocene where Greenland temperature variations are comparatively small, seasonal changes of precipitation as well as of evaporation conditions at the source region contribute possibly more to water isotope data variations (Werner et al., 2001; Huber et al., 2006; Kindler et al., 2014). A relatively new method for ice-core based temperature reconstructions uses the thermal fractionation of stable isotopes of air compounds (nitrogen and argon) within a firn layer of an ice sheet (Severinghaus et al., 1998; Severinghaus et al., 2001; Huber et al., 2006; Kobashi et al., 2011; Kindler et al., 2014). The measured nitrogen and argon isotope records of air enclosed in bubbles in an ice core can be used as a paleothermometer due to (i) the stability of isotopic compositions of nitrogen and argon in the atmosphere at orbital timescales and (ii) the fact that changes are only driven by firn processes (Mariotti, 1983; Severinghaus et al., 1998; Leuenberger et al., 1999). To robustly reconstruct the surface temperature for a given drilling site, the use of firn models describing gas and heat diffusion throughout the ice sheet is necessary for decomposing the gravitational from the thermal diffusion influence on the isotope signals.

This work addresses two issues relevant for nitrogen and argon isotope based temperature reconstructions. First, we introduce a novel, entirely automated approach for inverting gas isotope data to surface temperature estimates. For that, we force the output of a firn densification and heat diffusion model to fit gas isotope data. This methodology can be used for many different optimization tasks not restricted to ice core data. As we will show, the approach works besides $\delta^{15}\text{N}$ for all relevant gas isotope quantities ($\delta^{15}\text{N}$, $\delta^{40}\text{Ar}$, $\delta^{15}\text{N}_{\text{excess}}$) and for Holocene and glacial data as well. Furthermore, the possibility of fitting all relevant gas isotope quantities, individually or combined, makes it possible for the first time to validate the temperature solution gained from one single isotope species by comparison to the solution calculated from other isotope quantities. This approach is a completely new method which enables the automated fitting of gas isotope data without any manual tuning of parameters, minimizing any potential “subjective” impacts on temperature estimates as well as working hours. Also, except for the model spin up, the presented temperature reconstruction approach is completely independent from stable water isotopes ($\delta^{18}\text{O}_{\text{ice}}$, $\delta\text{D}_{\text{ice}}$), which provides the opportunity to validate water isotope based reconstructions (e.g. Masson Delmotte, 2005) or reconstructions where water isotopes are used together with $\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$ (e.g. Landais et al., 2004; Huber et al., 2006; Capron et al., 2010). To our knowledge, there are only two other reconstruction methods independent from stable water isotopes that have been applied to Holocene gas isotope data, without a priori assumption on the shape of a temperature change. The studies from Kobashi et al. (2008a, 2017) use the second order parameter $\delta^{15}\text{N}_{\text{excess}}$ to calculate firn temperature gradients, which are later temporally integrated from past to future over the time series of interest using the firn densification and heat diffusion model from Goujon et al. (2003). Additionally Orsi et al. (2014) use a linearized firn model approach together with $\delta^{15}\text{N}$ and $\delta^{40}\text{Ar}$ data to extract surface temperature histories. As both methods rely on $\delta^{15}\text{N}$ together with $\delta^{40}\text{Ar}$, they do not offer the possibility to validate one isotope based solution against the other. Also these two approaches can only be applied to ice cores where both isotope quantities are measured together with a sufficient precision.

Second, we investigate the accuracy of our novel fitting approach by examining the method on different synthetic nitrogen-1 Introduction

Holocene climate variability is of key interest to our society, since it represents a time of moderate natural variations prior to anthropogenic disturbance, often referred to as a baseline for today’s increasing greenhouse effect driven by mankind. Yet, high-resolution studies are still very sparse and therefore limit the investigation of decadal and even centennial climate variations over the course of the Holocene. One of the first studies about changes in the Holocene climate was conducted in the early 1970s by Denton and Karle’n (1973). The authors investigated rapid changes in glacier extents around the globe potentially resulting from variations of Holocene climatic conditions. Mayewski et al. (2004) used these data as the base of a multiproxy study identifying rapid climate changes (so called RCCs) globally distributed over the whole Holocene time period. Although not all proxy data are showing an equal behaviour in timing and extent during the quasi-periodic RCC patterns, the authors found evidence for a highly variable Holocene climate controlled by multiple mechanisms, which

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25 This work addresses two issues relevant for temperature reconstructions based on nitrogen and argon isotopes. First, we introduce a novel, entirely automated approach for inverting gas-isotope data to surface-temperature estimates. For that, we force the output of a firn-densification and heat-diffusion model to fit gas-isotope data. This methodology can be used for many different optimization tasks not restricted to ice-core data. As we will show, the approach works besides $\delta^{15}\text{N}$ for all relevant gas-isotope quantities ($\delta^{15}\text{N}$, $\delta^{40}\text{Ar}$, $\delta^{15}\text{N}_{\text{excess}}$) and for Holocene and glacial data as well. Furthermore, the possibility of fitting all relevant gas-isotope quantities, individually or combined, makes it possible for the first time to validate the temperature solution gained from one single isotope species by comparison to the solution calculated from other isotope quantities. This approach is a completely new method which enables the automated fitting of gas-isotope data without any manual tuning of parameters, minimizing any potential “subjective” impacts on temperature estimates as well as working hours. Also, except for the model spin-up, the presented temperature-reconstruction approach is completely independent from water stable-isotopes ($\delta^{18}\text{O}_{\text{ice}}$, $\delta\text{D}_{\text{ice}}$), which provides the opportunity to validate water-isotope-based reconstructions

(e.g. Masson-Delmotte, 2005) or reconstructions where water isotopes are used together with $\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$ (e.g. Landais et al., 2004; Huber et al., 2006; Capron et al., 2010). To our knowledge, there are only two other reconstruction methods independent from water stable-isotopes that have been applied to Holocene gas-isotope data, without a priori assumption on the shape of a temperature change. The studies from Kobashi et al. (2008a, 2017) use the second order parameter $\delta^{15}\text{N}_{\text{excess}}$ to calculate firn-temperature gradients, which are later temporally integrated from past to future over the time-series of interest using the firn-densification and heat-diffusion model from Goujon et al. (2003). Additionally Orsi et al. (2014) use a linearized firn-model approach together with $\delta^{15}\text{N}$ and $\delta^{40}\text{Ar}$ data to extract surface-temperature histories. As both methods rely on $\delta^{15}\text{N}$ together with $\delta^{40}\text{Ar}$, they do not offer the possibility to validate one isotope-based solution against the other. Also these two approaches can only be applied to ice cores where both isotope quantities are measured together with a sufficient precision.

Second, we investigate the accuracy of our novel fitting approach by examining the method on different synthetic nitrogen-isotope and temperature scenarios. The aim of this work is to study the uncertainties emerging from the algorithm itself. Furthermore the focal question in this study is: what is the minimal mismatch in $\delta^{15}\text{N}$ for Holocene-like data we can reach and what is the implication for the final temperature mismatches. Studying and moreover answering these questions makes it mandatory to create well defined $\delta^{15}\text{N}$ targets and related temperature histories. It is impossible to answer these questions without using synthetic data in a methodology study. The aim is to evaluate the accuracy and associated uncertainty of the inverse method itself to then later apply this method to real $\delta^{15}\text{N}$, $\delta^{40}\text{Ar}$ or $\delta^{15}\text{N}_{\text{excess}}$ datasets, for which of course the original driving temperature histories are unknown.

2. Methods and data

2.1 Firn densification and heat diffusion model

The surface temperature reconstruction relies on firn densification combined with gas and heat diffusion (Severinghaus et al., 1998). In this study, the firn densification and heat diffusion model, from now on referred to as firn model, developed by Schwander et al. (1997) is used to reconstruct firn parameters for calculating synthetic $\delta^{15}\text{N}$ values depending on the input time series. It is a semi-empirical model based on the work of Herron and Langway (1980), Barnola et al. (1991), and implemented using the Crank and Nicholson algorithm (Crank, 1975) and was also used for the temperature reconstructions by Huber et al. (2006) and Kindler et al. (2014). Besides surface temperature time series, accurate accumulation rate data is needed to run the model. The model then calculates the densification and heat

The problem that we deal with is an inverse problem, since the effect, observed as $\delta^{15}\text{N}$ variations, is dependent on its drivers, i.e. temperature and accumulation-rate changes. Hence, the temperature that we would like to reconstruct depends on $\delta^{15}\text{N}$ and accumulation-rate changes. To solve this inverse problem, the firn-densification and heat-diffusion model (from now on referred to as firn model), which is a non-linear transfer function of temperature and accumulation rate to firn states and relates to $\delta^{15}\text{N}$ values, is run iteratively to match the modelled and measured $\delta^{15}\text{N}$ values (or other gas species). The automated procedure is significantly more efficient and less time-consuming than a manual approach. The Holocene temperature-reconstruction is implemented by the following four steps (Fig. 01):

Step 1: diffusion history of the firn layer and provides parameters for calculating the fractionation of the nitrogen isotopes for each time step, according to the following equations:

$$\delta^{15}\text{N}_{\text{grav}}(z_{\text{LID}}, t) = \left(e^{\frac{\Delta m \cdot g \cdot z_{\text{LID}}(t)}{R \cdot \bar{T}(t)}} - 1 \right) \cdot 1000 \quad (1)$$

$$\delta^{15}\text{N}_{\text{therm}}(t) = \left[\left(\frac{T_{\text{surr}}(t)}{T_{\text{bottom}}(t)} \right)^{\alpha_T} - 1 \right] \cdot 1000 \quad (2)$$

$$\delta^{15}\text{N}_{\text{mod}}(t) = \delta^{15}\text{N}_{\text{grav}}(t) + \delta^{15}\text{N}_{\text{therm}}(t) \quad (3)$$

$\delta^{15}\text{N}_{\text{grav}}(t)$ is the component of the isotopic fractionation due to the gravitational settling (Craig et al., 1988; Schwander, 1989) and depends on the lock-in depth (LID) $z_{\text{LID}}(t)$ and the mean firn temperature $\bar{T}(t)$ (Leuenberger et al., 1999). g is the acceleration constant, Δm the molar mass difference between the heavy and light isotopes (equals 10^{-3} kg for nitrogen) and R the ideal gas constant. z_{LID} is defined as a density threshold ρ_{LID} , which is slightly sensitive to surface temperature, following the formula from Martinerie et al. (1994), with a small offset correction of 14 kg m^{-3} to account for the presence of a non-diffusive zone (Schwander et al., 1997):

$$\rho_{\text{LID}}(\text{kg} \cdot \text{m}^{-3}) = \frac{1}{\frac{1}{\rho_{\text{ice}}} - 6.95 \cdot 10^{-7} \cdot \bar{T} - 4.3 \cdot 10^{-5}} - 14 \quad (4)$$

where

$$\rho_{\text{ice}}(\text{kg} \cdot \text{m}^{-3}) = 916.5 - 0.14438 \cdot \bar{T} - 1.5175 \cdot 10^{-4} \cdot \bar{T}^2 \quad (5)$$

The thermal fractionation component of the $\delta^{15}\text{N}$ signal (Severinghaus et al., 1998) is calculated using Eq. (2), where $T_{\text{surf}}(t)$ and $T_{\text{bottom}}(t)$ stand for the temperatures at the top and the bottom of the diffusive firn layer. ~~In contrast to $T_{\text{surf}}(t)$ which is an input parameter for the model, $T_{\text{bottom}}(t)$ is calculated by the model for each time step. The thermal diffusion constant α_T was measured by Grachev and Severinghaus (2003) for nitrogen (see Eq. (6)), and closely matches the value used by Leuenberger et al. (1999) based on measurements of Boersma Klein and De Vries (1966):~~

$$\alpha_T = \left(8.656 - \frac{1323 \text{ K}}{T} \right) \cdot 10^{-3} \quad (6)$$

The firn model used here behaves purely as a forward model, which means that for the given input time series the output parameters (here finally $\delta^{15}\text{N}_{\text{mod}}(t)$) can be calculated, but it is not easily possible to construct from measured isotope data the related surface temperature or accumulation rate histories. The goal of the presented study is an automatization of this inverse modelling procedure for the reconstruction of the rather small Holocene temperature variations.

2.2 Measurement, input data and time scale

~~**Accumulation rate data:** Besides surface temperatures, accumulation rate data is needed to drive the firn model. In this study we use the original accumulation rate, reconstructed in Cuffey and Clow (1997) produced using an ice flow model adapted to the GISP2 location, but adapted to the GICC05 chronology (Rasmussen et al., 2008; Seierstad et al., 2014). Originally, the accumulation rate used to feed the ice flow model was optimised in order to match the time scale from Meese et al. (1994) for the Holocene, based on annual layer counting. Seierstad et al. (2014) transferred the GISP2 chronology to the GICC05 reference timeframe using multiple match points to the NGRIP and GRIP ice cores, both already on GICC05. We used these match points and modified the GISP2 ages in between match points linearly in order to match exactly the GICC05 duration for the considered interval duration. This way, the detailed GISP2 annual layer counting information is kept, but is only stretched/compressed in time. This was done for all intervals in between two match points. The accumulation data were then re-calculated accordingly as obviously this is needed in order to keep the same total amount of ice accumulated at the GISP2 site. From the three accumulation rate scenarios reconstructed in Cuffey and Clow (1997) and adapted here to the GICC05 chronology, the intermediate one is chosen (red curves in Fig. S01). Since the differences between the scenarios (Fig. S01) are not important for the evaluation of the reconstruction approach, they are not taken into account for this study.~~

~~**$\delta^{18}\text{O}_{\text{ice}}$ data:** Oxygen isotope data from the GISP2 ice core water samples measured at the University of Washington's Quaternary Isotope Laboratory is used to construct the surface temperature input of the model spin up (12 yr to 35 kyr b2k; see Sect. 2.3.1) (Groote et al., 1993; Meese et al., 1994; Steig et al., 1994; Stuiver et al., 1995; Groote and Stuiver, 1997).~~

~~**Time scale:** For the entire study the GICC05 chronology is used (Rasmussen et al., 2014; Seierstad et al., 2014). During the whole reconstruction procedure the two input time series (surface temperature and accumulation rate) are split into two parts.~~

~~The first part ranges from 20 yr to 10520 yr b2k (called “Holocene section”) and the second one from 10520 yr to 35000 yr b2k (“spin up section”). The entire accumulation rate input (see Sect. 2.3.1), as well as the spin up section of the surface temperature input, remain unchanged during the reconstruction procedure.~~

2.3 Reconstruction approach

The Holocene temperature reconstruction is implemented by the following four steps:

(i) A prior temperature input (first guess) is constructed, which serves as the starting point for the optimization.

(ii) **Step 2:** A smoothlong-term solution which passes through the $\delta^{15}\text{N}$ data (here synthetic target data) is generated following a Monte-Carlo approach. It is assumed that the smooth solution contains all long-term temperature trends (centuries to millennial) as well as firm-column-height changes (temperature and accumulation-rate dependent) that drive the gravitational background signal in $\delta^{15}\text{N}$.

(iii) **Step 3:** The smoothlong-term temperature solution is complemented by superimposing high-frequencyshort-term information directly extracted from the $\delta^{15}\text{N}$ data (here synthetic target data). This step adds short-term temperature changes (decadal) in the same time resolution as the data.

(iv) **Step 4:** The gained temperature solution is further corrected using information extracted from the mismatch between the synthetic target and modelled $\delta^{15}\text{N}$ time-series.

Accumulation rate input:

The raw accumulation rate data for the main part of the spin up section (12000-yr to 35000-yr b2k) is linearly interpolated to a 20-yr grid and low-pass filtered with a 200-yr cut-off period (cop) using cubic spline filtering (Enting, 1987). For the Holocene section (20-10520-yr b2k) and the transition part between Holocene and spin up section (10520-yr to 12000-yr b2k) the raw accumulation rate data is linearly interpolated to a 1-yr grid to obtain equidistant integer point to point distances which are necessary for the reconstruction, and to preserve as much information as possible for this time period (Fig. S02a). Except for these technical adjustments, the accumulation rate input data remains unmodified, assuming high reliability of this data during the Holocene. The accumulation data was indeed reconstructed using annual layer counting, and a thinning model which should lead to maximum relative uncertainty of 10 % for the first 1500 m of the 3000 m ice core (Cuffey and Clow, 1997).

In order to investigate the influence of smoothing of the accumulation rate data on the model outputs, the high resolution accumulation rate dataset in the time window of 20 yr to 12000-yr (Fig. S02a) was low-pass filtered with cops between 20 yr and 500 yr, and used to drive the firm model. The surface temperature input was set as constant with a value of $-31\text{ }^\circ\text{C}$ for this time window. Then, the deviations of the filtered from the unfiltered accumulation rates and model outputs were calculated. Figure S03 shows the absolute (I) as well as the relative deviations (II) (relative to the unfiltered scenario) as a function of the cops for the accumulation rate input data, $\delta^{15}\text{N}$, and LID model outputs. Regarding the standard deviation (1σ) of the relative accumulation deviations as a measure for the mean deviation of the filtered minus the unfiltered values show that

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filtering the accumulation rates leads to a mean deviation of about 20 % between the filtered and unfiltered accumulation rate data, depending on the used cop value (see Fig. S03IIa). We use the mean 99 % quantile of the same analysis (Fig. S03IIb) as a measure for the maximum deviation between the filtered and unfiltered values. The filtering clearly leads to a maximum accumulation rate deviation of about 50 %. The comparison of the related deviations in $\delta^{15}\text{N}$ and LID outputs reveals that the changes in the accumulation rates do not lead to a change in the same order for the model outputs. Indeed, the filtering of the accumulation rate data leads to deviations of less than 0.6 % and less than 1.5 % for the mean and the maximum $\delta^{15}\text{N}$ and LID deviations respectively (Fig. S03IIc,d). Therefore, it can be argued that a low pass filtering of the accumulation rates for cops between 20 yr and 500 yr does only have a small impact on the model outputs as long as the major trends are being conserved, because the filtering does not modify the mean accumulation. This result is expected due to the fact that the LID and finally $\delta^{15}\text{N}$ changes are the result of the integration of the accumulation over the whole firn column. The integration time corresponds to the age of the ice at the LID, which is the order of 200 yr for the Holocene in Greenland.

Finally, we test which fraction of the measured $\delta^{15}\text{N}$ variations can be attributed to accumulation changes. For this, we perform a sensitivity experiment (Fig. S04) where the temperature input was set as a constant value of -31°C , and used together with the high resolution accumulation rate data (Fig. S02a) to model the LID (Fig. S04a) and $\delta^{15}\text{N}$ (Fig. S04b) values. Due to the absence of temperature changes, only the accumulation rate changes drive the evolution of the diffusive column height (LID) over time which modulates the $\delta^{15}\text{N}$ values. Next, the modelled $\delta^{15}\text{N}$ variations are compared to the $\delta^{15}\text{N}$ measurement data (Fig. S06III) (Kobashi et al., 2008b) to examine the influence of the accumulation rate changes on changes in $\delta^{15}\text{N}$ for two cases. First, for the 8.2k event, the signal amplitude in $\delta^{15}\text{N}$ is about three times higher for the measured data compared to the modelled ones (measured data: $\Delta\delta^{15}\text{N}_{8.2\text{k},\text{meas}} \sim 60$ permeg (one permeg equals 10^{-6}); modelled data: $\Delta\delta^{15}\text{N}_{8.2\text{k},\text{mod}} \sim 20$ permeg). The comparison of the standard deviations of the measured data with the modelled $\delta^{15}\text{N}$ data for the last 10 kyr (both quantities were normalized with their respective means), shows an even higher deviation of the measured versus the modelled variabilities by a factor of about eight (measured data: $\text{std}[\delta^{15}\text{N}_{10\text{kyr},\text{meas}} - \text{mean}(\delta^{15}\text{N}_{10\text{kyr},\text{meas}})] \sim 37$ permeg; modelled data: $\text{std}[\delta^{15}\text{N}_{10\text{kyr},\text{mod}} - \text{mean}(\delta^{15}\text{N}_{10\text{kyr},\text{mod}})] \sim 4.5$ permeg). This analysis supports our assumption that the accumulation rate history alone cannot fully explain the observed variability in $\delta^{15}\text{N}$ during the Holocene, and gives an upper limit for the contribution of the accumulation rate to the $\delta^{15}\text{N}$ signal. Therefore, the remaining part of the measured $\delta^{15}\text{N}$ variations has to be related to changes in surface temperature.

Surface temperature spin up:

The surface temperature history of the spin up section (Fig. S02b) is obtained by calibrating the filtered and interpolated $\delta^{18}\text{O}_{\text{ice}}$ data (Eq. (7)) using the values for the temperature sensitivity $\alpha_{18\text{O}}$ and offset β found by Kindler et al. (2014) for the NGRIP ice core assuming a linear relationship of $\delta^{18}\text{O}_{\text{ice}}$ with temperature.

$$T_{\text{spin}}(t) = \frac{1}{\alpha_{18\text{O}}(t)} \cdot [\delta^{18}\text{O}_{\text{ice}}(t) + 35.2 \text{‰}] - 31.4^\circ\text{C} + \beta(t) \quad (7)$$

The values 35.2 ‰ and 31.4 °C are modern time parameters for the GISP2 site (Schwander et al., 1997; Grootes and Stuiver, 1997). The raw $\delta^{18}\text{O}_{\text{ice}}$ data is filtered and interpolated in the same way as the accumulation rate data for the spin up part. The spin up is needed to bring the firm model to a well defined starting condition that takes possible memory effects (influence of earlier conditions) of firm states into account.

Generating synthetic target data:

In order to develop and evaluate the presented algorithm, eight temperature scenarios were constructed and used to model synthetic $\delta^{15}\text{N}$ data, which serve later on as targets for the reconstruction. From these eight synthetic surface temperature and related $\delta^{15}\text{N}$ scenarios (S1-S5 and H1-H3), three data sets (later called Holocene like scenarios H1-H3) were constructed in such a way that the resulting $\delta^{15}\text{N}$ time series are very close to the $\delta^{15}\text{N}$ values measured by Kobashi et al. (2008) in terms of variability (amplitudes) and frequency (data resolution) of the GISP2 nitrogen isotope data (Fig. S05, Fig. S06).

The synthetic surface temperature scenarios S1-S5 are created by generating a smooth temperature time series ($T_{\text{syn,smooth}}$) analogous to the Monte Carlo part of the reconstruction procedure for only one iteration step (see Sect. 2.3.2). The values for the cop used for the filtering of the random values, and the s values (standard deviation of the random values, see Sect. 2.3.2) for the first 5 scenarios can be found in table S01. The smooth temperatures (Fig. S05I) are calculated on a 20-yr grid, which is nearly similar to the time resolution of the GISP2 $\delta^{15}\text{N}$ measurement values of about 17 yr (Kobashi et al., 2008b). For the Holocene like scenarios, the smooth temperature time series were generated from the temperature reconstruction for the GISP2 $\delta^{15}\text{N}$ data (not shown here). The final Holocene surface temperature solution was filtered with a 100-yr cop to obtain the smooth temperature scenario.

Following this, high frequency information is added to the smoothed temperature histories. A set of normally distributed random numbers with a zero mean and a standard deviation (1σ) of 1 K for scenarios S1-S5 and 0.3 K for Holocene like scenarios H1-H3 is generated on the same 20-yr grid and added up to the smooth temperature time series. Finally, the resulting synthetic target temperature scenarios (Fig. S05II, Fig. S06I) are linearly interpolated to a 1-yr grid.

These synthetic temperatures are combined with the spin up temperature and are used together with the accumulation rate input to feed the firm model. From the model output the synthetic $\delta^{15}\text{N}$ targets are calculated according to section 2.1. The firm model output provides ice age as well as gas age information. The final synthetic $\delta^{15}\text{N}$ target time series (Fig. S05III, Fig. S06II) are set intentionally on the ice age scale to mirror measured data, because no prior information is available for the gas-ice age difference (Δage) for ice core data.

2.3.1 Prior input (step 1)

The functionality of the presented inversion algorithm is schematically displayed in Fig. 01. It guides the reader through chapters and documents which variables, listed in Table 01, are in use. In the following a detailed description of each step is given.

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Step 1: prior input

The starting point of the optimization procedure is the first-guess. To construct the first-guess temperature-input $T_{g,0}(t)$, a constant temperature of about -29.6 °C is used for the complete Holocene section, which corresponds to the last value of the temperature spin-up (Fig. S02b).

Step 2.3.2: Monte-Carlo-type input-generator - Generating smooth long-term solutions (step 2)

During the second step of the optimization, the prior temperature-input $T_{g,0}(t)$ from step 1 is iteratively (i) changed following a Monte-Carlo approach. The basic idea of the Monte-Carlo approach is to generate smooth temperature-inputs $T_{mc,i}(t)$ by superimpose low-pass filtering-filtered values \vec{P}_i of uniformly-distributed random values, and to superimpose this signal \vec{P}_i on the prior input $T_{mc,i-1}$. Then, the new input is fed to the firm model and the mismatch D_{mc} in $D_{\delta^{15}N_{mc,i}}$ (with $X \equiv \delta^{15}N_{mc,i}$) between the modelled $\delta^{15}N$ signal $\delta^{15}N_{mc,i}$ (here $X_{mod,i}$), calculated from the model output, and the synthetic $\delta^{15}N$ target values $\delta^{15}N_{syn}$ (here X_{target}) is computed for every time step (i) of the target data $\delta^{15}N_{syn}$ according to:

$$D_{mc} D_X = \frac{1}{n} \sum_{i=1}^n |D_i| + \sum_{i=1}^n |D_{X,i}| = \frac{1}{n} \sum_{i=1}^n |X_{target,i} - X_{mod,i}| \quad (81)$$

D_{mc} (Note: If not otherwise stated, all mismatches in this study labelled with “D” are calculated similar to eq. (1))

$D_{\delta^{15}N_{mc}}$ serves as the criterion which is minimised during the optimization in step 2. If the mismatch $D_{\delta^{15}N_{mc,i}}$ decreases compared to the prior input $(T_{mc,i-1}, D_{\delta^{15}N_{mc,i-1}})$, the new input is saved and used as new guess $(T_{g,i} = T_{mc,i})$. This procedure is repeated until convergence is achieved.

leading to the final long-term temperature $T_{mc,fin}(t)$. Table 0402 lists the number of improvements and iterations performed for the different synthetic datasets.

The perturbation of the current guess $T_g(t) T_{g,i}$ is conducted in the following way: Let $\vec{T}_g = T_g \vec{T}_{g,0} = T_{g,0}(t)$ be the vector containing the prior temperature-input. A second vector \vec{P}_r with the same number of elements n_{mc} as \vec{T}_g is generated containing n_{mc} uniformly-distributed random numbers within the limits of an also randomly (equally-distributed) chosen standard deviation s . s is chosen from a range of 0.05-0.50 (Fig. S07H), which means that the maximum allowed perturbation of a single temperature value $T(t_0)$ is in a range of $\pm 5\%$ to $\pm 50\%$. Creating the synthetic frequencies, \vec{P}_r is low-pass filtered using cubic spline filtering-spline-filtering (Enting, 1987) with an equally distributed random eop (Fig. S07I) cut-off-period (COP) in the range of 500 yr to 2000 yr generating the vector \vec{P}_1 . Hereby the low-pass filtering of \vec{P}_r reduces the amplitudes of the perturbation of $\vec{T}_{g,0}$. The new surface temperature input $\vec{T}_{sm} T_{mc,1}$ is calculated from \vec{P}_1 according to:

$$\vec{T}_{sm} = \vec{T}_g^T \cdot (\hat{1} + \vec{P}) \quad (9)$$

$$\vec{T}_{mc,1} = \vec{T}_{g,0}^T \cdot (\hat{1} + \vec{P}_1) \quad (2)$$

The superscript “T” stands for transposed and $\hat{1}$ is the n by 1 matrix of ones.

This approach provides a high potential for parallel computing. In this study, an eight-core computer was used, generating and running eight different inputs of $\vec{T}_{sm}^T \cdot \vec{T}_{mc}$ simultaneously, minimizing the time to find an improved solution. For example, during the 706 iterations for scenario S2, about 5600 different inputs were created and tested, leading to 351 improvements (see Tab. 01/ Table 02). Since it is possible to find more than one improvement per iteration step due to the parallelization on eight CPU's, the solution giving the minimal misfit $D_{\delta^{15}N_{mc,i}}$ is chosen as new first-guess for the next iteration step. This leads to a decrease of the used improvements for the optimization (e.g. for S2, 172 of the 351 improvements were used). Additionally, a first gas-age scale ($\Delta age_{mc,fin}(t)$) is extracted from the model using the last improved conditions, which will then be used in step 3.

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2. Step 3.3: Adding short-term (high frequency) information (step 3)

In step 3 the missing high-frequency short-term temperature history providing a suitable fit between modelled and synthetic $\delta^{15}N$ data is directly extracted from the pointwise mismatch $D_{smooth,i} = D_{\delta^{15}N_{mc,fin,i}}$ between the modelled $\delta^{15}N_{smooth} = \delta^{15}N_{mc,fin}(t)$ obtained in step 2 and the synthetic $\delta^{15}N_{syn}$ target-data. Note that for a real reconstruction, this mismatch is calculated using the measured $\delta^{15}N_{meas}$ dataset instead of the synthetic one. $D_{smooth,i} = D_{\delta^{15}N_{mc,fin,i}}$ can be interpreted in first order as the detrended high-frequency signal of the synthetic $\delta^{15}N_{syn}$ target-values (Fig. 01e). This signal $D_{\delta^{15}N_{mc,fin,i}}$ is transferred to the gas-age scale using $\Delta age_{mc,fin}(t)$ provided by the firm-model output for the smooth temperature input $T_{mc,fin}(t)$. This is needed to insure synchronicity in-between the high-frequency temperature variations $\Delta T(t)$ extracted from the mismatch of $\delta^{15}N_{smooth} = \delta^{15}N_{mc,fin}(t)$ on the ice-age scale and the smooth temperature solution $T_{mc,fin}(t)$. Additionally, the signal is shifted by about 10 yr towards modern values to account for gas diffusion from the surface to the LID lock-in-depth (Schwander et al., 1993) (Schwander et al., 1993), which is not yet implemented in the firm model. This is necessary for adding the calculated short-term temperature changes $\Delta T(t)$ to the smooth signal $T_{mc,fin}(t)$. The ΔT values are calculated according to Eq. (10eq. (3)):

$$\Delta T_i = \frac{D_{smooth,i} \cdot D_{\delta^{15}N_{mc,fin,i}}}{\Omega_{N_2,i} \cdot \Omega_{N_2,i}}, \quad (10(3))$$

using the thermal diffusion sensitivity $\Omega_{N_2,i}$ for nitrogen-isotope fractionation from Grachev and Severinghaus (2003); using the thermal-diffusion sensitivity $\Omega_{N_2,i}$ for nitrogen-isotope fractionation from Grachev and Severinghaus (2003):

$$\Omega_{N_2,i} = \frac{8.656 \text{‰} \cdot 1232 \text{‰} \cdot K}{\bar{T}_i^2} - \frac{8.656 \text{‰} \cdot 1232 \text{‰} \cdot K}{\bar{T}_i^2} \quad (11) \quad (4)$$

$\bar{T}_i - \bar{T}_i$ is the mean firm temperature in Kelvin which is calculated by the firm model for each time point i. To reconstruct the final (high frequency) temperature input $T_{hr,i}(t)$, the extracted short-term temperature signal $\Delta T(t)$ is simply added to the smooth long-term temperature input $T_{sm} = T_{mc,fin}(t)$:

$$T_{\text{hfi}} = T_{\text{sm},\text{T}} T_{\text{mc,fin},i} + \Delta T_i \quad (125)$$

2.3. Step 4: Final correction of the surface temperature solution (step 4)

For a further improvement of the remaining $\delta^{15}\text{N}$ and resulting surface-temperature misfits ($D_{\delta^{15}\text{N,hf}}(t)$, $D_{T,\text{hf}}(t)$), it is important to find a correction method that contains information that is also available when using measured data. The benefit of the synthetic data study is that several later unknown quantities can be calculated, and used for improving the reconstruction approach (see Sect. 3 and 4). For instance, it is possible to split the synthetic $\delta^{15}\text{N}_{\text{syn}}$ data in the gravitational and thermo-diffusion parts or to use the temperature misfit, which is unknown in reality. The idea underlying the correction algorithm explained hereafter is that the remaining misfits of $\delta^{15}\text{N}$ ($D_{\delta^{15}\text{N,hf}}(t)$) and temperature ($D_{T,\text{hf}}(t)$) are connected to the Monte-Carlo (step 2) and high-frequency part (step 3) of the reconstruction algorithm. In the present inversion framework, it is not possible to find a smooth long-term solution $\delta^{15}\text{N}_{\text{mc,fin}}$ (or $T_{\text{mc,fin}}$) which exactly passes through the $\delta^{15}\text{N}_{\text{syn}}$ (or T_{syn}) target data in the middle of the variance in all parts of the time-series. This leads to a slightly over- or underestimation of the $\delta^{15}\text{N}_{\text{mc,fin}}$ and their corresponding temperature values $T_{\text{mc,fin}}$. For example, a slightly too low (or too high) smooth temperature estimate $T_{\text{mc,fin}}$ leads to a small increase (or decrease) of the firm-column-height, creating a wrong gravitational background signal in $\delta^{15}\text{N}_{\text{mc,fin}}$ on a later point in time (because the firm column needs some time to react). An additional error in the thermal-diffusion signal is also created due to the high-frequency part of the reconstruction (step 3), because the high-frequency information is directly extracted from the deviation of the (synthetic) $\delta^{15}\text{N}$ target data $\delta^{15}\text{N}_{\text{syn}}(t)$ and the modelled $\delta^{15}\text{N}_{\text{mc,fin}}(t)$ from the smooth final long-term solution $T_{\text{mc,fin}}(t)$ of the Monte-Carlo part. Therefore, this error is transferred into the next step of the reconstruction and partly creates the remaining deviations.

To investigate this problem, the deviations $D_{\text{smooth},\delta^{15}\text{N,mc,fin}}(t)$ of the synthetic target data $\delta^{15}\text{N}_{\text{target}}$ to the smooth data $\delta^{15}\text{N}_{\text{smooth}}$ of the Monte-Carlo part are numerically integrated over a time window of 200 yr (see Sect. 4, Supple. S3), and thereafter the window is shifted from past to future in 1 yr steps resulting in a time-series called IF(t). IF(t) equals a 200 yr running-mean of $D_{\text{smooth},\delta^{15}\text{N,mc,fin}}(t)$. For t, the mid position of the window is allocated. The time evolution of IF(t) is a measure for the deviation of the smooth long-term solution in $\delta^{15}\text{N}_{\text{mc,fin}}(t)$ (or temperature) $T_{\text{mc,fin}}(t)$ from the perfect middle passage through the target data $\delta^{15}\text{N}_{\text{syn}}(t)$ (or $T_{\text{syn}}(t)$) and for the slightly over- and underestimation of the resulting temperature.

$$\text{IF}(t_i) = \int_{t_i}^{t_i+200} (\delta^{15}\text{N}_{\text{target}}(t) - \delta^{15}\text{N}_{\text{smooth}}(t)) dt \quad (13)$$

$$\text{where } t_i = t_1 + \frac{t_2 - t_1}{2} \quad (14)$$

$$\text{IF}(t) = \frac{1}{200} \int_{t-100}^{t+100} (\delta^{15}\text{N}_{\text{syn}}(t) - \delta^{15}\text{N}_{\text{mc,fin}}(t)) dt = \frac{1}{200} \int_{t-100}^{t+100} D_{\delta^{15}\text{N,mc,fin}}(t) dt \quad (6)$$

Next, the sample-cross-correlation-function (xcf) (Box et al., 1994) (Box et al., 1994) is applied to IF(t) and the remaining misfits $D_{\delta^{15}\text{N,hf}}(t)$ of $\delta^{15}\text{N}$ after the high-frequency part. The xcf shows two extrema (Fig. 023a), a maximum (xcf_{max}) and a minimum (xcf_{min}) at two certain lags ($\text{lag}_{\text{max},\delta^{15}\text{N}}$ at $\text{xcf}_{\text{max},\delta^{15}\text{N}}$ and $\text{lag}_{\text{min},\delta^{15}\text{N}}$ at $\text{xcf}_{\text{min},\delta^{15}\text{N}}$). Now, the same analysis is conducted for IF(t) versus the temperature mismatch $D_{T,\text{hf}}(t)$ (Fig. 023b), which shows an equal behaviour (two extrema,

lag_{max,T} at xcf_{max,T} and lag_{min,T} at xcf_{min,T}). Comparing the two cross correlations shows that lag_{max,δ¹⁵N} equals the negative lag_{min,T} and lag_{min,δ¹⁵N} corresponds to the negative lag_{max,T} (Fig. 023d,e). The idea for the correction is that the extrema in the cross-correlation IF(t) vs. D_{δ¹⁵N,hf}(t) with the positive lag (positive means here that D_{δ¹⁵N,hf}(t) has to be shifted to past values relative to IF(t)) creates the misfit of temperature D_{T,hf}(t) on the negative lag (modern direction) of IF(t) vs. D_{T,hf}(t) and vice versa. So IF(t) yields information about the cause and allows us to correct this effect between the remaining mismatches of δ¹⁵N_{δ¹⁵N,hf}(t) and temperature D_{T,hf}(t) over the whole time-series. The lags are not sharp signals, due to the fact that (i) the cross-correlations are conducted over the whole analysed record, leading to an averaging of this cause and effect relationship as well as that (ii) IF(t) is a smoothed quantity itself. The correction of the reconstructed temperature after the high-frequency part is conducted in the following way: From the two linear relationships between IF(t) and D_{δ¹⁵N,hf}(t) at the two lags (lag_{max,δ¹⁵N} at xcf_{max,δ¹⁵N}, lag_{min,δ¹⁵N} at xcf_{min,δ¹⁵N}) two sets of δ¹⁵N correction values (Δδ¹⁵N_{max}(t) from xcf_{max,δ¹⁵N} and Δδ¹⁵N_{min}(t) from xcf_{min,δ¹⁵N}) are calculated. Then the lags are being inverted (Fig. 023c,e) shifting the two sets of the δ¹⁵N correction values to the attributed lags of the cross correlation between IF(t) and D_{T,hf}(t) (e.g. Δδ¹⁵N_{min}(t) to lag from xcf_{max,T} from the cross correlation between IF(t) and D_{T,hf}(t)) therefore changing the time assignments of Δδ¹⁵N_{min}(t) and Δδ¹⁵N_{max}(t) to Δδ¹⁵N_{min}(t+lag_{max,T}) and Δδ¹⁵N_{max}(t+lag_{min,T}). Now, the Δδ¹⁵N_{max}(t) and Δδ¹⁵N_{min}(t) are component-wise summed up leading to the time-series Δδ¹⁵N_{cv}(t). From Eq. (10) eq. (3) with Δδ¹⁵N_{cv,i} instead of D_{smooth,δ¹⁵N,mc,fin,i} the corresponding temperature correction values are calculated and added to the high-frequency temperature solution T_{hf}(t) giving the corrected temperature T_{corr}(t). Finally, T_{corr}(t) is used to run the firm model to calculate the corrected δ¹⁵N_{corr}(t) time-series (Fig. 03). This cause and effect relationship found in the cross-correlations between IF(t) and D_{δ¹⁵N,hf}(t) and IF(t) and D_{T,hf}(t) is exemplarily shown in Fig. 0203 for scenario S1 and was found for all eight synthetic scenarios. The derived correction algorithm leads to a further reduction of the mismatches of about 40 % in δ¹⁵N and temperature (see Sect. 3.2).

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2.2 Firm densification and heat diffusion model

Surface-temperature reconstruction relies on firm densification combined with gas- and heat-diffusion (Severinghaus et al., 1998). In this study, the firm-densification and heat-diffusion model, developed by Schwander et al. (1997) is used to reconstruct firm parameters for calculating synthetic δ¹⁵N values depending on the input time-series. It is a semi-empirical model based on the work of Herron and Langway (1980), Barnola et al. (1991), and implemented using the Crank and Nicholson algorithm (Crank, 1975) and was also used for the temperature reconstructions by Huber et al. (2006) and Kindler et al. (2014). Besides surface-temperature time-series, accurate accumulation-rate data are needed to run the model. The model then calculates the densification and heat-diffusion history of the firm layer and provides parameters for calculating the fractionation of the nitrogen isotopes for each time step, according to the following equations:

$$\delta^{15}\text{N}_{\text{grav}}(z_{\text{LID}}, t) = \left(e^{\frac{\Delta m \cdot g \cdot z_{\text{LID}}(t)}{R \cdot T(t)}} - 1 \right) \cdot 1000 \quad (7)$$

$$\delta^{15}\text{N}_{\text{therm}}(t) = \left[\left(\frac{T_{\text{surf}}(t)}{T_{\text{bottom}}(t)} \right)^{\alpha_T} - 1 \right] \cdot 1000 \quad (8)$$

$$\delta^{15}\text{N}_{\text{mod}}(t) = \delta^{15}\text{N}_{\text{grav}}(t) + \delta^{15}\text{N}_{\text{therm}}(t) \quad (9)$$

$\delta^{15}\text{N}_{\text{grav}}(t)$ is the component of the isotopic fractionation due to the gravitational settling (Craig et al., 1988; Schwander, 1989) and depends on the lock-in-depth (LID) $z_{\text{LID}}(t)$ and the mean firn temperature $\bar{T}(t)$ (Leuenberger et al., 1999). g is the gravitational acceleration, Δm the molar mass-difference between the heavy and light isotopes (equals 10^{-3} kg per mol for nitrogen) and R the ideal gas-constant. z_{LID} is defined as a density threshold ρ_{LID} , which is slightly sensitive to surface temperature, following the formula from Martinerie et al. (1994), with a small offset correction of 14 kg m^{-3} to account for the presence of a non-diffusive zone (Schwander et al., 1997):

$$\rho_{\text{LID}}(\text{kg} \cdot \text{m}^{-3}) = \frac{1}{\frac{1}{\rho_{\text{ice}}} - 6.95 \cdot 10^{-7} \cdot \bar{T} - 4.3 \cdot 10^{-5}} - 14 \quad (10)$$

where

$$\rho_{\text{ice}}(\text{kg} \cdot \text{m}^{-3}) = 916.5 - 0.14438 \cdot \bar{T} - 1.5175 \cdot 10^{-4} \cdot \bar{T}^2 \quad (11)$$

The thermal-fractionation component of the $\delta^{15}\text{N}$ signal (Severinghaus et al., 1998) is calculated using eq. (8), where $T_{\text{surf}}(t)$ and $T_{\text{bottom}}(t)$ stand for the temperatures at the top and the bottom of the diffusive firn-layer. In contrast to $T_{\text{surf}}(t)$ which is an input parameter for the model, $T_{\text{bottom}}(t)$ is calculated by the model for each time step. The thermal-diffusion constant α_T was measured by Grachev and Severinghaus (2003) for nitrogen (eq. (12)):

$$\alpha_T = \left(8.656 - \frac{1323 \text{ K}}{\bar{T}} \right) \cdot 10^{-3} \quad (12)$$

The firn model used here behaves purely as a forward model, which means that for the given input time-series the output parameters (here finally $\delta^{15}\text{N}_{\text{mod}}(t)$) can be calculated, but it is not easily possible to construct from measured isotope data the related surface-temperature or accumulation-rate histories. The goal of the presented study is an automatization of this inverse-modelling procedure for the reconstruction of the rather small Holocene temperature variations.

2.3 Measurement, input data and time scale

Time scale

For the entire study the GICC05 chronology is used (Rasmussen et al., 2014; Seierstad et al., 2014). During the whole reconstruction procedure the two input time-series (surface temperature and accumulation rate) are split into two parts. The first part ranges from 20 yr to 10520 yr b2k (called ‘‘Holocene section’’) and the second one from 10520 yr to 35000 yr b2k (‘‘spin-up section’’). The entire accumulation-rate input, as well as the spin-up section of the surface-temperature input remains unchanged during the reconstruction procedure.

Accumulation-rate data

Besides surface temperatures, accumulation-rate data are needed to drive the firn model. In this study we use the original accumulation rates, reconstructed in Cuffey and Clow (1997) produced using an ice-flow model adapted to the GISP2

location, but adapted to the GICC05 chronology (Rasmussen et al., 2008; Seierstad et al., 2014). A detailed description of the adaption procedure can be found in supplement S1. The raw accumulation-rate data for the main part of the spin-up section (12000 yr to 35000 yr b2k) are linearly interpolated to a 20 yr grid and low-pass filtered with a 200 yr cut-off-period (COP) using cubic-spline-filtering (Enting, 1987). For the Holocene section (20-10520 yr b2k) and the transition part between Holocene and spin-up section (10520 yr to 12000 yr b2k) the raw accumulation-rate data are linearly interpolated to a 1 yr grid to obtain equidistant integer point-to-point distances which are necessary for the reconstruction, and to preserve as much information as possible for this time period (Fig. 02a). Except for these technical adjustments, the accumulation-rate input remains unmodified, assuming high reliability of these data during the Holocene. The accumulation data were reconstructed using annual-layer-counting, and a thinning model which should lead to maximum relative uncertainty of 10 % for the first 1500 m of the 3000 m ice core (Cuffey and Clow, 1997). From the three accumulation-rate scenarios reconstructed in Cuffey and Clow (1997) and adapted here to the GICC05 chronology, the intermediate one is chosen (red curves in Fig. S01). Since the differences between the scenarios are not important for the evaluation of the reconstruction approach, they are not taken into account for this study.

Additionally, two sensitivity experiments were conducted (see supplement S2) in order to investigate (i) the influence of low-pass-filtering of the high-resolution accumulation rates on the model outputs and (ii) the possible contribution of the accumulation-rate variability on the $\delta^{15}\text{N}$ data during the Holocene. The first experiment shows that filtering the accumulation-rates with cut-off-periods in the range of 20 yr to 500 yr has nearly no influence on the modelled $\delta^{15}\text{N}$ or lock-in-depth as long as the major trends are being conserved. The second experiment leads to the finding that the accumulation-rate variability explains about 12 % to 30 % of $\delta^{15}\text{N}$ variability. 30 % corresponds to the 8.2 kyr event and 12 % for the mean of the whole Holocene period including the 8.2 kyr event. Hence the influence of accumulation changes, excluding the extreme 8.2 kyr event, is generally below 10 % during most parts of the Holocene.

$\delta^{18}\text{O}_{\text{ice}}$ data

Oxygen-isotope data from the GISP2 ice-core-water samples measured at the University of Washington's Quaternary Isotope Laboratory are used to construct the surface-temperature input of the model spin-up (12 yr to 35 kyr b2k; Grootes et al., 1993; Meese et al., 1994; Steig et al., 1994; Stuiver et al., 1995; Grootes and Stuiver, 1997). The raw $\delta^{18}\text{O}_{\text{ice}}$ data are filtered and interpolated in the same way as the accumulation-rate data for the spin-up part.

Surface-temperature spin-up

The surface-temperature history of the spin-up section (Fig. 02a) is obtained by calibrating the filtered and interpolated $\delta^{18}\text{O}_{\text{ice}}$ data (eq. (13)) using the values for the temperature sensitivity $\alpha_{18\text{O}}$ and offset β found by Kindler et al. (2014) for the NGRIP ice core assuming a linear relationship of $\delta^{18}\text{O}_{\text{ice}}$ with temperature.

$$T_{\text{spin}}(t) = \frac{1}{\alpha_{18\text{O}}(t)} \cdot [\delta^{18}\text{O}_{\text{ice}}(t) + 35.2 \text{‰}] - 31.4^\circ\text{C} + \beta(t) \quad (13)$$

The values 35.2 ‰ and -31.4 °C are modern-time parameters for the GISP2 site (Schwander et al., 1997; Grootes and Stuiver, 1997). The spin-up is needed to bring the firm model to a well-defined starting condition that takes possible memory effects (influence of earlier conditions) of firm states into account.

5 Generating synthetic target data

In order to develop and evaluate the presented algorithm, eight temperature scenarios were constructed and used to model synthetic $\delta^{15}\text{N}$ data, which serve later as targets for the reconstruction. From these eight synthetic surface-temperature and related $\delta^{15}\text{N}$ scenarios (S1-S5 and H1-H3), three data sets (later called Holocene like scenarios H1-H3) were constructed in such a way that the resulting $\delta^{15}\text{N}$ time-series are very close to the $\delta^{15}\text{N}$ values measured by Kobashi et al. (2008b) in terms of variability (amplitudes) and frequency (data resolution) of the GISP2 nitrogen-isotope data (Fig. 04, Fig. 05).

The synthetic surface-temperature scenarios S1-S5 are created by generating a long-term temperature time-series ($T_{\text{syn,smooth}}$) analogous to the Monte-Carlo part of the reconstruction procedure for only one iteration step (see Sect. 2.1). The values for the cut-off-period used for the filtering of the random values, and the s values (standard deviation of the random values, see Sect. 2.1) for the first five scenarios can be found in Table 03. The long-term temperatures (Fig. 04I) are calculated on a 20 yr grid, which is nearly similar to the time resolution of the GISP2 $\delta^{15}\text{N}$ measurement values of about 17 yr (Kobashi et al., 2008b). For the Holocene-like scenarios, the smooth temperature time-series were generated from the temperature reconstruction for the GISP2 $\delta^{15}\text{N}$ data (not shown here). The final Holocene surface-temperature solution was filtered with a 100 yr cut-off to obtain the long-term temperature scenario.

Following this, high frequency information is added to the long-term temperature histories. A set of normally-distributed random numbers with a zero mean and a standard deviation (1σ) of 1 K for scenarios S1-S5 and 0.3 K for Holocene-like scenarios H1-H3 is generated on the same 20 yr grid and added up to the long-term temperature time-series. Finally, the resulting synthetic target-temperature-scenarios (Fig. 04II, Fig. 05I) are linearly interpolated to a 1 yr grid.

These synthetic temperatures are combined with the spin-up temperature and are used together with the accumulation-rate input to feed the firm model. From the model output the synthetic $\delta^{15}\text{N}$ targets are calculated according to section 2.1. The firm-model output provides ice-age as well as gas-age information. The final synthetic $\delta^{15}\text{N}$ target time-series ($\delta^{15}\text{N}_{\text{syn}}$) are set intentionally on the ice-age scale to mirror measured data, because no prior information is available for the gas-ice-age difference (Δage) for ice-core data.

3. Results

3.1 Monte Carlo type input generator

Figure S0806 shows the evolution of the mean-misfit D_{mean} of $\delta^{15}\text{N}$ from $D_{\delta^{15}\text{N}_{\text{mc},j}}$ between the synthetic target data ($\delta^{15}\text{N}_{\text{syn}}$) versus the modelled data-output $\delta^{15}\text{N}_{\text{mc},j}$ of the Monte-Carlo part (step 2) as a function of the applied iterations (j) for all synthetic scenarios. One can easily see that all scenarios show a steep decline of the mismatch during the first 50 to 200

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iterations followed by a rather moderate decrease, which finally leads to a constant value. During the Monte-Carlo part, it was possible to reduce the misfit of $\delta^{15}\text{N}_{\text{mc}}$ compared to the first-guess solution $D_{\delta^{15}\text{N},g,0}$ by about 15 % to 75 % depending on the scenario and the mismatch of the first-guess solution (see [Tab. 04 Table 02](#)). This leads to a reduction of the temperature mismatches $D_{T,\text{mc}}$ compared to the first-guess temperature $D_{T,g,0}$ mismatch of about 51 % to 87 %.

Figure 0407 provides the comparison between the first-guess ([g.0; step 1](#)) and Monte-Carlo ([mc.fin; step 2](#)) solution versus the synthetic target data ([syn](#)) for the modelled $\delta^{15}\text{N}$ (a-c) and surface-temperature values (d-f) for scenario S5. Subplots (a) and (d) show the time-series of the synthetic target data (black dotted line), the first-guess solution (blue line) and the Monte-Carlo solution (red line) for $\delta^{15}\text{N}$ and temperature. In subplots (b) and (e), the distribution of the pointwise mismatch D_i of the first-guess (blue) and the Monte-Carlo solution (red) versus the synthetic target data for $\delta^{15}\text{N}$ ($D_{\delta^{15}\text{N}}$) and temperature (D_T) can be found. Subplots (c) and (f) contain the time-series for D_i for $\delta^{15}\text{N}_{\text{mc},i}$ and temperature $D_{T,i}$. The D_i for $\delta^{15}\text{N}_{\text{mc},i}$ data is (red) are used later on to calculate the high-frequency signal, that is superimposed to the smooth long-term temperature solution $T_{\text{mc},\text{fin}}$ according to [Eq. \(4\) Eq. \(3\)](#) and [Eq. \(2\) Eq. \(5\)](#) (see [Sect. 2.3-1, step 3](#)). From [Fig. 0407](#) it can be concluded that the Monte-Carlo part of the reconstruction algorithm (step 2) leads to two major improvements of the first-guess solution. First, it is obvious that the Monte-Carlo approach corrects the offsets of the first-guess input, ([g.0](#)), which shifts the midpoint of the distributions of $D_{\text{mc},\delta^{15}\text{N},i}$ and $D_{T,\text{mc},i}$ to zero (see [blue against red in Fig. 047b,e](#)). The second improvement is that the ~~distribution becomes~~ distributions become more symmetric and the misfit is overall reduced (the distributions become narrower) compared to the first-guess, due to the middle passage through the $\delta^{15}\text{N}_{\text{syn}}$ targets. These improvements can be observed for all eight synthetic scenarios, showing the robustness of the Monte-Carlo part (see [Tab. 04 Table 02](#), [Fig. 0407](#)).

3.2 High frequency step and final correction

Figure 0308 provides the comparison between the Monte-Carlo ([mc.fin; step 2](#)), the high-frequency ([hf; step 3](#)) and the correction ([corr; step 4](#)) parts of the reconstruction procedure for the scenarios S5. Additional data for all other scenarios can be found in [table 02 Table 04](#). The upper four plots (a-d) illustrate each reconstruction step and their effect on the modelled $\delta^{15}\text{N}$; the bottom four plots (e-h) show the corresponding results on the temperature. Plots (a) and (e) contain the time-series of the synthetic $\delta^{15}\text{N}_{\text{syn}}$ or temperature T_{syn} target ([syn](#); black dotted line), the high-frequency solution ([hf](#); blue line), and the final solution after the correction part ([corr](#); red line). For visibility reasons, subplots (b) and (f) display a zoom-in for a randomly chosen time-window of about 500 yr for the same quantities, which shows the excellent agreement in timing and amplitudes of the modelled $\delta^{15}\text{N}$ and temperature compared to the synthetic target data. Histograms (c) and (g) and subplots (d) and (h) show the distribution and the time-series of the pointwise mismatches (D_i , $D_{\delta^{15}\text{N},i}$ for $\delta^{15}\text{N}$, ΔT_i , $D_{T,i}$ for temperature) between the modelled and the synthetic target data in $\delta^{15}\text{N}$ and temperature for each reconstruction step.

Compared to the Monte-Carlo solution, the high-frequency part leads to a large refinement of the reconstructions. For the mean $\delta^{15}\text{N}$ misfits $D_{\delta^{15}\text{N}}$, the improvement between the Monte-Carlo and the high-frequency parts is in the range of 64 % to 76 % (see [Tab. 02 Table 04](#)). This leads to a reduction of the temperature mismatches D_T of 43 % to 67 %. The standard

deviations (1σ) of the pointwise mismatches (Fig. 0308c,d,g,h) in $\delta^{15}\text{N}$ and temperature after the high-frequency parts are in the range of about 2.7 permeg to 5.4 permeg (one permeg equals 10^{-6}) for $\delta^{15}\text{N}$ and 0.22 K to 0.40 K for the reconstructed temperatures depending on the scenario, which is clearly visible in the decreasing width of the histograms (subplots (c) and (g) of Fig. 0308, blue against grey).

5 The mismatches after the correction part of the reconstruction approach show clearly a further decrease of the misfits. This means that the width of the distributions of the pointwise mismatches of $\delta^{15}\text{N}$ ($D_{\delta^{15}\text{N},i}$) as well as of temperature ($D_{T,i}$) is further reduced, and the distributions become more symmetric (long tails disappear; see histogram (c) and (g); red against blue of Fig. 0308). The time series of the mismatches (subplots (d) and (h) of Fig. 0308) clearly illustrate that the correction approach mainly tackles the extreme deviations (sharp reduction of extreme values occurrence in the red distribution compared to the blue distribution) leading to a further improvement of about 40 % in $\delta^{15}\text{N}$ and temperature. Finally, the 10 95 % quantiles ($2\sigma_{\delta^{15}\text{N},\text{corr},95}$, $2\sigma_{T,\text{corr},95}$) of the remaining pointwise mismatches of $\delta^{15}\text{N}$ and temperature ($D_{\delta^{15}\text{N},i}$ or $A_{T,i}$) were calculated for the final solutions for all scenarios and are used as an estimate for the 2σ uncertainty of the reconstruction algorithm (see Fig. 0308c,g and Tab. 2Table 04). The final uncertainties (2σ) are in the order of 3.0 permeg to 6.3 permeg for $\delta^{15}\text{N}$ and 0.23 K to 0.51 K for the surface temperature misfits. It is noteworthy that the measurement 15 uncertainties (per point) of state of the art $\delta^{15}\text{N}$ measurements are in the same order of magnitude, i.e. 3 permeg to 5 permeg (Kobashi et al., 2008b)(Kobashi et al., 2008b), highlighting the effectiveness of the presented fitting approach. Table 0305 contains the final mismatches (2σ) in Δage between the synthetic target and the final modelled data after the correction step for all scenarios and shows that with a known accumulation rate and assumed perfect firn physics, it is possible to fit the Δage history in the Holocene with mean uncertainties better than 2 yr. In other words, the uncertainty in Δage reconstruction 20 due to the inversion algorithm alone is in the order of 2 yr.

4. Discussion

4.1 Monte Carlo type input generator

Figure S0709 shows the distribution of the eopcut-off-periods (COP) (I) and s values (II) used to create the improvements (Sect. 2.3-1, step 2) for all scenarios. The eop valuescut-off-periods are more or less evenly distributed, which shows that 25 nearly the whole of the allowed frequency range (allowed eops were 500 yr to 2000 yr) was used to create the improvements during the iterations. In contrast, the distributions of the s values show clearly that mostly small s values are used to create the improvements, which implies that iterations with small perturbations more likely lead to an improvement than larger ones.

Figure S0806 reveals a weak point of the Monte-Carlo part, namely the absence of a suitable termination criterion for the 30 optimization. The implementation until now is conducted such that the maximum number of iterations is given by the user or the iterations are terminated after a certain time (e.g. 15 h). Figure S0806 shows that for nearly all scenarios it would be possible to stop the optimization after about 400 iterations, due to rather small additional improvements later on. This would

decrease the time needed for the Monte-Carlo part to about 10 h (a single iteration needs about 90 s). Since the goal of the Monte-Carlo part is to find a temperature realisation that leads to an optimal middle passage through the $\delta^{15}\text{N}$ target data, it would be possible to use the mean difference between the $\delta^{15}\text{N}$ target and spline-filtered $\delta^{15}\text{N}$ data using a certain cut-off-period as a termination criterion. This issue is under investigation at the moment. Another possibility to decrease the time needed for the Monte-Carlo part could be an increase in the numbers of CPUs used for the parallelization of the model runs. For this study an eight-core parallelization was used. A further increase in numbers of workers would improve the speed of the optimization.

4.2 High frequency step and final correction

Several analyses were conducted in order to investigate the timing and contributions of the remaining mismatches in $\delta^{15}\text{N}$ and temperature for scenario S1 after the high-frequency (step 3) and the correction part (step 4), different cross-correlation experiments were conducted (see supplement S3). The experiments lead to equal results. The major fraction of the reconstruction respectively. First, final mismatches of $\delta^{15}\text{N}$ emerges from mismatches in the total misfit of $\delta^{15}\text{N}$ ($D_{\delta^{15}\text{Ntot}}$) was separated into two fractions: gravitational ($D_{\delta^{15}\text{Ngrav}}$) and thermal-diffusion mismatches (component $D_{\delta^{15}\text{Ntherm}}$) of $\delta^{15}\text{N}$ (Fig. 04). Figure 04 indicates that the main fraction, Also a cancelation effect between the gravitational component $D_{\delta^{15}\text{Ngrav}}$ and $D_{\delta^{15}\text{Ntherm}}$ of the total mismatch in $\delta^{15}\text{N}$ became obviously, affecting the calculation of $\text{lag}_{\text{max},\delta^{15}\text{N}}$ is due to the misfit of the thermal diffusion component of the $\delta^{15}\text{N}$ signal, whereas the gravitational misfit of $\delta^{15}\text{N}$ has only a minor contribution. The ratio of the standard deviations $\sigma(D_{\delta^{15}\text{Ntherm}})/\sigma(D_{\delta^{15}\text{Ngrav}})$ is about 2.4 for the high frequency solution, and about 2.3 and $\text{lag}_{\text{min},\delta^{15}\text{N}}$ and most likely leading to a fundamental residual uncertainty in the low-permeg level for the corrected signal, showing that the misfit in the thermal diffusion part is more than twice as high as in the gravitational component.

To investigate the timing and contributions of the mismatches in $\delta^{15}\text{N}$ and temperature for scenario S1, different xefs were calculated (Fig. S09a-d) $\delta^{15}\text{N}$ data. The same analyses were conducted for all synthetic scenarios, leading to similar results. In Fig. S09a the xef between the mismatch of total $\delta^{15}\text{N}$ ($D_{\delta^{15}\text{Ntot,hf}}$) and the misfit of temperature ($D_{T,hf}$) is shown. The cross correlation leads to two extrema ($r_{1a}=0.70$, $r_{2a}=-0.55$) on two certain lags ($l_{1a}=-2$ yr, $l_{2a}=+126$ yr). In subplot (b) and (c) the same analysis is conducted between the mismatch of the gravitational ($D_{\delta^{15}\text{Ngrav,hf}}$) component (b), and the thermal diffusion ($D_{\delta^{15}\text{Ntherm,hf}}$) component (c) of $\delta^{15}\text{N}$ and the temperature mismatch. It is obvious that the xef of (a) is a combination of (b) and (c). The direct correlation on l_{1a} of (a) can be attributed mainly to the mismatch of the thermal diffusion component of $\delta^{15}\text{N}$, whereas the negative correlation on l_{2a} is due to the mismatch of the gravitational component of $\delta^{15}\text{N}$. Regarding the xefs of (a) (c) at a certain lag l , i.e. $l=0$ yr shows that here (and on most of the other lags) the correlations between $D_{\delta^{15}\text{Ngrav,hf}}$ with $D_{T,hf}$ and $D_{\delta^{15}\text{Ntherm,hf}}$ with $D_{T,hf}$ work in opposite directions, which makes it difficult to find a way to correct the remaining temperature mismatch using only information from $D_{\delta^{15}\text{Ntot,hf}}$ for measurement data (when only $D_{\delta^{15}\text{Ntot,hf}}$ is available). The correlation on l_{1a} in (a) is weakened, whereas the lag l_{2a} is shifted to higher values because of the superposition of gravitational and thermal diffusion mismatch. Figure S09d shows also that the gravitational and thermal diffusion mismatches of $\delta^{15}\text{N}$ are not independent, but the correlations at the extrema are relatively weak ($r_{1a}=0.38$,

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$r_{2,d} = -0.56$). The negative correlation $r_{2,d}$ is a sign for the compensation effect between the gravitational and thermal diffusion signals in $\delta^{15}\text{N}$ due to the high frequency part of the reconstruction, whereas no explanation could be found for the positive correlation $r_{1,d}$. The symmetric behaviour of the lags for $r_{1,d}$ and $r_{2,d}$ ($l_{1,d} = -88 \text{ yr} \approx -l_{2,d} = 93 \text{ yr}$) suggest that $r_{1,d}$ could be an artefact of a periodic behaviour of $D_{\delta^{15}\text{N}_{\text{grav},\text{hr}}}$ and $D_{\delta^{15}\text{N}_{\text{therm},\text{hr}}}$. Figures S10a-d show the same analysis after the correction part of the reconstruction. It is evident that in all cases the extrema in the different xefs break down due to the correction of the temperature signal, which is the consequence of the decreasing mismatches of temperature as well as of $\delta^{15}\text{N}$. The comparison of the subplots (a), (b) and (c) also shows that the remaining temperature misfits after the correction are mainly driven by the mismatches of the thermal diffusion signal of $\delta^{15}\text{N}$ with a minor contribution of the gravitational misfit.

Figures S09e-h show the cross correlations between IF(t) used for the correction of the high frequency temperature solution, and the temperature misfit (e), the mismatch of total $\delta^{15}\text{N}$ (f), the mismatch of the gravitational (g) and thermal diffusion (h) component of the $\delta^{15}\text{N}$ signal calculated from the high frequency temperature solution. For the correction, the cross correlations (e) and (f) were used (see Sect. 2.3.4 and Fig. 02). Since for measured data neither information about the temperature mismatch (the true temperature is not known) nor about the mismatch of the components of $\delta^{15}\text{N}$ (gravitational, thermal diffusion) are available, it is imperative that the symmetric behaviour between the xef(IF(t), $D_{T,\text{hr}}(t)$) and inverted xef(IF(t), $D_{\delta^{15}\text{N}_{\text{tot},\text{hr}}}(t)$) holds true. This criterion is fulfilled for all eight synthetic data scenarios and especially for H1-H3. The comparison of the subplots (f), (g) and (h) of Fig. S09 show the same findings as before, namely that the xef for IF versus $D_{\delta^{15}\text{N}_{\text{tot},\text{hr}}}$ is the combination of the xefs of IF(t) versus $D_{\delta^{15}\text{N}_{\text{grav},\text{hr}}}$ and IF(t) versus $D_{\delta^{15}\text{N}_{\text{therm},\text{hr}}}$ and that the major fraction of $D_{\delta^{15}\text{N}_{\text{tot},\text{hr}}}$ is contributed from $D_{\delta^{15}\text{N}_{\text{therm},\text{hr}}}$. The advantage to use IF(t) for the correction is the symmetry between the two cross correlations, which is created by two factors. The first one is the allocation of the window mid position to the entries of IF, which leads to the symmetric behaviour of the gravitational and thermal diffusion misfits. Second, the shifting of the window in 1 yr steps creating IF(t) over the whole data set leads to an averaged information, but even more importantly, to constant dependency between the temperature and $\delta^{15}\text{N}$ mismatches. This can be used later on to fit measured data.

Additionally, the influence of the window length, used for the construction calculation of IF(t), on the correction was analysed. The construction was conducted for different window lengths ranging from 50 yr to 750 yr (Fig. S11). Also, the correction was calculated by using only xef_{max} or xef_{min} of IF(t) versus $D_{\delta^{15}\text{N},\text{hr}}$ for correcting the temperature input. Figures S11a,b show the remaining mismatches of $\delta^{15}\text{N}$ ($D_{\delta^{15}\text{N},\text{corr}}$) (a), and temperature ($D_{T,\text{corr}}$) (b) after the correction as a function of the used window length for IF(t). The analysis shows, showing that for all investigated window lengths the correction reduces the mismatches of $\delta^{15}\text{N}$ and temperature, whatever correction mode was used (calculated with xef_{max} , xef_{min} , or both quantities, see comparison with the blue line in (a) and (b)). Furthermore, Moreover, the correction works best is most efficient for window lengths in the range of 100 yr to 300 yr with an optimum at 200 yr for all cases. This indicates that the maximum mean duration effect of a $\delta^{15}\text{N}$ mismatch creating a temperature mismatch (and vice versa) is in the same range for the investigated scenarios and such small deviations (low permeg level). It is also visible that the correction using both extrema (xef_{max} and xef_{min}) leads to a better correction as the approach using only one quantity. This is

5 somehow surprising because the two extrema are the result of the periodicity of $IF(t)$, $D_{\delta^{15}N, hf}$ and $D_{T, hf}$. An explanation for this result could be that a larger section of the temperature time series is corrected when both extrema are used for the correction, due to shifts in both directions. The correction using $x_{cf, max}$ only leads to a better fit than the one with $x_{cf, min}$, which can be attributed to the higher correlation between $IF(t)$ and $D_{\delta^{15}N, hf}$. Figures S11e,f show the evolution of the lags corresponding to the two extrema for the cross correlations between $IF(t)$, and the $\delta^{15}N$ and temperature mismatches, respectively. The linear dependency between the lags and the window length (the lags are nearly half of the window length) is the result of the construction of $IF(t)$, which means the averaging due to the integration in the window of this certain length and the symmetric behaviour due to the allocation of the window mid position to the entries of $IF(t)$.

4.3 Key points to be considered for the application to real data

Benefits of the novel gas isotope fitting approach

10 In addition to the fitting of $\delta^{15}N$ data, the algorithm is able to fit $\delta^{40}Ar$ and $\delta^{15}N_{excess}$ data as well using the same basic concepts (Fig. S12). Here the $\delta^{40}Ar$ and $\delta^{15}N_{excess}$ data from Kobashi et al. (2008) were used as the fitting targets using the same approach. We reach final mismatches (2σ) of 4.0 permeg for $\delta^{40}Ar/4$ and 3.7 permeg for $\delta^{15}N_{excess}$, which are for both quantities below the analytical measurement uncertainty of 4.0 permeg to 9.0 permeg for $\delta^{40}Ar/4$ and 5.0 permeg to 9.8 permeg for $\delta^{15}N_{excess}$ measured data (Kobashi et al., 2008).

The automated inversion of different gas 4.3 Key points to be considered for the application to real data

Benefits of the novel gas isotope fitting approach

20 In addition to the fitting of $\delta^{15}N$ data, the algorithm is able to fit $\delta^{40}Ar$ and $\delta^{15}N_{excess}$ data as well using the same basic concepts (Fig. 10). Here the $\delta^{40}Ar$ and $\delta^{15}N_{excess}$ data from Kobashi et al. (2008b) were used as the fitting targets. We reach final mismatches (2σ) of 4.0 permeg for $\delta^{40}Ar/4$ and 3.7 permeg for $\delta^{15}N_{excess}$, which are for both quantities below the analytical measurement uncertainty of 4.0 permeg to 9.0 permeg for $\delta^{40}Ar/4$ and 5.0 permeg to 9.8 permeg for $\delta^{15}N_{excess}$ measured data (Kobashi et al., 2008b).

25 The automated inversion of different gas-isotope quantities ($\delta^{15}N$, $\delta^{40}Ar$, $\delta^{15}N_{excess}$) provides a unique opportunity to study the differences in the gained solutions using different targets and to improve our knowledge about the uncertainties of gas-isotope-based temperature reconstructions using a single firm model. Next, the presented algorithm is not dependent on the firm model, which leads to the implication that the algorithm can be coupled to different firm models describing firm physics in different ways. Furthermore, an automated reconstruction algorithm avoiding manual manipulation and leading to reproducible solutions makes it possible for the first time, to study and learn from the differences in-between solutions matching different targets. Finally, differences obtained by applying different firm physics (densification equations, convective zone, etc.) but the very same inversion algorithm may help to assess firm model shortcomings, resulting in more
30 robust uncertainty estimates than it was ever possible before.

In this publication we show the functionality and the basic concepts of the automated inversion algorithm using well known synthetic $\delta^{15}\text{N}$ fitting targets. In this “perfect world scenario” the forward problem, converting surface temperature to $\delta^{15}\text{N}$, as well as the inverse problem, converting $\delta^{15}\text{N}$ to surface temperature, is completely described by the used firn model. Consequently all sources of signal noise are ignored. For the later use of the algorithm on $\delta^{15}\text{N}$, $\delta^{40}\text{Ar}$ or $\delta^{15}\text{N}_{\text{excess}}$ measured data this will not be the case anymore due to different sources of signal noise in the used measured data. As a result, differences ~~in~~ between temperature solutions obtained from individual targets ($\delta^{15}\text{N}$, $\delta^{40}\text{Ar}$, $\delta^{15}\text{N}_{\text{excess}}$) will become obvious. These differences will allow to quantify the uncertainties associated with different unconstrained processes. Next, we will list and discuss potential sources of uncertainties and try to provide suggestions for their handling and quantification in our approach.

Measurement uncertainty and firn heterogeneity (cm-scale variability):

~~Many studies have investigated the influence of firn heterogeneity (or density fluctuations) on measurements of air compounds and quantities (e.g. $\delta^{15}\text{N}$, $\delta^{40}\text{Ar}$, CH_4 , CO_2 , O_2/N_2 ratio, air content) extracted from ice cores resulting in cm-scale variability and leading to additional noise on the measured data (e.g., Etheridge et al., 1992; Huber and Leuenberger, 2004; Fujita et al., 2009; Capron et al., 2010; Hörhold et al., 2011; Rhodes et al., 2013, 2016; Fourteau et al., 2017). Using discrete measurement technique instead of continuous sampling methods makes it difficult to quantify these effects. However, during discrete analyses of ice core air data it is common to measure replicates for given depths, from which the measurement uncertainties of the gas isotope data is calculated using pooled standard deviation (Hedges L. V., 1985). Often it is not possible to take real replicates (same depth) and instead the replicates are taken from nearby depths. Hence, any potential cm-scale variability is to some degree already included in the measurement uncertainty, because each measurement point represents the average over a few centimetres of ice. This is especially the case for low accumulation sites or glacial ice samples for which the vertical length of a sample (e.g., 10-25 cm long for the glacial part of the NGRIP ice core, Kindler et al., 2014) covers the equivalent of 20-yr to 50-yr of ice at approximately 35 kyr b2k. Increasing the depth resolution of the samples would increase our knowledge of cm-scale variability, for e.g. identifying anomalous entrapped gas layers that could have been rapidly isolated from the surface due to an overlying high density layer (e.g., Rosen et al., 2014). As this variability is likely due to heterogeneity in the density profile, modelling such heterogeneities (if possible at all) may not help to better reconstruct a meaningful temperature history, but rather to reproduce the source of noise. This means that the potential cm-scale variability, in many cases, is already incorporated in the analytical noise obtained from gas isotope measurements, due to analytical techniques themselves. Assuming the measurement uncertainty as Gaussian distributed, it is easy to incorporate this source of uncertainty in the inverse modelling approach presented here. This will increase the uncertainty of the temperature according to Eq. (10). The same equation can also be used for the calculation of the uncertainty in temperature related to measurement uncertainty in general.~~

Measurement uncertainty and firn heterogeneity (cm-scale variability):

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25 To answer the pertinent question of how to better extract a meaningful temperature history from a noisy ice-core record, an excellent – but costly – solution is of course to use multiple ice cores. For example, a $\delta^{15}\text{N}$ -based temperature reconstruction from the combination of data from the GISP2 ice core with the “sister ice core” GRIP drilled only a few30 kilometres apart is likely one of the best ways to overcome potential cm-scale variability. A comparison of ice cores that were drilled even closer might be even more advantageous.

Smoothing effects due to gas diffusion and trapping:

30 It is known that gas diffusion and trapping processes in the firm can smooth out fast signals and result in a damping of the amplitudes of gas isotope signals (e.g. Spahni et al., 2003; Grachev and Severinghaus, 2005). The duration of gas diffusion from the top of the diffusive column to the bottom where the air is closed off in bubbles is for Holocene conditions in Greenland approximately in the order of 10 yr (Schwander et al. 1997), whereas the data resolution of the synthetic targets was set to 20 yr to mimic the measurement data from Kobashi et al. (2008) with a mean data resolution of about 17 yr (see Sect. 2.3: “Generating synthetic target data”). In the study of Kindler et al. (2014) it was shown that a glacial Greenland LID

leads to a damping of the $\delta^{15}\text{N}$ signal of about 30 % for a 10 K temperature rise in 20 yr. We further assume that the smoothing according to the lock-in process is negligible for Greenland Holocene conditions according to the much smaller amplitude signals and shallower LID. Yet, for glacial conditions it requires attention.

Accumulation rate uncertainties:

For the synthetic data study presented in this paper it is assumed that the used accumulation rate data is well known that gas-diffusion and trapping processes in the firm can smooth out fast signals and result in a damping of the amplitudes of gas-isotope signals (e.g. Spahni et al., 2003; Grachev and Severinghaus, 2005). The duration of gas diffusion from the top of the diffusive column to the bottom where the air is closed off in bubbles is for Holocene conditions in Greenland approximately in the order of 10 yr (Schwander et al. 1997), whereas the data resolution of the synthetic targets was set to 20 yr to mimic the measurement data from Kobashi et al. (2008b) with a mean data resolution of about 17 yr (see Sect. 2.3: “Generating synthetic target data”). In the study of Kindler et al. (2014) it was shown that a glacial Greenland lock-in-depth leads to a damping of the $\delta^{15}\text{N}$ signal of about 30 % for a 10 K temperature rise in 20 yr. We further assume that the smoothing according to the lock-in process is negligible for Greenland Holocene conditions according to the much smaller amplitude signals and shallower LID. Yet, for glacial conditions it requires attention.

Accumulation rate uncertainties:

For the synthetic data study presented in this paper it is assumed that the used accumulation-rate data are well known with zero uncertainty. This simplification is used to show the functionality and basic concepts of the presented fitting algorithm in every detail on well-known $\delta^{15}\text{N}$ and temperature targets and to focus on the final uncertainties originating from the presented fitting algorithm itself. For the later reconstruction using measured gas-isotope data together with the published accumulation-rate scenarios shown in Fig. S01+supplement S1 this will not be the case anymore. Uncertainties in layer-counting and corrections for ice thinning lead to a fundamental uncertainty. Especially in the early Holocene, this can easily exceed 10 %. As the accumulation-rate data is used to run the firm model, all potential accumulation uncertainties are in part incorporated into the temperature reconstruction. On the other hand, as we discussed in section 2.3+supplement S2, the accumulation rate variability has a minor impact compared to the input temperature on the variability of $\delta^{15}\text{N}$ data in the Holocene (see also Fig. S03, Fig. S04). The influence of these quantities, accumulation rate or temperature, on the temperature reconstruction is not equal; during the Holocene, accumulation-rate variability explains about 12 % to 30 % of $\delta^{15}\text{N}$ variability. 30 % corresponds to the 8.2 kyr event and 12 % for the mean of the whole Holocene period including the 8.2 kyr event. Hence the influence of accumulation changes, excluding the extreme 8.2 kyr event, is generally below 10 % during the Holocene. If the accumulation is assumed to be completely correct then the missing part will be assigned to temperature variations. Nevertheless for the fitting of the Holocene measurement-data we will use all three accumulation-rate scenarios as shown in Fig. S04+S1. The difference in the reconstructed temperatures arising from the differences of these three scenarios will be used for the uncertainty calculation as well and is most likely higher than the uncertainty arising from

uncertainties due to the process of producing the accumulation-rate data and from the conversion of the accumulation-rate data to the GICC05 timescale.

Convective zone variability:

Many studies have shown the existence of a non diffusive zone at the top of the diffusive firn column, called convective zone (CZ). The CZ is formed by strong katabatic winds and pressure gradients between the surface and the firn (e.g. Kawamura et al., 2006, 2013; Severinghaus et al., 2010). The existence of a CZ changes the gravitational background signal in $\delta^{15}\text{N}$ and $\delta^{40}\text{Ar}$ as it reduces the diffusive column height. The presented fitting algorithm was used together with the two most frequently used firn models for temperature reconstructions based on stable isotopes of air, the Schwander et al. (1997) model which has no CZ build-in (or better a constant CZ of 0 m) and the Goujon firn model (Goujon et al., 2003) (which assumes a constant convective zone over time, that can easily be set in the code). This difference between the two firn models only changes significantly the absolute temperature rather than the temperature anomalies as it was shown by other studies (e.g., Guillevie et al., 2013, Fig. 3). In the presented work, we show the results using the model from Schwander et al. (1997), because the differences between the obtained solutions using the two models are negligible besides a constant temperature offset. Also, noteworthy is that there is no firn model at the moment which uses a dynamically changing CZ. Indeed, this should be investigated but requires additional intense work. Additionally, the knowledge of the time evolution of CZ changes for time periods of millennia to several hundreds of millennia (in frequency and magnitude) is too poor to estimate the influence of this quantity on the reconstruction. In principle it is possible to cancel out the influence of a potentially changing CZ by using $\delta^{15}\text{N}_{\text{excess}}$ data for temperature reconstruction, as due to the subtraction of $\delta^{40}\text{Ar}/4$ from $\delta^{15}\text{N}$ the gravitational term of the signals is eliminated. From that point of view it will be interesting to compare temperature solutions gained from $\delta^{15}\text{N}_{\text{excess}}$ fitting with the solutions based on $\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$ alone. This can offer a useful tool for quantifying the magnitude and frequency of CZ changes in the time interval of interest.

It is known that for some very low accumulation rate sites in areas with strong katabatic winds (e.g. "Megadunes", Antarctica) extremely deep CZs can occur, which are potentially able to smooth out even decadal scale temperature variations (Severinghaus et al., 2010). For this its deepness would need to be of several dozens of meters, which is highly unrealistic even for glacial Summit conditions (Guillevie et al., 2013, see discussion in Annex A4, p. 1042) as well as for the rather stable Holocene period in Greenland for which no low accumulation and strong katabatic wind situations are to be expected.

4.4 Proof of concept for glacial data

For glacial conditions the task of reconstructing temperature (with correct frequency and magnitude) without using $\delta^{18}\text{O}_{\text{ice}}$ information is much more challenging due to the highly variable gas age - ice age differences (Δage) between stadial and interstadial conditions. Here, contrary to the rather stable Holocene period, the Δage can vary by several hundreds of years. Also the accumulation rate data is more uncertain than for the Holocene. To prove that the presented fitting algorithm also

works for glacial conditions we inverted the $\delta^{15}\text{N}$ data measured for the NGRIP ice core by Kindler et al. (2014) for two Dansgaard-Oeschger events, namely DO6 and DO7. Since the magnitudes of those events are higher and the signals are smoother than in the Holocene we only had to use the Monte Carlo type input generator (see Sect. 2.3.2) for changing the temperature inputs. To compare our results to the $\delta^{18}\text{O}_{\text{ice}}$ -based and manually calibrated values from Kindler et al. (2014) we use the ss09sea06bm time scale (NGRIP members: Andersen et al., 2004; Johnsen et al., 2001) as it was done in the Kindler et al. publication. For the model spin up we use the accumulation rate and temperature data from Kindler et al. (2014) for the time span 36.2 kyr to 60 kyr. The reconstruction window (containing DO6 and DO7) is set to 32 kyr to 36.2 kyr. As the first guess (starting point) of the reconstruction we use the accumulation rate data for NGRIP from the ss09sea06bm time scale together with a constant temperature of about -49°C for this time window. As minimization criterion D for the reconstruction we simply use the sum of the mean squared errors of the $\delta^{15}\text{N}$ and Δage mismatches weighted with their uncertainties (wRMSE) according to the following equation instead of the mean $\delta^{15}\text{N}$ misfit alone as used for the Holocene (Eq. (8)):

$$D = \sqrt{\text{wRMSE}(\delta^{15}\text{N})} + \sqrt{\text{wRMSE}(\Delta\text{age})} \quad (15)$$

Convective zone variability:

Many studies have shown the existence of a non-diffusive zone at the top of the diffusive-firm-column, called convective zone (CZ). The CZ is formed by strong katabatic winds and pressure gradients between the surface and the firm (e.g. Kawamura et al., 2006, 2013; Severinghaus et al., 2010). The existence of a CZ changes the gravitational background signal in $\delta^{15}\text{N}$ and $\delta^{40}\text{Ar}$ as it reduces the diffusive-column-height. The presented fitting algorithm was used together with the two most frequently used firm models for temperature reconstructions based on stable isotopes of air, the Schwander et al. (1997) model which has no CZ build in (or better a constant CZ of 0 m) and the Goujon firm model (Goujon et al., 2003) (which assumes a constant convective zone over time, that can easily be set in the code). This difference between the two firm models only changes significantly the absolute temperature rather than the temperature anomalies as it was shown by other studies (e.g., Guillevic et al., 2013, Fig. 3). In the presented work, we show the results using the model from Schwander et al. (1997), because the differences between the obtained solutions using the two models are negligible besides a constant temperature offset. Also, noteworthy is that there is no firm model at the moment which uses a dynamically changing CZ. Indeed, this should be investigated but requires additional intense work. Additionally, the knowledge of the time-evolution of CZ changes for time periods of millennia to several hundreds of millennia (in frequency and magnitude) is too poor to estimate the influence of this quantity on the reconstruction. In principle it is possible to cancel-out the influence of a potentially changing CZ by using $\delta^{15}\text{N}_{\text{excess}}$ data for temperature reconstruction, as due to the subtraction of $\delta^{40}\text{Ar}/4$ from $\delta^{15}\text{N}$ the gravitational term of the signals is eliminated. From that point of view it will be interesting to compare temperature solutions gained from $\delta^{15}\text{N}_{\text{excess}}$ fitting with the solutions based on $\delta^{15}\text{N}$ or $\delta^{40}\text{Ar}$ alone. This can offer a useful tool for quantifying the magnitude and frequency of CZ changes in the time interval of interest.

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4.4 Proof of concept for glacial data

For glacial conditions the task of reconstructing temperature (with correct frequency and magnitude) without using $\delta^{18}\text{O}_{\text{ice}}$ information is much more challenging due to the highly variable gas-age - ice-age differences (Δage) between stadial and interstadial conditions. Here, contrary to the rather stable Holocene period, the Δage can vary by several hundreds of years. Also the accumulation-rate data are more uncertain than for the Holocene. To prove that the presented fitting algorithm also works for glacial conditions we inverted the $\delta^{15}\text{N}$ data measured for the NGRIP ice core by Kindler et al. (2014) for two

Dansgaard-Oeschger events, namely DO6 and DO7. Since the magnitudes of those events are higher and the signals are smoother than in the Holocene we only had to use the Monte-Carlo-type input-generator (see Sect. 2.3.2) for changing the temperature inputs. To compare our results to the $\delta^{18}\text{O}_{\text{ice}}$ -based and manually calibrated values from Kindler et al. (2014) we use the ss09sea06bm time scale (NGRIP members: Andersen et al., 2004; Johnsen et al., 2001) as it was done in the Kindler et al. publication. For the model spin-up we use the accumulation-rate and temperature data from Kindler et al. (2014) for the time span 36.2 kyr to 60 kyr. The reconstruction window (containing DO6 and DO7) is set to 32 kyr to 36.2 kyr. As the first-guess (starting point) of the reconstruction we use the accumulation-rate data ($\text{Acc}_{g,0}$) for NGRIP from the ss09sea06bm time-scale together with a constant temperature of about -49°C for this time window. As minimization-criterion D_g for the reconstruction we simply use the sum of the root-mean-squared-errors of the $\delta^{15}\text{N}$ and Δage mismatches weighted with their uncertainties (wRMSE) according to the following equation, instead of the mean $\delta^{15}\text{N}$ misfit alone as used for the Holocene (eq. (1)).

$$D_{g1} = \text{wRMSE}(\delta^{15}\text{N}) + \text{wRMSE}(\Delta\text{age}) \quad (14)$$

$$= \sqrt{\frac{1}{N} \sum_i \left[\frac{\delta^{15}\text{N}_{\text{meas},i} - \delta^{15}\text{N}_{\text{mod},i}}{\epsilon_{\delta^{15}\text{N},i}} \right]^2} + \sqrt{\frac{1}{M} \sum_j \left[\frac{\Delta\text{age}_{\text{meas},j} - \Delta\text{age}_{\text{mod},j}}{\epsilon_{\Delta\text{age},j}} \right]^2} + \sqrt{\frac{1}{M} \sum_k \left[\frac{\Delta\text{age}_{\text{meas},k} - \Delta\text{age}_{\text{mod},k}}{\epsilon_{\Delta\text{age},k}} \right]^2}$$

Here $\epsilon_{\delta^{15}\text{N},i}$ and $\epsilon_{\Delta\text{age},j}$ are the uncertainties in $\delta^{15}\text{N}$ and Δage for the measured values i or j (Δage match points: Guillevic, M. (2013) Guillevic, M. (2013), p.65, Tab. 3.2) and N, M the number of measurement values. We set $\epsilon_{\delta^{15}\text{N},i} = 20$ permeg for all i (Kindler et al., 2014) and $\epsilon_{\Delta\text{age},j} = 50$ yr for all j . The relative uncertainties in Δage can easily reach up to 50 % and more in the Glacial using the ss09sea06bm time-scale which results in a pre-eminence of the $\delta^{15}\text{N}$ misfits over the Δage misfits (10 % to 20 % when using GICC05 time-scale; Guillevic (2013), p. Guillevic, M., 2013, p. 65 Tab. 3.2). Due to this issue we have to set Δage uncertainties to 50 yr to make both terms equally important for the fitting algorithm. In Fig. S13.11 we show preliminary results. The $\delta^{15}\text{N}$ and Δage fitting (a, b) and the resulting gained temperature and accumulation-rate solutions (c, d) using the presented algorithm are completely independent from $\delta^{18}\text{O}_{\text{ice}}$ which provides the opportunity to evaluate the $\delta^{18}\text{O}_{\text{ice}}$ -based reconstructions. In this study the algorithm was used in three steps. First, starting with the first-guess (constant temperature), the temperature was changed as explained before. The accumulation rate was changed in parallel to the temperature allowing a random offset shift (up and down) together with a stretching or compressing (in y direction) of the accumulation-rate signal over the whole time-window (32 kyr to 36.2 kyr). This first step leads to the “Monte-Carlo Solution 0” (MCS0) which provides a first approximation and is the base for the next step. For the next step, we fixed the accumulation rate and let the algorithm only change the temperature to improve the $\delta^{15}\text{N}$ -fit (MSC1). Finally, we allow the algorithm to change the temperature together with the accumulation rate using the Monte-Carlo-type input-generator for both quantities. This allows to change the shape of the accumulation-rate data. This final step can be seen as a fine tuning of the gained solutions from the steps before. The obtained mismatches in $\delta^{15}\text{N}$ and Δage of all steps are at least of the same quality or better than the $\delta^{18}\text{O}_{\text{ice}}$ -based manual method from Kindler et al. (2014)

(see [Tab. S02/ Table 06](#)). The gained temperature solutions show a very good agreement in timing and magnitude compared to the reconstruction of Kindler et al. (2014). Also the accumulation-rate solutions show that the accumulation has to be reduced significantly compared to the ss09sea06bm data to allow a [high-quality suitable](#) fit of the $\delta^{15}\text{N}$ and Δage target data, a result highly similar to Guillevic et al. (2013) and Kindler et al. (2014). The mismatches in $\delta^{15}\text{N}$ and Δage of the final MCS FIN solution show a 15 % smaller misfit ~~in~~ of $\delta^{15}\text{N}$ (2σ) and an about 31 % smaller misfit ~~for~~ of Δage (2σ) compared to the Kindler et al. (2014) solution. Keeping in mind that the used approach is completely independent from $\delta^{18}\text{O}_{\text{ice}}$ strengthens the functionality and quality of the presented gas-isotope fitting approach also for glacial reconstructions. As this section contains a ~~proof-of-concept~~ of the presented automated gas-isotope fitting algorithm on glacial data, preliminary results and ongoing work were shown here. Furthermore as the presented fitting algorithm was developed and tested in first order for Holocene-like data, it is highly probable that the functionality of the algorithm using glacial data will be further extended and adjusted in future studies.

5. Conclusion

A novel approach is introduced and described for inverting a firm-densification and heat-diffusion model to fit small gas-isotope-data variations as observed throughout the Holocene. From this new fitting method, it is possible to extract the surface-temperature history that drives the firm status which in turn leads to the gas-isotope time-series. The approach is a combination of a Monte-Carlo-based iterative method and the analysis of remaining mismatches between modelled and target data. The procedure works fully automated and provides a high potential for parallel computing for time consumption optimization. Additional sensitivity experiments have shown that accumulation-rate changes have only a minor influence on short-term variations of $\delta^{15}\text{N}$, which themselves are mainly driven by high-frequency temperature variations. To evaluate the performances of the presented approach, eight different synthetic $\delta^{15}\text{N}$ time-series were created from eight known temperature histories. The fitting approach leads to an excellent agreement in timing and amplitudes between the modelled and synthetic $\delta^{15}\text{N}$ and temperature data. The obtained final mismatches follow a symmetric standard-distribution-function. 95 % of the mismatches compared to the synthetic data are in an envelope ~~in~~ between 3.0 permeg to 6.3 permeg for $\delta^{15}\text{N}$ and 0.23 K to 0.51 K for temperature, depending on the synthetic temperature ~~history~~-scenarios. These values can therefore be used as a 2σ estimate for the reconstruction uncertainty arising from the presented fitting algorithm itself. For $\delta^{15}\text{N}$ the obtained final uncertainties are in the same order of magnitude as state of the art ~~experimental~~-measurement uncertainty. The presented reconstruction approach was also successfully applied to $\delta^{40}\text{Ar}$ and $\delta^{15}\text{N}_{\text{excess}}$ measured data. Moreover, we have shown that the presented fitting approach can also be applied to glacial temperature reconstructions with minor algorithm modifications. Based on the demonstrated flexibility of our inversion methodology, it is reasonable to adapt this approach for reconstructions of other non-linear physical processes.

Competing interests

The authors declare that they have no competing financial interests.

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