

**Title: Early warnings and missed alarms for abrupt monsoon transitions**  
**Author(s): Z.A. Thomas et al.**  
**MS No.: cp-2015-39**  
**MS Type: Research Article**

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**Editor Decision: Reconsider after major revisions** (08 Sep 2015) by Prof. Dr. Martin Claussen

Comments to the Author:

Dear authors,

The referees agree that your paper has substantially improved. Referee 1 and 3 request only minor revisions, while referee 2 is still not convinced by your presentation. As far as I can judge, the latter criticism does not point at major flaws. Nonetheless some of your presentation does not seem to be very clear. Since this is a matter of concise formulation, I am convinced that you will be able to properly deal with it. Hence I encourage you to submit a re-revision which will be reviewed by referee 2.

Best regards

Martin Claussen

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Dear Martin

Many thanks for the referee comments. We were very pleased to hear that our manuscript has substantially improved. We have carefully looked at all the comments and have revised and clarified our manuscript accordingly. We thank all three reviewers for their helpful suggestions. We hope you will find further improvement in our responses and revised manuscript.

Best wishes

Zoë Thomas (on behalf of all co-authors)

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## Report #1

Submitted on 18 Aug 2015  
Anonymous Referee #3

**Anonymous during peer-review:** Yes No

**Anonymous in acknowledgements of published article:** Yes No

### Recommendation to the Editor

#### 1) Scientific Significance

Does the manuscript represent a substantial contribution to scientific progress within the scope of this journal (substantial new concepts, ideas, methods, or data)?

Excellent **Good** Fair Poor

## 2) Scientific Quality

Are the scientific approach and applied methods valid? Are the results discussed in an appropriate and balanced way (consideration of related work, including appropriate references)?

Excellent **Good** Fair Poor

## 3) Presentation Quality

Are the scientific results and conclusions presented in a clear, concise, and well structured way (number and quality of figures/tables, appropriate use of English language)?

Excellent **Good** Fair Poor

For final publication, the manuscript should be

**accepted as is**

accepted subject to **technical corrections**

**accepted subject to minor revisions**

reconsidered after **major revisions**

I would like to review the revised paper

I would NOT be willing to review the revised paper

**rejected**

Please note that this rating only refers to this version of the manuscript!

## Suggestions for revision or reasons for rejection (will be published if the paper is accepted for final publication)

2nd Review of "Early warnings and missed alarms for abrupt monsoon transitions" by Z. A. Thomas, F. Kwasniok, C. A. Boulton, P. M. Cox, R. T. Jones, T. M. Lenton, and C. S. M. Turney.

The revised version of the manuscript I find much improved and a lot more convincing. I especially like the revised section two with the separate subsection on assessing significance.

Nonetheless, I still have a few – by now relatively minor – points:

- The discussion of significance of the increases in ACF and VAR for the earlier transitions is much improved, but it still isn't clear immediately why the EWS for all of them are rejected. This would become clearer, if the lines marking the Kendall tau values for the various periods in Fig. 5 were annotated. This way it would become clear, which Kendall tau value is achieved for which transition (though the reader CAN, of course, get this information from Fig. 4), thus making understanding this point more intuitive.

A detailed description of how the surrogate time series are obtained can be found in Section 2.3.1, however, we have pointed the reader to this section in the Figure caption, and include a brief explanation of what a high/low Kendall tau means, as also suggested by Reviewer #3 (lines 248-249). We thank the reviewer for the suggestion of annotating the bars in Figure 5 to show the periods to which they correspond; we have implemented this, which makes the interpretation much clearer.

- The discussion of Fig. 9 is still exceedingly brief. Yes, of course it cannot be expected that such a simple model cannot capture the full dynamics of the system, but this is not discussed at all when the figure is discussed (page 18, lines 432 to page 19, line 455). This way the reader is left wondering what conclusions to draw – the simple one being that the potential model is plain wrong. Therefore the figure needs to be better discussed in order to lend credibility to the use of the potential model.

We have extended the discussion of both the potential model (see lines 297-305, 406-421) and Figure 9 (519-522), including some remarks on the limitations of the potential model:

*“Palaeoclimatic records reflect a multitude of complex processes and any model as simple as equation (1) cannot be expected to be more than a skeleton model used to pinpoint and contrast*

*basic dynamical mechanisms*” (lines 338-342).

- Line 31: The term “monsoon termination” is highly interesting. Is that standard usage? What is the definition?

The term ‘monsoon termination’ is used relatively widely within palaeo-monsoon literature e.g. Cheng et al. 2006, *Geology* and Kelly et al. 2006, *Palaeo3*. It simply refers to the timing of the glacial terminations with respect to the monsoon records, rather than the atmospheric CO<sub>2</sub> record.

- Line 44-46: Future monsoon shifts having societal impacts similar to past monsoon shifts would imply that the vulnerability of society has not changed. There are good reasons for doubting this. This is a fair point in that the vulnerability of society clearly has changed. We have reworded this to remove this potential confusion: “*Though the vulnerability of society has clearly changed, future abrupt monsoon shifts, whether caused by orbital or anthropogenic forcing, are likely to have major devastating societal impacts (Donges et al., 2015).*” (lines 49-63).

## Report #2

Submitted on 02 Sep 2015

Anonymous Referee #2

**Anonymous during peer-review: Yes No**

**Anonymous in acknowledgements of published article: Yes No**

### Recommendation to the Editor

#### 1) Scientific Significance

Does the manuscript represent a substantial contribution to scientific progress within the scope of this journal (substantial new concepts, ideas, methods, or data)?

Excellent **Good** Fair Poor

#### 2) Scientific Quality

Are the scientific approach and applied methods valid? Are the results discussed in an appropriate and balanced way (consideration of related work, including appropriate references)?

Excellent Good **Fair** Poor

#### 3) Presentation Quality

Are the scientific results and conclusions presented in a clear, concise, and well structured way (number and quality of figures/tables, appropriate use of English language)?

Excellent Good Fair **Poor**

For final publication, the manuscript should be

**accepted as is**

accepted subject to **technical corrections**

accepted subject to **minor revisions**

**reconsidered after major revisions**

**I would like to review the revised paper**

I would NOT be willing to review the revised paper

**rejected**

Please note that this rating only refers to this version of the manuscript!

**Suggestions for revision or reasons for rejection (will be published if the paper is accepted for final publication)**

Review of revised manuscript “Early warnings and missed alarms for abrupt monsoon transitions” by Thomas et al.

Main points of criticism on the first version of this ms concentrated on a lack of critical attitude, lack of explanation on methods, and presentation. All reviewers found the subject matter and analysis interesting. While this revision certainly has improved, I still feel it falls somewhat short of standards for a publication in *Climate of the Past*. Nevertheless, I still believe the authors should be capable of submitting a version that meets these standards.

Specific comments:

I am not always convinced by the presentation and (lack of) flow of the narrative. At present methodological details are explained before or after the results/figures they apply to. This gives the ms the appearance of a series of disconnected or separate paragraphs. To some extent this may be a matter of taste but there are several places where this becomes problematic.

We are sorry that the reviewer still finds some inconsistencies with our narrative. We have carefully reviewed this again and hope that our changes are satisfactory.

1. Figure 1. What are we seeing here? Delta-O18. But what does it mean? Temperature? Precipitation? There is some discussion on Delta-18 2 pages after introducing Fig. 1, but this is insufficient. If the data represent precipitation, the question is what precip? Annual mean? Summer mean? Extreme values? To know this exactly or as good as possible is important as the authors later on model these timeseries, a.o. with a model based on a Langevin equation. One cannot judge the validity of the model if one does not know what “x” in this model means.

Related to the point above, we feel that the discussion on speleothem  $\delta^{18}\text{O}$  is in the most appropriate place without disrupting the introduction of the manuscript. We do understand the reviewer's point though, and we have therefore added a brief explanation of what the speleothem  $\delta^{18}\text{O}$  refers to earlier in the manuscript when Figure 1 is introduced, and then point to the Section that addresses this in more detail (lines 44-45). Speleothem  $\delta^{18}\text{O}$  from Chinese caves is interpreted to be a precipitation proxy, with more negative  $\delta^{18}\text{O}$  values corresponding to a weaker monsoon and less negative  $\delta^{18}\text{O}$  values corresponding to a stronger monsoon. We thank the reviewer for highlighting this, and have also added an annotation to illustrate this more clearly in Figure 1, which we believe further increases the clarity.

2. The authors defend the Langevin-model by saying it is just a simple skeleton model. This does not mean that assumptions underlying this model should not be discussed and motivated. One assumption is white noise. If we know what x or x-dot means we can discuss how well this assumption is. If eta reflects some precipitation measure it can be validated from actual observations and actual (climate model) runs. Same for the linear relation between insolation and x-dot. There is a lot written about the relation between hydrological cycle and radiative forcing.

We think it is canonical to start with white noise and a linear forcing in order to keep the model simple and the number of parameters to a minimum. It is beyond the scope of the present study to rigorously test these assumptions with data. Specifically, this model is used to pinpoint and contrast basic dynamical mechanisms, rather than exactly replicating the detailed dynamics of the monsoon. We have compared our model against a simpler model without insolation forcing and against a more complicated model where all four parameters of the potential depend on time. Based on the likelihood function and both the Akaike and the Bayesian information criterion, we are able to refute the other models. More detail on this is now given in the revised manuscript (lines 406-421).

3. In particular, it seems that the amplitude of the noise is chosen by the model or seen as an arbitrary tuning parameter varied in the discussion. The amplitude of the noise determines whether one finds early warning signals or not. Again, the amplitude should and could be constrained by actual observations and modeling time series. See also Fig. 11 and subsequent discussion.

The noise level is robustly estimated directly from the speleothem data, “*determined from the dynamical likelihood function based on the time evolution of the system (Kwasniok, 2015)*” (lines 323-325), together with the other model parameters (also lines 310-311 further clarified). The uncertainty in all parameters, including the noise level, is very small, making our model estimation

robust. The noise level is then subsequently varied in order to study early warning signals in a hypothetical scenario with different noise level (see lines 363-365 and 372-373).

4. The authors introduce Type-I and Type\_II errors without explaining what they mean. These terms may be common in a small mathematical-statistical expert-group, but this does not extend to the general Climate of the Past readership.

We have included a brief definition of these terms to ensure clarity: “*Although efforts have been taken to reduce the chances of type I (incorrect rejection of a true null hypothesis, otherwise known as a ‘false positive’) and type II (failure to reject a false null hypothesis, or ‘false negative’) errors...*” (lines 136-144).

5. One wonders why both 90% and 95% percentiles are used, seemingly at random, for rejecting hypotheses.

The 90% and 95% significance levels are commonly used as benchmarks for statistical significance. However, we should be consistent with which significance levels we use in Figure 5, so we have amended the plot to show the 90% level on all four plots. There is currently no consensus with regards the suitable significance level that should be used (as stated in lines 252-257). Most tipping point literature identifies an increasing trend using the Kendall tau statistic and measures the robustness using a similar null model, where p values of  $<0.1$  are considered ‘robust’ e.g. Dakos et al. 2008, Boulton and Lenton 2015, *PNAS*. We have thus chosen p values of  $<0.1$  as the benchmark for significance for our study (see lines 260-262).

6. In Fig. 5 the authors could explain more how the surrogate time series are obtained, what it means if the Kendall low or high for specific subsections of the timeseries and which bar in panels a and b corresponds to which period.

A detailed description of how the surrogate time series are obtained can be found in Section 2.3.1, however, we have pointed the reader to this section in the Figure caption, and include a short section explain what a high/low Kendall tau means (lines 248-249). We have colour-coded the bars in Figure 5 to show the periods to which they correspond, which we agree makes interpretation much clearer.

7. The lack of EWS in other subsections of the timeseries than 150-129 ka BP is attributed to a lack of resolution. The possibility of stochastic resonance or noise-induced transitions is not discussed at all. The authors simply “jump” to a conclusion, or even worse, say “we speculate” without addressing other options or motivating their speculation.

We do briefly discuss the possibility of noise-induced switches and stochastic resonance (lines 109-113, 297-305), and conclude that in our potential model, the two stable states are not available at the same time for long enough for noise-induced transitions to play a significant role. We have, however, included a paragraph in the discussion section to further explain why do not consider these alternate scenarios to be likely (lines 614-623).

8. Figure 10 shows the potential well flattening over a normal transition cycle and a transition cycle at the termination. The distinction between these two is nowhere explained or illustrated. Which cycles do we see? In what respect are they different? Which time period? Please point to the original data!

The two transition cycles in Figure 10 are the termination (150-128.5 kyr) and the period 198-175 kyr, as shown in Figure 10a. We are not quite sure what original data the reviewer is referring to here; this data is the same Sanbao cave  $\delta^{18}\text{O}$  data as used in the potential model. We have amended the figure caption to make this clear. Figure 10 is intended to illustrate that the potential well is flatter during the transition cycle at the termination in comparison to one of the termination cycles from the glacial period. This distinction helps to explain why early warning signals in the form of increasing autocorrelation and variance are found immediately preceding the termination, but not for the other monsoon transitions (see lines 562-564).

## Report #3

Submitted on 06 Sep 2015

Anonymous Referee #1

**Anonymous during peer-review:** Yes No

**Anonymous in acknowledgements of published article:** Yes No

**Recommendation to the Editor**

**1) Scientific Significance**

Does the manuscript represent a substantial contribution to scientific progress within the scope of this journal (substantial new concepts, ideas, methods, or data)?

Excellent Good **Fair** Poor

**2) Scientific Quality**

Are the scientific approach and applied methods valid? Are the results discussed in an appropriate and balanced way (consideration of related work, including appropriate references)?

Excellent Good **Fair** Poor

**3) Presentation Quality**

Are the scientific results and conclusions presented in a clear, concise, and well structured way (number and quality of figures/tables, appropriate use of English language)?

Excellent **Good** Fair Poor

For final publication, the manuscript should be

**accepted as is**

accepted subject to **technical corrections**

**accepted subject to minor revisions**

reconsidered after **major revisions**

I would like to review the revised paper

I would NOT be willing to review the revised paper

**rejected**

Please note that this rating only refers to this version of the manuscript!

**Suggestions for revision or reasons for rejection (will be published if the paper is accepted for final publication)**

In my opinion, the authors have managed to come up with a much clearer and more transparent manuscript. It is now clear to me what the authors do and why: The fundamental question is whether one can distinguish from the speleothem record if the abrupt monsoon switches are associated with bifurcations or with switches between permanent alternative states. The authors point to this question and show that their potential model is in line with the bifurcation hypothesis. In principle, I think that this result just merits a publication because I see no killing argument against it. However, it still remains unclear to me to what extent the author's results are any evidence for the bifurcation hypothesis in contrast to a sophisticated speculation. I hope that further research will tackle this question more thoroughly, and that the authors still improve their manuscript, by addressing some of the following points.

The authors state that their potential model should "supplement the analysis of the speleothem records and help interpret the results". I rather think that this model is at the heart of the analysis and that the message of the paper rests on this model. It is thus important to argue why it is an appropriate model, and why alternative explanations (e.g. nonlinear response to forcing, or stochastic resonance) are less plausible, ideally by using statistical tests to refute some hypothesis. The fact that the authors come up with a model that describes the abrupt changes as bifurcations does not prove that the model is more likely to be true than any other model. Although the way the authors derive the model is now transparent, it is not very transparent to me how sensitive the

results are to different choices during the model derivation. The fact that a simpler approach fails due to a negative leading coefficient indicates that the model is not robust. I still wonder how robust the results are to the choices during the model derivation. For example, why is the solar forcing a linear term added to the potential U? Why not say that the four parameters of U all depend on time?

We have compared our model against a simpler model without insolation forcing and against a more complicated model where all four parameters of the potential depend on time. Based on the likelihood function and both the Akaike and the Bayesian information criterion, we are able to refute the other models. More detail on this is now given in the revised manuscript (lines 406-421).

The authors do not find “early warnings” though they would be expected if their bifurcation hypothesis was true, and argue that the time series are too short and the noise level is too large for a detection. Is there any further line of evidence to substantiate this claim? How robust is the noise level estimate?

The noise level is robustly estimated directly from the speleothem data, “*determined from the dynamical likelihood function based on the time evolution of the system (Kwasniok, 2015)*” (lines 323-325), together with the other model parameters (also lines 310-311 further clarified). The estimation of all model parameters, including the noise level, is robust; the parameter uncertainties are very small. Based on the assumption that the monsoon transitions are characterized by a bifurcation (which is supported by both our model, and previous studies e.g. Schewe et al. 2012), Figure 11 shows that with a reduced noise level and higher resolution in the potential model simulations, early warning signals are detected. We have, however, added to the initial discussion of false positives of early warning signals (lines 136-144), as well as a further point: “*To guard against type I errors, we determine for this study that ‘statistically significant’ early warning indicators occur with increases in both autocorrelation and variance with p-values > 0.1. We have chosen this benchmark in line with previous studies using a similar null model that have described results with  $p < 0.1$  as ‘robust’ (Dakos et al., 2008; Boulton & Lenton, 2015)*” (lines 257-262, also lines 440-442).

I think it is sensible in this context to check the dependence of “early warnings” on noise level and resolution, using the potential model, as the authors do. However, it is not clear to me whether the results confirm the claim that most transitions are below detectability, while termination II is above detectability. At which length of the record would the signal become significant? I think this is something else than examining the resolution because of the autocorrelation in the time series (see my point on characteristic timescale below).

Figure 11 is intended to illustrate the effects of the noise level and resolution on the potential, and shows that much lower Kendall tau values are measured with an increasing sample step (lower resolution), and a higher noise level. Given that our potential model (and other studies of the EASM) indicates that the monsoon system has bifurcation points between the strong and weak states, a possible explanation is that the resolution of the speleothem data is below detectability, since Figure 11 clearly illustrates the detrimental effect of a lower resolution on Kendall tau values, particularly for autocorrelation (lines 626-628). Indeed, Figure 5 shows that higher Kendall tau values are detected for variance in the monsoon transitions prior to 150 ka BP. Since the monsoon transition at the termination does display early warning signals, we suggest that this may be because the background state of the climate system is different to that of the other monsoon transitions, and may well present a longer timescale of internal variability, which allows the detection of early warning signals.

By the way, just from looking at the data, the time series from Hulu cave does not occur bimodal to me, and the shifts are less abrupt / less permanent. The authors often refer to “the speleothem data”, but I have the impression it is only the Sanbao record they use for their potential model, while they still analyse early warnings in the Hulu record. This seems to be contradictory.

The Hulu cave speleothem record is markedly shorter than the Sanbao cave speleothem record. Indeed the Hulu cave data duplicates only the last 30 kyr of the 100 kyr long Sanbao cave record, where the bimodal character is also less visually strong. The reviewer is correct that we use only the Sanbao cave data to create the potential model; we have made this more explicit.

Further (minor) remarks

Another problem that I think remains in the revised manuscript is the lack of a physical mechanism to explain the relaxation time of the system. The authors correctly point out in line 102 that “Detecting the phenomenon of critical slowing down relies on a timescale separation, whereby the timescale forcing the system is much slower than the timescale of the system’s internal dynamics, which is in turn much longer than the frequency of data sampling the system (Held and Kleinen, 2004).” However, I missed an explanation why this timescale separation applies to the East Asian monsoon (why should monsoon respond much slower to forcing than the resolution of the record, i.e. ~100 years?). Also, this seems to be at odds to the often cited Zickfeld/Levermann/Schewe model which seems to have a much faster timescale given the rapid processes in the atmosphere. I guess it must be the model’s parameters determined by the ocean that somehow adjust slowly to the change in insolation?

We apologise for the confusion here. We interpret the timescale of the forcing to be on an orbital scale – that is, driven by the 23 ka precession cycle. Importantly, the monsoon transitions span hundreds of years (several data points), this meets the criterion that the frequency of our sampling is higher than the timescale of the transition of the system (lines 130-133). This therefore suggests that it is the slow ocean dynamics, rather than faster atmospheric dynamics that may be governing shifts in the ITCZ. This is supported by Deplazes et al. (2013) *Nature Geoscience*, who show that the marine records of monsoon transitions occur over centuries rather than decades. Similarly, the strong correlation in the last glacial cycle between Dansgaard-Oeschger events (linked to changes in ocean circulation) and abrupt monsoon shifts, suggests that it is the slow ocean dynamics that ultimately govern monsoon shifts.

line 97: “While it has been theoretically established that autocorrelation and variance should both increase together (Ditlevsen and Johnsen, 2010; Thompson and Sieber, 2011), there are some factors which can negate this, discussed in detail in Dakos et al. (2012b, 2014).”

I still don’t see clearly why this is noted here. What does it tell about the author’s results? Would they expect an increasing variance in case of the monsoon, and why (not)? As autocorrelation and variance do increase together before termination II, where is the problem?

We have amended this line to remove confusion (lines 120-125).

The test for trends in Kendall’s Tau seem to be done via surrogate time series, which I think is a good idea. But it seems that the surrogate time series have no autocorrelation because it is destroyed by the shuffling. The true data is autocorrelated and thus trends are less robust. Wouldn’t the trend significance then be overestimated? The authors refer to Dakos et al. (2008), and the approach seems to correspond to their H0\_1 - one could instead use their Null-hypothesis 2 and/or 3, which take autocorrelation into account.

Importantly, a timeseries with an autocorrelation that remains around 0 and one that remains around 0.5 will have no effect on the value of the Kendall tau, since the tau value is calculated relatively. Thus, the fact that the autocorrelation is destroyed by the shuffling does not change the null model distribution (see lines 247-249). Furthermore, Table S2 of Dakos et al. 2008 shows the p values from each test under each null model, and in all but one of the original time series records, testing with null model 1 (random shuffling) gives the highest p values, meaning that in 7 out of the 8 cases it actually slightly underestimates the significance of the trend. The results are also mixed for their simulated records, suggesting that there is no real preference to which null model is chosen in this case. Figure S3 in Dakos et al. (2008) further shows that there are negligible differences from the null model distributions.

I have the impression the term “tipping point analysis” has been made up by the authors and is very vague. One could instead refer to particular steps in the statistical analysis by using established conventions. Moreover, “noise-induced transition” is not the right term for a random shift of the system into a different attractor basin. As far as I know the term does not refer to one particular event in a stationary time series but to the sudden change of a system’s long-term statistics when the noise level is changed. For example, see books and articles by Berglund, Gentz, Horsthemke and Lefever on this topic.

We use the term ‘tipping point analysis’ to refer to both the pre-processing and the measuring of the trends in autocorrelation and variance over a sliding window. By using ‘tipping point analysis’ as one of our sub-section headings, we feel that the explanation as to what this involves is clear.

We refer to noise-induced transitions in terms of the recent Achuis et al. (2012) *Phil Trans A*



paper, which refers to noise-induced tipping as ‘stochastic perturbations...which drive long-term climate variations’. We have included this reference and definition in our paper when we refer to noise-induced transitions (lines 109-113). There are several examples in the literature where noise-induced tipping is described in this way, e.g. Lenton (2011) *Nature Climate Change* describes noise-induced transitions as “short-term internal variability [which]...causes a large, nonlinear change in the system state without any change in forcing control”, and Ditlevsen and Johnson (2010) *GRL*, analyse the Dansgaard-Oeschger events and determine that these are “induced by stochastic fluctuations”.

I still think that some figures are not required, for example

Fig. 1: c, d;

Fig. 6 and 7: c, d.

We have removed panels 1c, 6c, 6d, 7c, 7d. However, we would like to keep panel 1d since we emphasize the fact that the data spans an entire glacial cycle, and finishes with Glacial Termination II, of which panel 1d (now 1c) provides good visual evidence.

Fig. 10: I suggest to use individual potential plots, or arrows between potentials and time periods in the record, or write the letter directly next to the line in the plot.

We have amended to add the letter directly next to the line in the plot.

The caption of Fig. 11 is incomprehensible to me.

We have reworded to increase clarity (lines 597-607).

1 **Early warnings and missed alarms for abrupt monsoon transitions**

2

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5

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13

14 **Abstract**

15 Palaeo-records from China demonstrate that the East Asian Summer Monsoon (EASM) is  
16 dominated by abrupt and large magnitude monsoon shifts on millennial timescales,  
17 switching between periods of high and weak monsoon rains. It has been hypothesised that  
18 over these timescales, the EASM exhibits two stable states with bifurcation-type tipping  
19 points between them. Here we test this hypothesis by looking for early warning signals of  
20 past bifurcations in speleothem  $\delta^{18}\text{O}$  records from Sanbao Cave and Hulu Cave, China,  
21 spanning the penultimate glacial cycle. We find that although there are increases in both  
22 autocorrelation and variance preceding some of the monsoon transitions during this period,  
23 it is only immediately prior to the abrupt monsoon shift at the penultimate deglaciation  
24 (Termination II) that statistically significant increases are detected. To supplement our data  
25 analysis, we produce and analyse multiple model simulations that we derive from these

26 data. We find hysteresis behaviour in our model simulations with transitions directly forced  
27 by solar insolation. However, signals of critical slowing down, which occur on the approach  
28 to a bifurcation, are only detectable in the model simulations when the change in system  
29 stability is sufficiently slow to be detected by the sampling resolution of the dataset. This  
30 raises the possibility that the early warning ‘alarms’ were missed in the speleothem data  
31 over the period 224-150 kyr and it was only at the monsoon termination that the change in  
32 the system stability was sufficiently slow to detect early warning signals.

Zoe Thomas 20/10/2015 14:37

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33  
34 **Keywords: Speleothem, monsoon, bifurcation, early warning signals, tipping point**

### 35 36 **1.1 Introduction**

37 The Asian Summer Monsoon directly influences over 60% of the world’s population (Wu et  
38 al., 2012) and yet the drivers of past and future variability remain highly uncertain  
39 (Levermann et al., 2009; Zickfeld et al., 2005). Evidence from radiometrically-dated East  
40 Asian speleothem records of past monsoon behaviour (Yuan et al., 2004) suggests that on  
41 millennial timescales, the EASM is driven by a 23 kyr precession cycle (Kutzbach, 1981;  
42 Wang et al., 2008), but also influenced by feedbacks in sea surface temperatures and  
43 changing boundary conditions including Northern Hemisphere ice volume (An, 2000; Sun  
44 et al., 2015). The abrupt nature of the monsoon behaviour (interpreted as a precipitation  
45 proxy from  $\delta^{18}\text{O}$  values from Chinese speleothem records; see Section 1.4) in comparison  
46 to the sinusoidal insolation forcing strongly implies that this response is non-linear (Figure  
47 1); whilst Northern Hemisphere Summer Insolation (NHSI) follows a quasi-sinusoidal  
48 cycle, the  $\delta^{18}\text{O}$  profile in speleothems exhibits a step function, suggesting the presence of  
49 threshold behaviour in the monsoon system (Schewe et al., 2012). Though the vulnerability  
50 of society has clearly changed, future abrupt monsoon shifts, whether caused by orbital or

Zoe Thomas 16/10/2015 15:37

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Zoe Thomas 16/10/2015 15:44

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62 | [anthropogenic forcing, are likely to have major devastating societal impacts \(Donges et al.,](#)  
63 | [2015\).](#)

64

65

66 | **Figure 1:** (a) Northern Hemisphere Summer Insolation (NHSI) at June 30°N (Berger &  
67 | Loutre, 1991) (grey),  $\delta^{18}\text{O}$  speleothem data from Sanbao Cave (Wang et al., 2008) (dark  
68 | blue), (b)  $\delta^{18}\text{O}$  speleothem data from Hulu Cave (Wang et al., 2001); speleothem MSH  
69 | (red), MSP (blue) and MSX (yellow), (c)  $\delta^{18}\text{O}$  per mille benthic carbonate (Lisiecki &  
70 | Raymo, 2005) (proxy for global ice volume) (purple).

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73 | A minimum conceptual model of the East Asian Summer Monsoon developed by Zickfeld  
74 | et al. (2005), stripped down by Levermann et al. (2009) and updated by Schewe et al.  
75 | (2012), shows a non-linear solution structure with thresholds for switching a monsoon  
76 | system between ‘on’ or ‘off’ states that can be defined in terms of atmospheric humidity –  
77 | in particular, atmospheric specific humidity over the adjacent ocean (Schewe et al., 2012).  
78 | Critically, if specific humidity levels pass below a certain threshold, for instance, as a result  
79 | of reduced sea surface temperatures, insufficient latent heat is produced in the atmospheric  
80 | column and the monsoon fails. This moisture-advection feedback allows for the existence of  
81 | two stable states, separated by a saddle-node bifurcation (Zickfeld et al., 2005) (although  
82 | interestingly, the conceptual models of Levermann et al. (2009) and Schewe et al. (2012)  
83 | are characterised by a single bifurcation point for switching ‘off’ the monsoon and an  
84 | arbitrary threshold to switch it back ‘on’). Crucially, the presence of a critical threshold at  
85 | the transition between the strong and weak regimes of the EASM means that early warning

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**Deleted:** in comparison to the sinusoidal insolation forcing strongly implies that this response is non-linear (Figure 1); whilst Northern Hemisphere Summer Insolation (NHSI) follows a quasi-sinusoidal cycle, the  $\delta^{18}\text{O}$  profile in speleothems exhibits a step function, suggesting the presence of threshold behaviour in the monsoon system (Schewe et al., 2012).

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**Deleted:** CO<sub>2</sub> (ppmv) from the Antarctic Vostok ice core (Petit et al., 1999) (black), (d)

97 signals related to ‘critical slowing down’ (Dakos et al., 2008; Lenton et al., 2012) could be  
98 detectable in suitable proxy records.

99

100 The aim of this study was twofold: (1) to test whether shifts in the EASM during the  
101 penultimate glacial cycle (Marine Isotope Stage 6) are consistent with bifurcational tipping  
102 points, and (2) if so, is it possible to detect associated early warning signals. To achieve  
103 this, we analyse two  $\delta^{18}\text{O}$  speleothem records from China, and construct a simple model  
104 that we derive directly from this data to test whether we can detect early warning signals of  
105 these transitions.

106

### 107 | **1.2 Detecting early warning signals**

108 We perform ‘tipping point analysis’ on both the  $\delta^{18}\text{O}$  speleothem records and on multiple  
109 simulations derived from our model. This analysis aims to find early warning signs of  
110 impending tipping points that are characterised by a bifurcation (rather than a noise-induced

111 | tipping, induced by stochastic fluctuations with no change in forcing control, or rate-

112 | dependent tipping, where a system fails to track a continuously changing quasi-static

113 | attractor e.g. (Ashwin et al., 2012)). These tipping points can be mathematically detected by  
114 looking at the pattern of fluctuations in the short-term trends of a time-series before the

115 transition takes place. A phenomenon called ‘critical slowing down’ occurs on the approach  
116 to a tipping point, whereby the system takes longer to recover from small perturbations

117 (Kleinen et al., 2003; Held & Kleinen, 2004; Dakos et al., 2008). This longer recovery rate  
118 causes the intrinsic rates of change in the system to decrease, which is detected as a short-

119 term increase in the autocorrelation or ‘memory’ of the time-series (Ives, 1995), often

120 | accompanied by an increasing trend in variance (Lenton et al., 2012). It has been

121 | theoretically established that autocorrelation and variance should both increase together

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125 | (Ditlevsen & Johnsen, 2010; Thompson & Sieber, 2011). Importantly, it is the increasing  
126 | trend, rather than the absolute values of the autocorrelation and variance that indicate  
127 | critical slowing down. Detecting the phenomenon of critical slowing down relies on a  
128 | timescale separation, whereby the timescale forcing the system is much slower than the  
129 | timescale of the system's internal dynamics, which is in turn much longer than the  
130 | frequency of data sampling the system (Held & Kleinen, 2004). Importantly, the monsoon  
131 | transitions span hundreds of years (corresponding to several data points), meeting the  
132 | criterion that the frequency of sampling is higher than the timescale of the transition of the  
133 | system.

### 135 | **1.3 Missed alarms**

136 | Although efforts have been taken to reduce the chances of type I (incorrect rejection of a  
137 | true null hypothesis, otherwise known as a 'false positive') and type II (failure to reject a  
138 | false null hypothesis, or 'false negative') errors by correct pre-processing of data e.g.  
139 | (Lenton, 2011), totally eradicating the chances of false positive and false negative results  
140 | remains a challenge (Scheffer, 2010; Lenton et al., 2012; Dakos et al., 2014). Type II errors  
141 | or 'missed alarms', as discussed in Lenton (2011), may occur when internal noise levels are  
142 | such that the system is 'tipped' into a different state prior to reaching the bifurcation point,  
143 | precluding the detection of early warning signals. Type I errors are potentially easier to  
144 | guard against by employing strict protocols by which to reject a null hypothesis.

### 146 | **1.4 Using speleothem $\delta^{18}\text{O}$ data as a proxy of past monsoon strength**

147 | Highly-resolved ( $\sim 10^2$  years) and precisely dated speleothem records of past monsoonal  
148 | variability are well placed to test for early warning signals. The use of speleothem-based  
149 | proxies to reconstruct patterns of palaeo-monsoon changes has increased rapidly over recent

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153 decades with the development of efficient sampling and dating techniques. However, there  
154 is currently some debate surrounding the climatic interpretation of Chinese speleothem  $\delta^{18}\text{O}$   
155 records (An et al., 2015), which can be influenced by competing factors that affect isotope  
156 fractionation. The oxygen isotopic composition of speleothem calcite is widely used to  
157 reconstruct palaeohydrological variations due to the premise that speleothem calcite  $\delta^{18}\text{O}$   
158 records the stable isotopic content of precipitation, which has been shown to be inversely  
159 correlated with precipitation amount (Dansgaard, 1964; Lee & Swann, 2010), a relationship  
160 known as the ‘amount effect’. Although the  $\delta^{18}\text{O}$  of speleothem calcite in China has  
161 traditionally been used as a proxy for the ‘amount effect’ (Cheng et al., 2006; Wang et al.,  
162 2008; Cheng et al., 2009; Wang et al., 2009), this has been challenged by other palaeo-  
163 wetness proxies, notably Maher (2008), who argues that speleothems may be influenced by  
164 changes in rainfall source rather than amount. The influence of the Indian Monsoon has also  
165 been proposed as an alternative cause for abrupt monsoon variations in China (Liu et al.,  
166 2006; Pausata et al., 2011), though this has since been disputed (Wang & Chen, 2012; Liu  
167 et al., 2014). Importantly, however, robust replications of the same  $\delta^{18}\text{O}$  trends in  
168 speleothem records across the wider region suggest they principally represent changes in  
169 the delivery of precipitation  $\delta^{18}\text{O}$  associated with the EASM (Cheng et al., 2009; Cheng et  
170 al., 2012; Li et al., 2013; Duan et al., 2014; Liu et al., 2014; Baker et al., 2015).

171

172 Specific data requirements are necessary to search for early warning signs of tipping points  
173 in climate systems; not only does the data have to represent a measure of climate, it also  
174 must be of a sufficient length and resolution to enable the detection of critical slowing  
175 down. In addition, since time series analysis methods require interpolation to equidistant  
176 data points, a relative constant density of data points is important, so that the interpolation  
177 does not skew the data. The speleothem  $\delta^{18}\text{O}$  records that we have selected fulfil these

178 criteria, as described in more detail in section 2.1.

179

180

## 181 **2. Methods**

### 182 **2.1 Data selection**

183 We used the Chinese speleothem sequences from Sanbao Cave (31°40'N, 110°26'E) (Wang  
184 et al., 2008), and Hulu Cave (32°30'N, 119°10'E) (Wang et al., 2001) to search for early  
185 warning signals. Sanbao Cave (speleothem SB11) and Hulu Cave (speleothem MSP) have  
186 two of the highest resolution chronologies in the time period of interest, with a relatively  
187 constant density of data points, providing some of the best records of Quaternary-scale  
188 monsoonal variation. Speleothem  $\delta^{18}\text{O}$  records offer considerable advantages for  
189 investigating past changes in the EASM: their long duration ( $10^3$ - $10^4$  years), high-resolution  
190 (~100 years) and precise and absolute-dated chronologies (typically 1 kyr at  $1\sigma$ ), make  
191 them ideal for time series analysis. Speleothem SB11 has one of the longest, continuous  
192  $\delta^{18}\text{O}$  records in China, and is the only series spanning an entire glacial cycle without using a  
193 spliced record (Wang et al. 2008). Speleothem MSP has a comparable resolution and  
194 density to SB11, though is significantly shorter. Crucially, the cave systems lie within two  
195 regionally distinct areas (Figure 2), indicating that parallel changes in  $\delta^{18}\text{O}$  cannot be  
196 explained by local effects.

197

198

199 **Figure 2** Map showing the location of Sanbao and Hulu caves.

200

201

### 202 **2.2 Searching for bimodality**



203 A visual inspection of a histogram of the speleothem  $\delta^{18}\text{O}$  data was initially undertaken to  
204 determine whether the data are likely to be bimodal. We then applied a Dip-test of  
205 unimodality (Hartigan & Hartigan, 1985) to test whether our data is bimodal. To investigate  
206 further the dynamical origin of the modality of our data we applied non-stationary potential  
207 analysis (Kwasniok, 2013; Kwasniok, 2015). A non-stationary potential model (discussed  
208 in more detail in section 2.4) was fitted, modulated by the solar forcing (NHSI June  
209  $30^\circ\text{N}$ ), covering the possibility of directly forced transitions as well as noise-induced  
210 transitions with or without stochastic resonance.

211

212

### 213 **2.3 Tipping point analysis**

214 A search for early warning signals of a bifurcation at each monsoon transition was carried  
215 out between 224-128 kyr of the Sanbao Cave and Hulu Cave speleothem records. Stable  
216 periods of the Sanbao Cave  $\delta^{18}\text{O}$  record (e.g. excluding the abrupt transitions) were initially  
217 identified visually and confirmed by subsequent analysis using a climate regime shift  
218 detection method described by Rodionov (2004). Data pre-processing involved removal of  
219 long term trends using a Gaussian kernel smoothing filter and interpolation to ensure that  
220 the data is equidistant (a necessary assumption for time-series analysis), before the trends in  
221 autocorrelation and variance (using the R functions *acf()* and *var()* respectively) are  
222 measured over a sliding window of half the data length (Lenton et al., 2012). The density of  
223 data points over time do not change significantly in either record and thus the observed  
224 trends in autocorrelation are not an artefact of the data interpolation. The smoothing  
225 bandwidth was chosen such that long-term trends were removed without overfitting the  
226 data. A sensitivity analysis was undertaken by varying the size of the smoothing bandwidth  
227 and sliding window to ensure the results were robust over a range of parameter choices. The

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231 nonparametric Kendall's tau rank correlation coefficient was applied (Kendall, 1948; Dakos  
232 et al., 2008) to test for statistical dependence for a sequence of measurements against time,  
233 varying between +1 and -1, describing the sign and strength of any trends in autocorrelation  
234 and variance.

235

### 236 **2.3.1 Assessing significance**

237 The results were tested against surrogate time series to ascertain the significance level of the  
238 results found, based on the null hypothesis that the data are generated by a stationary  
239 Gaussian linear stochastic process. This method for assessing significance of the results is  
240 based on Dakos et al. (2012a). The surrogate time series were generated by randomising the  
241 original data over 1000 permutations, which is sufficient to adequately estimate the  
242 probability distribution of the null model, and destroys the memory while retaining the  
243 amplitude distribution of the original time series. The autocorrelation and variance for the  
244 original and each of the surrogate time series was computed, and the statistical significance  
245 obtained for the original data by comparing against the frequency distribution of the trend  
246 statistic (Kendall tau values of autocorrelation and variance) from the surrogate data.

247 Importantly, the Kendall tau values are calculated relatively, thus when the autocorrelation  
248 is destroyed by randomisation, the null model distribution does not change. Higher Kendall  
249 tau values indicate a stronger increasing trend. The 90<sup>th</sup> and 95<sup>th</sup> percentiles provided the  
250 90% and 95% rejection thresholds (or p-values of 0.1 and 0.05) respectively. According to  
251 the fluctuation-dissipation theorem (Ditlevsen & Johnsen, 2010), both autocorrelation and  
252 variance should increase together on the approach to a bifurcation. Previous tipping point  
253 literature has often used a visual increasing trend of autocorrelation and variance as  
254 indicators of critical slowing down. Although using surrogate data allows a quantitative  
255 assessment of the significance of the results, there is no consensus on what significance

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257 level is necessary to the declare the presence of precursors of critical slowing down. To  
258 guard against type I errors, we determine for this study that ‘statistically significant’ early  
259 warning indicators occur with increases in both autocorrelation and variance with p-values  
260 < 0.1. We have chosen this benchmark in line with previous studies using a similar null  
261 model that have described results with p<0.1 as ‘robust’ (Dakos et al., 2008; Boulton &  
262 Lenton, 2015).

263

#### 264 **2.4 Non-stationary potential analysis**

265 To supplement the analysis of the speleothem records and help interpret the results, a simple  
266 stochastic model derived directly from the Sanabo cave  $\delta^{18}\text{O}$  data was constructed. Non-  
267 stationary potential analysis (Kwasniok, 2013; Kwasniok, 2015) is a method for deriving  
268 from time series data a simple dynamical model which is modulated by external factors,  
269 here solar insolation. The technique allows extraction of basic dynamical mechanisms and  
270 to distinguish between competing dynamical explanations.

271

272 The dynamics of the monsoon system are conceptually described as motion in a time-  
273 dependent one-dimensional potential landscape; the influence of unresolved spatial and  
274 temporal scales is accounted for by stochastic noise. The governing equation is a one-  
275 dimensional non-stationary effective Langevin equation:

$$276 \quad \dot{x} = -V'(x; t) + \sigma\eta \quad (1)$$

277  $\eta$  is a white Gaussian noise process with zero mean and unit variance, and  $\sigma$  is the  
278 amplitude of the stochastic forcing. The potential landscape is time-dependent, modulated  
279 by the solar insolation:

$$280 \quad V(x; t) = U(x) + \gamma I(t)x \quad (2)$$

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282 The time-independent part of the potential is modelled by a fourth-order polynomial,  
283 allowing for possible bi-stability (Kwasniok & Lohmann, 2009):

$$U(x) = \sum_{i=1}^4 a_i x^i \quad (3)$$

284  
285  $I(t)$  is the insolation forcing and  $\gamma$  is a coupling parameter. The modulation of the potential  
286 is only in the linear term, that is, the time-independent potential system is subject to the  
287 scaled insolation forcing  $\gamma I(t)$ . The model variable  $x$  is identified with the speleothem  
288 record. The insolation is represented as a superposition of three main frequencies as

$$I(t) = \alpha_0 + \sum_{i=1}^3 [\alpha_i \cos(2\pi t/T_i) + \beta_i \sin(2\pi t/T_i)] \quad (4)$$

289  
290 with time  $t$  measured in kyr. The expansion coefficients  $\alpha_i$  and  $\beta_i$  are determined by least-  
291 squares regression on the insolation time series over the time interval of the speleothem  
292 record. The periods  $T_i$  are found by a search over a grid with mesh size 0.5kyr. They are, in  
293 order of decreasing contribution  $\alpha_i^2 + \beta_i^2$ ,  $T_1 = 23\text{kyr}$ ,  $T_2 = 19.5\text{kyr}$  and  $T_3 = 42\text{kyr}$ . This  
294 yields an excellent approximation of the insolation time series over the time interval under  
295 consideration here.

296

297 The potential model covers and allows to us distinguish between two possible scenarios: (i)

298 In the bifurcation scenario, the monsoon transitions are directly forced by the insolation,

299 where two states are stable in turn, one at a time. This corresponds to a fairly large value of

300  $\gamma$ . (ii) Alternatively, two stable states could be available at all times with noise-induced

301 switching between them. This is realised with  $\gamma = 0$ , giving a stationary potential. The

302 height of the potential barrier separating the two states could be modulated by the

303 insolation, possibly giving rise to a stochastic resonance which would explain the high

304 degree of coherence between the solar forcing and the monsoon transitions. The latter

305 variant would correspond to a small but non-zero value of  $\gamma$ .

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309

310 The shape of the potential, as well as the noise level, are estimated directly from the  
311 speleothem data according to the maximum likelihood principle. We take a two-step  
312 approach, combining non-stationary probability density modelling (Kwasniok, 2013) and  
313 dynamical modeling (Kwasniok, 2015). The shape of the potential is estimated from the  
314 probability density of the data. The quasi-stationary probability density of the potential  
315 model is

$$p(x; t) = Z^{-1}(t) \exp[-2V(x; t)/\sigma^2] \quad (5)$$

316

317 with a time-dependent normalisation constant  $Z(t)$ . The coefficients  $a_i$  and the coupling  
318 constant  $\gamma$  are estimated by maximising the likelihood function

$$L(x_1, \dots, x_N) = \prod_{i=1}^N p(x_i; t_i) \quad (6)$$

319

320 as described in Kwasniok (2013). The size of the data set is  $N=1288$ . This leaves the noise  
321 level undetermined as a scaling of the potential with a constant  $c$  and a simultaneous scaling  
322 of the noise variance with  $c$  keeps the quasi-stationary probability density unchanged. We  
323 set  $\sigma = 1$  for the (preliminary) estimation of  $a_i$  and  $\gamma$ . The noise level is now determined  
324 from the dynamical likelihood function based on the time evolution of the system  
325 (Kwasniok, 2015). The Langevin equation is discretised according to the Euler-Maruyama  
326 scheme:

$$x_{n+1} = x_n - \delta t_n V'(x_n; t_n) + \sqrt{\delta t_n} \sigma \eta_n \quad (7)$$

327

328 The sampling interval of the data is  $\delta t_n = t_{n+1} - t_n$ . The log-likelihood function of the  
329 data is

$$l(x_1, \dots, x_N | x_0) = -\frac{N}{2} \log 2\pi - N \log \sigma - \frac{1}{2} \sum_{n=0}^{N-1} \left( \log \delta t_n + \frac{[x_{n+1} - x_n + \delta t_n V'(x_n; t_n)]^2}{\delta t_n \sigma^2} \right) \quad (8)$$

330

331 The scaling constant  $c$  is searched on a grid with mesh size 0.01 and the log-likelihood  
332 maximised, giving the final estimates of all parameters. Both estimation procedures are  
333 applied directly to the unevenly sampled data without any prior interpolation. We remark  
334 that the more natural and simpler approach of estimating all parameters simultaneously  
335 from the dynamical likelihood (Kwasniok, 2015) here yields a negative leading-order  
336 coefficient  $a_4$  and thus the model cannot be integrated over a longer time period without the  
337 trajectory escaping to infinity. This possibly points at limitations in the degree of validity of  
338 the one-dimensional potential model. Palaeoclimatic records reflect a multitude of complex  
339 processes and any model as simple as [equation \(1\)](#) cannot be expected to be more than a  
340 skeleton model [used to pinpoint and contrast basic dynamical mechanisms](#). The described  
341 estimation method guarantees a positive leading-order coefficient  $a_4$  and therefore a  
342 globally stable model.

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344 It has been suggested that the EASM system responds specifically to 21<sup>st</sup> July insolation at  
345 [65°N](#) with a “near-zero phase lag” (Ruddiman, 2006). However, given that EASM  
346 development is affected by both remote and local insolation forcing (Liu et al., 2006), we  
347 use an insolation latitude local to the Sanbao Cave record, consistent with earlier studies  
348 from this and other speleothem sequences (Wang et al., 2001). Since the monthly maximum  
349 insolation shifts in time with respect to the precession parameter, the 30°N June insolation  
350 was used, though we acknowledge that the insolation changes of 65°N 21 July as used by  
351 Wang et al. (2008) are similar with regard to the timing of maxima and minima. Crucially,  
352 immediately prior to Termination II, the Chinese speleothem data (including Sanbao Cave)  
353 record a ‘Weak Monsoon Interval’ between 135.5 and 129 [kyr](#) (Cheng et al., 2009),  
354 suggesting a lag of approximately 6.5 kyrs following Northern Hemisphere summer  
355 insolation (Figure 1).

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360 Having derived a model from the data, 100 realisations were analysed to test whether early  
361 warning signals could be detected in the model output, using the methods set out in section  
362 2.3. We initially chose the sampling resolution of the model outputs to be comparable to the  
363 speleothem data ( $10^2$  years). Subsequently, the model was manipulated by changing both  
364 the noise level and the sampling resolution in order to explore the effect of these on the  
365 early warning signals in a hypothetical scenario. To enable a straightforward comparison of  
366 the rate of forcing and the sampling resolution we linearized the solar insolation using the  
367 minimum and maximum values of the solar insolation over the time span of the model (224-  
368 128 kyr). This approach was preferred rather than using a sinusoidal forcing since early  
369 warning signals are known to work most effectively when there is a constant increase in the  
370 forcing. To detrend the time series data, we ran the model without any external noise  
371 forcing to obtain the equilibrium solution to the system, which we then subtracted from the  
372 time series, which did include noise. In addition, we manipulated the noise level of the  
373 model by altering the amplitude of the stochastic forcing ( $\sigma$  in Equation 1). The time step in  
374 the series was reduced so that 6000 time points were available prior to the bifurcation and to  
375 ensure no data from beyond the tipping point was included in the analysis. Sampling the  
376 same time series at different resolutions allowed us to explore the effect of this on the early  
377 warning signals. When comparing early warning signals for differing sample steps and  
378 noise levels, the same iteration of the model was used to enable a direct comparison.

379

### 380 3. Results

#### 381 3.1 Bimodality and non-stationary potential modelling

382 A histogram of  $\delta^{18}\text{O}$  values suggests there are two modes in the EASM between 224-128  
383 kyr, as displayed by the double peak structure in Figure 3a, supporting a number of studies

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394 that observe bimodality in tropical monsoon systems (Zickfeld et al., 2005; Schewe et al.,  
395 2012). We also apply a Dip-test of unimodality (Hartigan & Hartigan, 1985) and find that  
396 our null hypothesis of unimodality is rejected ( $D=0.018$ ,  $p=0.0063$ ) and thus our data is at  
397 least bimodal. To investigate further the dynamical origin of this bimodality we  
398 applied non-stationary potential analysis (Kwasniok, 2013; Kwasniok, 2015). This showed  
399 a bi-stable structure to the EASM with hysteresis (Figure 3b, c), suggesting that abrupt  
400 monsoon transitions may involve underlying bifurcations. The monsoon transitions appear  
401 to be predominantly directly forced by the insolation. There is a phase in the middle of the  
402 transition cycle between the extrema of the insolation where two stable states are available  
403 at the same time but this phase is too short for noise-induced switches to play a significant  
404 role.

405  
406 We are able to clearly refute from the speleothem data the scenario of noise-induced  
407 switching between two simultaneously available states in favour of the bifurcation scenario.  
408 When fitting a model without solar insolation forcing (that is,  $\gamma = 0$ ) we obtain a stationary  
409 potential with two deep wells and noise-driven switching between them. However, the pdf-  
410 based log-likelihood of equation (6) is  $l = -2149.1$  versus  $l = -1943.2$  for the model with  
411 insolation forcing and the dynamical log-likelihood of equation (8) is  $l = -353.6$  versus  $l = -$   
412 346.6. This provides very strong evidence for the bifurcation scenario; based on both  
413 likelihood functions, both the Akaike and the Bayesian information criterion clearly prefer  
414 the model with solar insolation forcing. The value of  $\gamma$  is fairly large and the stationary part  
415 of the potential is not strongly bistable, as evidence by the shape of the potential given in  
416 Figure 3, ruling out the stochastic resonance scenario. The uncertainty in all parameters,  
417 including the noise level, is very small, making our model estimation robust. We tried more  
418 complicated models where also the higher-order terms in the potential are modulated by the



419 insolation rather than just the linear term or where the solar insolation enters nonlinearly  
420 into the model; the gain in likelihood is found to be rather minor compared to the gain  
421 achieved when adding the modulation in the linear term of the potential.

422

423

424 **Figure 3** (a) Histogram showing the probability density of the speleothem data aggregated

425 over 224-128 kyr. (b) Bifurcation diagram obtained from potential model analysis, showing

426 bi-stability and hysteresis. Solid black lines indicate stable states, dotted line unstable states,

427 and dashed vertical lines the jumps between the two stable branches. Coloured vertical lines

428 correspond to the insolation values for which the potential curve is shown in panel c; (c)

429 Shows how the shape of the potential well changes over one transition cycle (198-175 kyr)

430 (green long dash = 535 W/m<sup>2</sup>, purple short dash = 531 W/m<sup>2</sup>, blue solid = 490 W/m<sup>2</sup>, red

431 dotted = 449 W/m<sup>2</sup>) (for more details see Figure 10).

432

433

### 434 3.2 Tipping point analysis

435 We applied tipping point analysis on the Sanbao Cave  $\delta^{18}\text{O}$  record on each section of data

436 prior to a monsoon transition. Although autocorrelation and variance do increase prior to

437 some of the abrupt monsoon transitions (Figure 4), these increases are not consistent

438 through the entire record. Surrogate datasets used to test for significance of our results

439 showed that p-values associated with these increases are only  $<0.1$  for both autocorrelation

440 and variance (Figure 5) in one instance. Although a visual increasing trend has been used in

441 previous literature as an indicator of critical slowing down, we choose more selective

442 criteria to guard against the possibility of false positives.

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449 **Figure 4** a)  $\delta^{18}\text{O}$  speleothem data from Sanbao Cave (SB11) (blue line) and NHSI at July  
450 65°N (grey line). Grey hatched areas show the sections of data selected for tipping point  
451 analysis. b) Autocorrelation and variance for each period prior to a transition.

452

453

454 **Figure 5** Histogram showing frequency distribution of Kendall tau values from 1000  
455 realisations of a surrogate time series model (described in Section 2.3.1), for Sanbao Cave  
456 (a, b) and Hulu Cave (c, d)  $\delta^{18}\text{O}$  data. The grey dashed lines indicate the 90% ( $p < 0.1$ ) and  
457 95% ( $p < 0.05$ ) significance level. Each coloured line denotes the Kendall tau values for  
458 autocorrelation and variance, for each section of speleothem data analysed (red = 131-156  
459 kyr; yellow = 166-177 kyr; purple = 180-189 kyr; green = 191-198 kyr; orange = 200-208  
460 kyr; blue = 214-225 kyr).

461

462

463 The only section of data prior to a monsoon transition that sees p-values of  $< 0.1$  for the  
464 increases in both autocorrelation and variance is for the data spanning the period 150 to 129  
465 kyr in the Sanbao Cave record, before Monsoon Termination II (Figure 6). We find that the  
466 Kendall tau value for autocorrelation has a significance level of  $p < 0.05$  and for variance a  
467 significance level of  $p < 0.1$  (Figure 5a and 5b). These proportional positive trends in both  
468 autocorrelation and variance are consistent with critical slowing down on the approach to a  
469 bifurcation (Ditlevsen & Johnsen, 2010).

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472 **Figure 6** Tipping Point analysis on data from Sanbao Cave (Speleothem SB11) ( $31^{\circ}40'\text{N}$ ,

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**Deleted:** Figure 6c illustrates the density of data points before and after interpolation, showing that this pre-processing is unlikely to have biased the results.

481 110°26'E). (a) Data was smoothed over an appropriate bandwidth (purple line) to produce  
482 data residuals (b), and analysed over a sliding window (of size between the two grey  
483 vertical lines). The grey vertical line at 131 ka BP indicates the tipping point, and the point  
484 up to which the data is analysed. (d) AR(1) values and associated Kendall tau value, and (e)  
485 displays the variance and associated Kendall tau value.

487 To test whether the signal is present in other EASM records, we undertook the same  
488 analysis on a second speleothem sequence of comparable age (Figure 7). We find that  
489 speleothem MSP from Hulu Cave (32°30'N, 119°10'E) (Wang et al., 2001) displays a  
490 comparable increase in autocorrelation and variance to speleothem SB11 from Sanbao  
491 Cave, though these do display slightly lower p-values (Figure 5c and 5d).

493  
494 **Figure 7** Tipping Point analysis on data from Hulu Cave (Speleothem MSP) (32°30' N,  
495 119°10' E) (a) Data was smoothed over an appropriate bandwidth (purple line) to produce  
496 data residuals (b), and analysed over a sliding window (of size between the two grey  
497 vertical lines). The grey vertical line at 131 ka BP indicates the tipping point, and the point  
498 up to which the data is analysed. (d) Autocorrelation values and associated Kendall tau  
499 value, and (e) the variance and associated Kendall tau value.

501  
502 Furthermore, a sensitivity analysis was performed (results shown for data preceding the  
503 monsoon termination in both speleothem SB11 and MSP, Figure 8) to ensure that the  
504 results are robust over a range of parameters by running repeats of the analysis with a range  
505 of smoothing bandwidths used to detrend the original data (5-15% of the time series length)

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519 and sliding window sizes in which indicators are estimated (25-75% of the time series  
520 length). The colour contours show how the Kendall tau values change when using different  
521 parameter choices; for the autocorrelation at Sanbao Cave the Kendall tau values are over  
522 0.8 for the vast majority of smoothing bandwidth and sliding window sizes (Figure 8a),  
523 indicating a robust analysis.

524

525

526 **Figure 8** Contour plots showing a range of window and bandwidth sizes for the analysis;  
527 (a) Sanbao SB11 autocorrelation, (b) Sanbao SB11 variance, (c) Hulu MSP autocorrelation,  
528 (d) Hulu MSP variance. Black stars indicate the parameters used for the analysis in Figures  
529 6 and 7.

530

531

### 532 **3.3 Potential model simulations**

533 To help interpret these results we applied our potential model. In the model we find  
534 transitions occur under direct solar insolation forcing when reaching the end of the stable  
535 branches, explaining the high degree of synchronicity between the transitions and solar  
536 forcing. The initial 100 realisations produced from our potential model appear broadly to  
537 follow the path of June insolation at 30°N with a small phase lag (Figure 9). The model  
538 simulations also follow the speleothem palaeodata for all but the monsoon transition at 129  
539 ka BP near Termination II, where the model simulations show no extended lag with respect  
540 to the insolation. Again it has to be kept in mind that the potential model as a skeleton  
541 model can only be expected to qualitatively reproduce the main features of the data.  
542 Actually observing the speleothem record as a realisation of the model will always be  
543 highly unlikely with any model as simple as the present one.

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548 **Figure 9** Probability range of 100 model simulations, with the June 30°N NHSI (in red),

549 and the palaeodata from SB11 (in green).

550

551

552 No consistent early warning signals were found in the initial 100 model simulations during

553 the period 224-128 kyr. In order to detect critical slowing down on the approach to a

554 bifurcation, the data must capture the gradual flattening of the potential well. We suggest

555 that early warning signals were not detected due to a relatively fast rate of forcing compared

556 to the sampling of the system; this comparatively poor sampling prevents the gradual

557 flattening of the potential well from being recorded in the data; a feature common to many

558 palaeoclimate datasets. Figure 10 illustrates the different flattening of the potential well

559 over a transition cycle during the glacial period and over the transition cycle at the

560 termination. There is more visible flattening in the potential at the termination, as seen in

561 panel (c), which is thought to be due to the reduced amplitude of the solar forcing at the

562 termination. The distinction between these two transitions cycles helps to explain why early

563 warning signals in the form of increasing autocorrelation and variance are found

564 immediately preceding the termination, but not for the other monsoon transitions.

565

566

567 **Figure 10** Potential analysis from the Sanabo  $\delta^{18}\text{O}$  data showing the changing shape of the

568 potential well over (b) a transition cycle during the glacial period (198-175 kyr); and (c) the

569 transition cycle at the termination (150-128.5 kyr). Dotted lines show stages of the

570 transition over high, medium, and low insolation values, as depicted in panel (a).

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579 To test the effect on the early warning signals of the sampling resolution of the model, we  
 580 compared a range of different sampling time steps in the model (see section 2.4) measuring  
 581 the Kendall tau values of autocorrelation and variance over each realisation of the model  
 582 (one realisation displayed in Figure 11), which demonstrates the effects of increasing the  
 583 sampling time step in the model. We found that whereas an increasing sampling time step  
 584 produces a steady decrease in the Kendall tau values for autocorrelation (Figure 11b),  
 585 Kendall tau values remain fairly constant for variance (Figure 11c), suggesting that the  
 586 latter is not affected by time step changes. This supports the contention by Dakos et al.  
 587 (2012b) that ‘high resolution sampling has no effect on the estimate of variance’. In  
 588 addition, we manipulated the noise level and found that decreasing the noise level by a  
 589 factor of 2 was necessary to identify consistent early warning signals. This is illustrated in  
 590 Figure 11a, where the grey line represents the noise level as determined by the model,  
 591 which does not follow a step transition, and cannot be adequately detrended by the equation  
 592 derived from the model. However, once the noise level is sufficiently reduced, early  
 593 warning signals (displayed here as high Kendall tau values for autocorrelation and variance)  
 594 can be detected.

595

596

597 **Figure 11** a) Example of single realisation of the approach to a bifurcation from our  
 598 potential model, which has been generated using 4 different noise levels (original noise =  
 599 grey, 0.5 noise = black, 0.2 noise = blue, 0.1 noise = green). Tipping point analysis was  
 600 applied on each realisation, where the red line depicts the detrending line and the grey  
 601 dashed vertical line is the cut-off point where data is analysed up to; distribution of Kendall

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606 tau values for (a) autocorrelation and (b) variance over increasing sample step and differing  
607 noise levels.

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Deleted: ; c) distribution of Kendall tau values for variance over increasing sample step.

#### 610 4. Discussion

611 It is important to note here that although the detection of early warning signals in time  
612 series data has been widely used for the detection of bifurcations in a range of systems  
613 (Dakos et al., 2008), there are instances when critical slowing down cannot be  
614 detected/recorded prior to a bifurcation. First is the assumption that the abrupt monsoon  
615 shifts are characterised by a bifurcation, rather than noise-induced tipping or stochastic  
616 resonance. The bifurcation hypothesis is supported by previous studies (Zickfeld et al.,  
617 2005; Levermann et al., 2009; Schewe et al., 2012) as well as our potential model, which  
618 selects a bifurcation as the most likely scenario (whilst considering noise-induced tipping  
619 and stochastic resonance). In a noise-induced tipping or stochastic resonance scenario, no  
620 early warning signals would be expected since there would be no gradual change in the  
621 stability of the system (Lenton, 2011). Even within the bifurcation scenario, it is possible  
622 that early warning signals may not be detected, due to external dynamics of the system, such  
623 as a high level of stochastic noise, or when there is an insufficient sampling resolution. The  
624 results illustrated in Figure 11 confirm that early warning signals may not be detected for  
625 bifurcations if the rate of forcing is too fast compared to the sampling rate, such that the  
626 flattening of the potential is poorly recorded in time series; Figure 11c clearly illustrates the  
627 detrimental effect of a lower resolution on Kendall tau values, particularly for  
628 autocorrelation. 'Missed alarms' may therefore be common in palaeodata where there is an  
629 insufficient sampling resolution to detect the flattening of the potential; a high sampling  
630 resolution is thus recommended to help avoid this issue. There is more flattening visible in

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637 the potential for the monsoon transition at 129 ka BP (Termination II), which is due to the  
638 reduced amplitude of the orbital forcing at the termination, but it is unclear whether this is  
639 sufficient to explain the early warming signal detected in the palaeodata. We suggest that  
640 additional forcing mechanisms may be driving the termination e.g. (Caley et al., 2011)  
641 which cannot be captured by the potential model (as evidenced by the trajectory of the data  
642 falling outside the probability range of the potential model (Figure 9)).

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644 One possible reason for the detection of a critical slowing down immediately prior to the  
645 termination (129 ka BP) is a change in the background state of the climate system.

646 Termination II is preceded by a Weak Monsoon Interval (WMI) in the EASM at 135.5-129

647 kyr (Cheng et al., 2009), characterised by the presence of a longer lag between the change  
648 in insolation and the monsoon transition. The WMI is thought to be linked to migrations in

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649 the Inter-tropical Convergence Zone (ITCZ) (Yancheva et al., 2007). Changes in the  
650 latitudinal temperature gradient (Rind, 1998) or planetary wave patterns (Wunsch, 2006)  
651 driven by continental ice volume (Cheng et al., 2009) and/or sea ice extent (Broccoli et al.,  
652 2006) have been suggested to play a role in causing this shift in the ITCZ. For instance, the  
653 cold anomaly associated with Heinrich event 11 (at 135 ka BP) has been invoked as a  
654 possible cause of the WMI, cooling the North Atlantic and shifting the Polar Front and  
655 Siberian High southwards, forcing an equatorward migration of westerly airflow across  
656 Asia (Broecker et al., 1985; Cheng et al., 2009; Cai et al., 2015). Such a scenario would  
657 have maintained a low thermal gradient between the land and sea, causing the Weak  
658 Monsoon Interval and potentially suppressing a simple insolation response. The implication  
659 is that during the earlier monsoon transitions in Stage 6, continental ice volume and/or sea-  
660 ice extent was less extensive than during the WMI, allowing the solar insolation response to  
661 dominate.



664

665

## 666 **5. Conclusions**

667 We analysed two speleothem  $\delta^{18}\text{O}$  records from China over the penultimate glacial cycle as  
668 proxies for the past strength of the EASM to test whether we could detect early warning  
669 signals of the transitions between the strong and weak regimes. After determining that the  
670 data was bimodal, we derived a non-stationary potential model directly from this data  
671 featuring a fold bifurcation structure. We found evidence of critical slowing down before  
672 the abrupt monsoon shift at Termination II (129 ka BP) in the speleothem  $\delta^{18}\text{O}$  data.

673 However, we do not find consistent early warning signals of a bifurcation for the abrupt  
674 monsoon shifts in the period between 224-150 kyr, which we term ‘missed alarms’.

675 Exploration of sampling resolution from our model suggests that the absence of robust  
676 critical slowing down signals in the palaeodata is due to a combination of rapid forcing and  
677 the insufficient sampling resolution, preventing the detection of the steady flattening of the  
678 potential that occurs before a bifurcation. We also find that there is a noise threshold at  
679 which early warning signals can no longer be detected. We suggest that the early warning  
680 signal detected at Termination II in the palaeodata is likely due to the longer lag during the  
681 Weak Monsoon Interval, linked to cooling in the North Atlantic. This allows a steadier  
682 flattening of the potential associated with the stability of the EASM and thus enables the  
683 detection of critical slowing down. Our results have important implications for identifying  
684 early warning signals in other natural archives, including the importance of sampling  
685 resolution and the background state of the climate system (full glacial versus termination).  
686 In addition, it is advantageous to use archives which record multiple transitions, rather than  
687 a single shift, such as the speleothem records reported here; the detection of an early  
688 warning signal during one transition compared to previous events in the same record

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690 provides an insight into changing/additional forcing mechanisms.

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818

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823 [http://hurricane.ncdc.noaa.gov/pls/paleox/f?p=519:1:::P1\\_STUDY\\_ID:8641](http://hurricane.ncdc.noaa.gov/pls/paleox/f?p=519:1:::P1_STUDY_ID:8641) and Hulu:

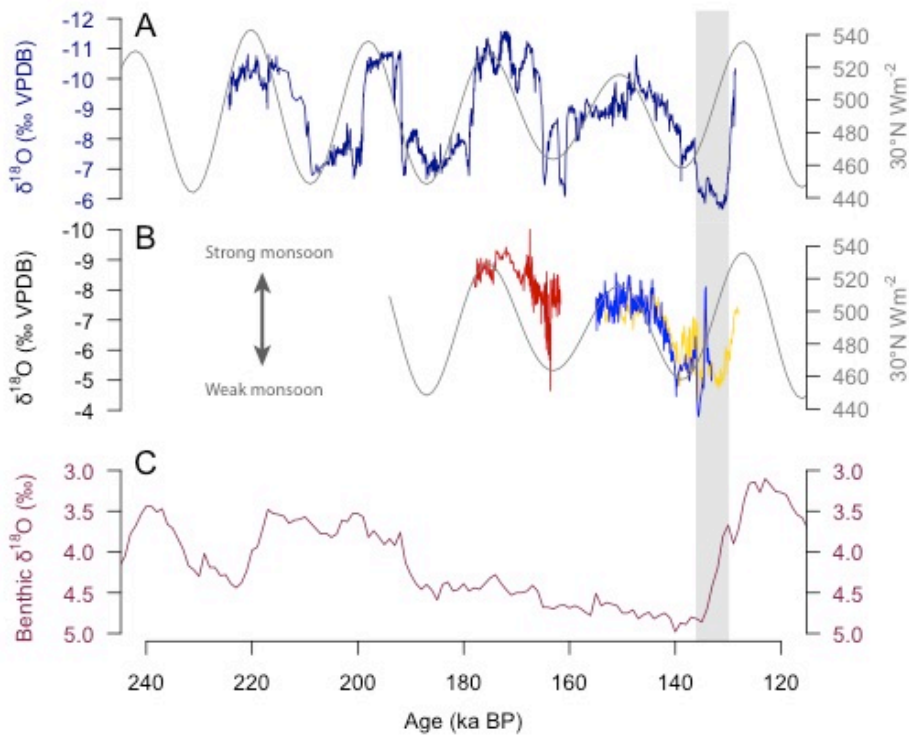
824 [http://hurricane.ncdc.noaa.gov/pls/paleox/f?p=519:1:::P1\\_STUDY\\_ID:5426](http://hurricane.ncdc.noaa.gov/pls/paleox/f?p=519:1:::P1_STUDY_ID:5426))

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826 **Competing financial interests**

827 The authors declare no competing financial interests.

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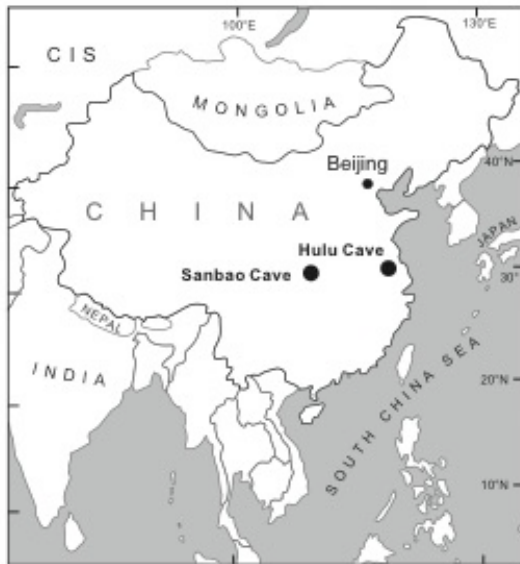
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831 Figure 1

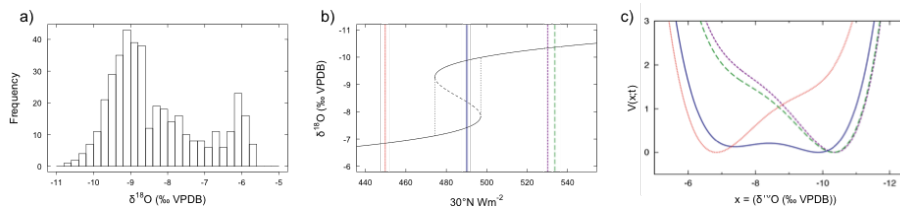
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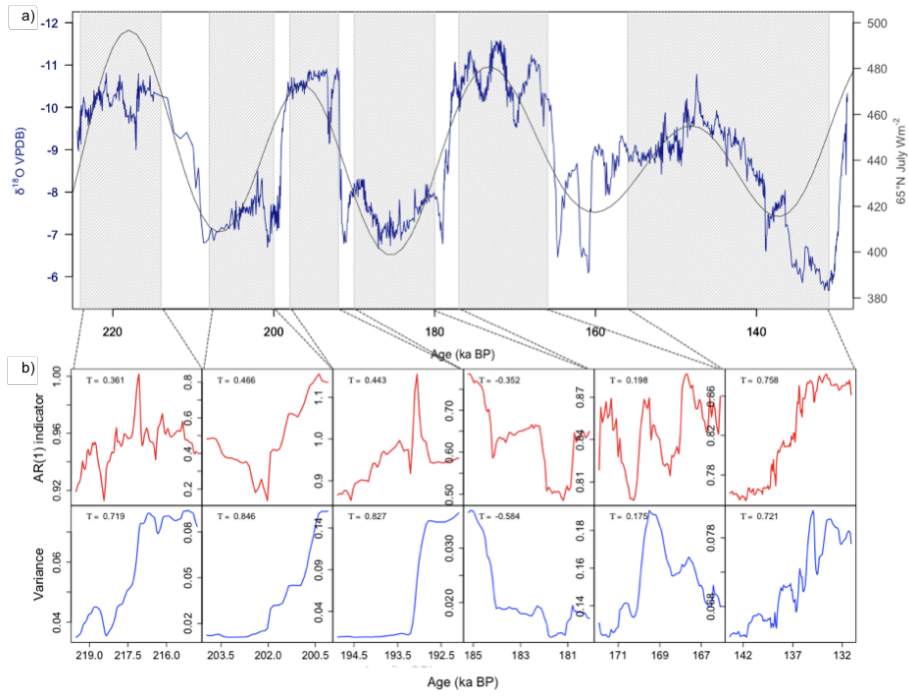
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833 Figure 2



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835 Figure 3



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837 Figure 4

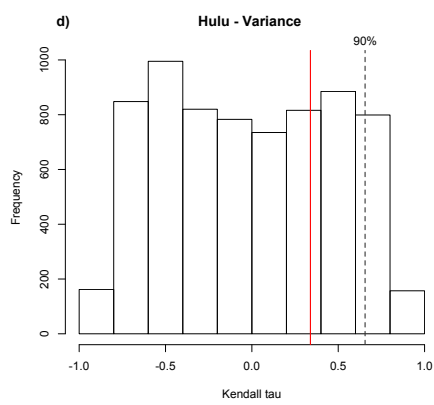
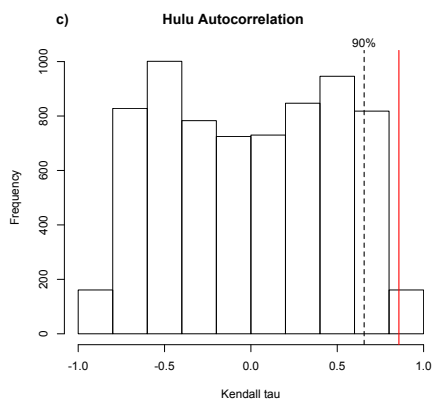
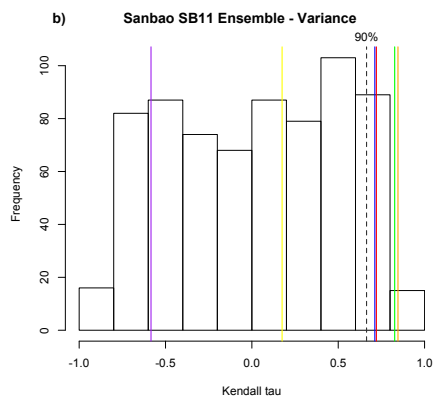
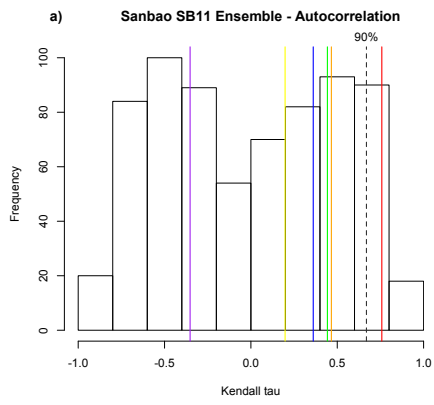
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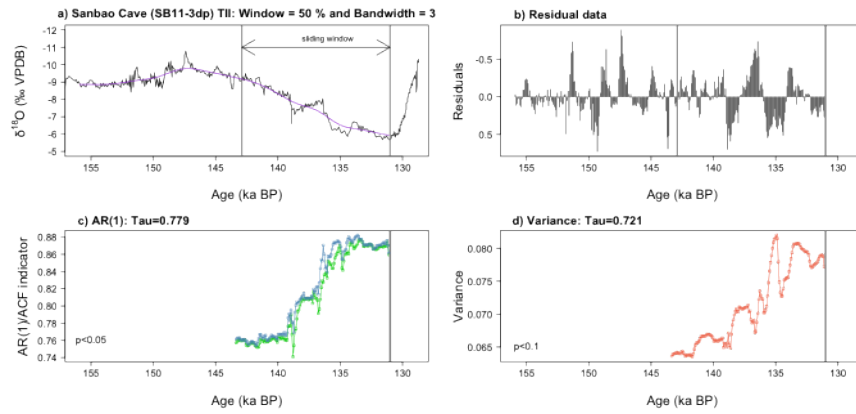
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844 Figure 5

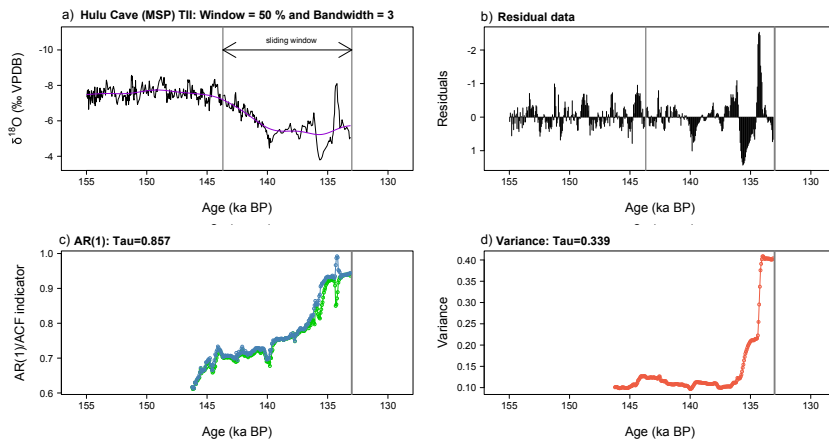
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847 Figure 6

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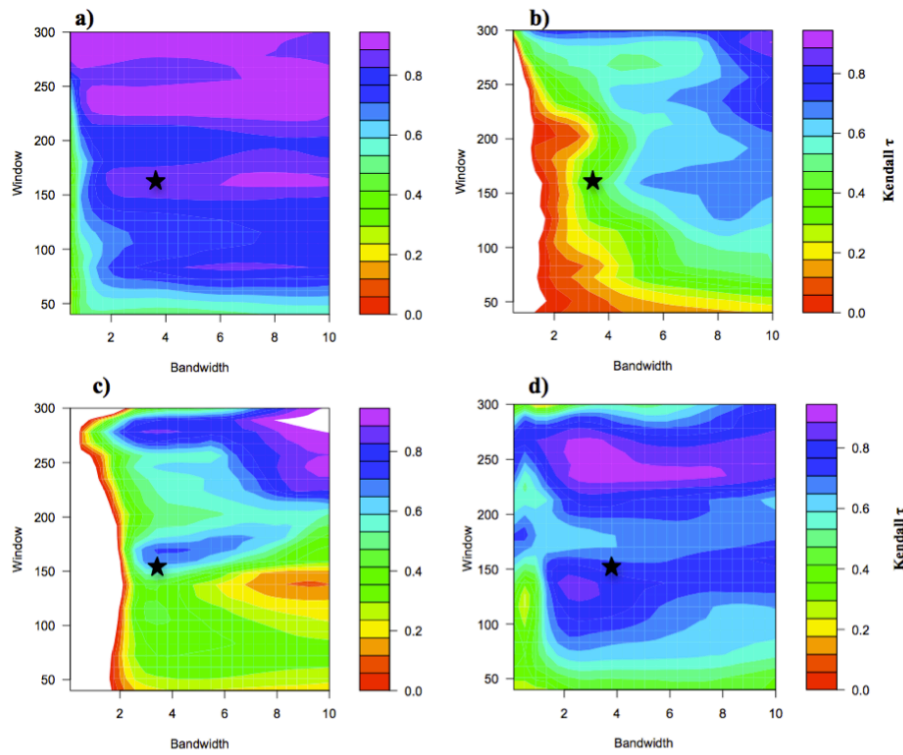
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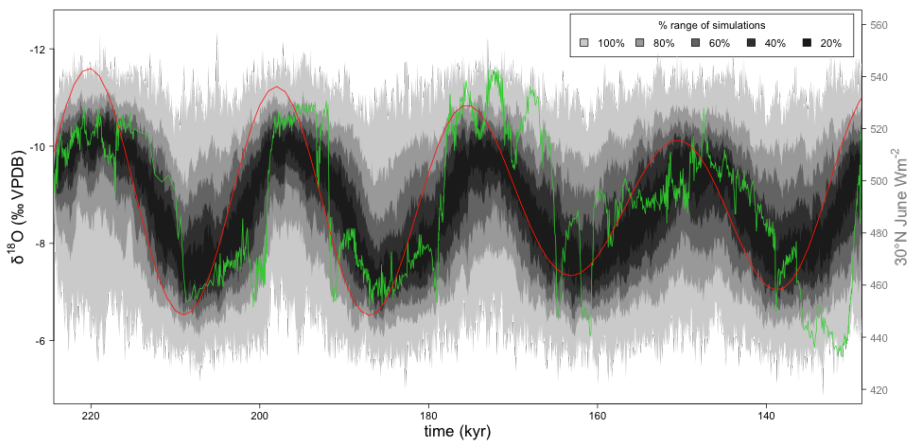
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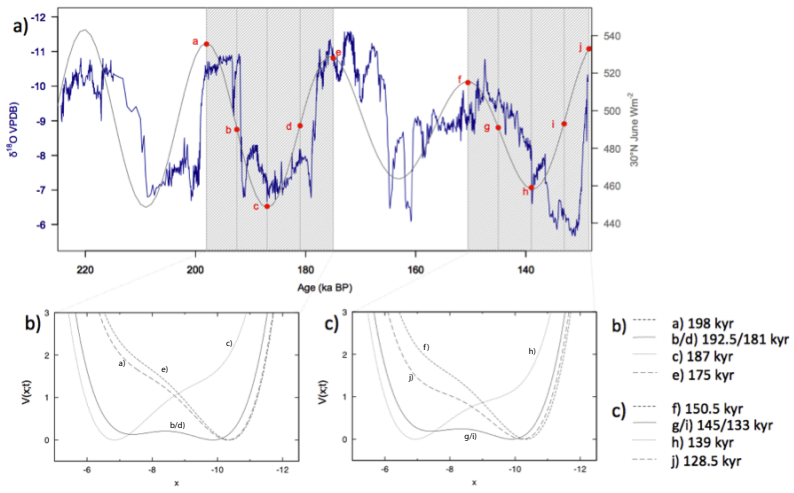
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852 Figure 8



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854 Figure 9

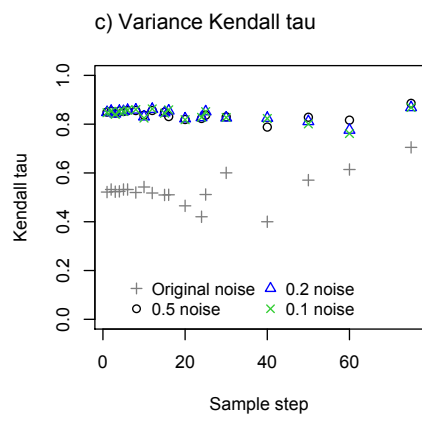
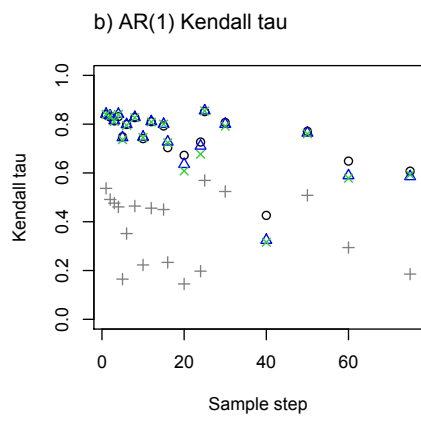
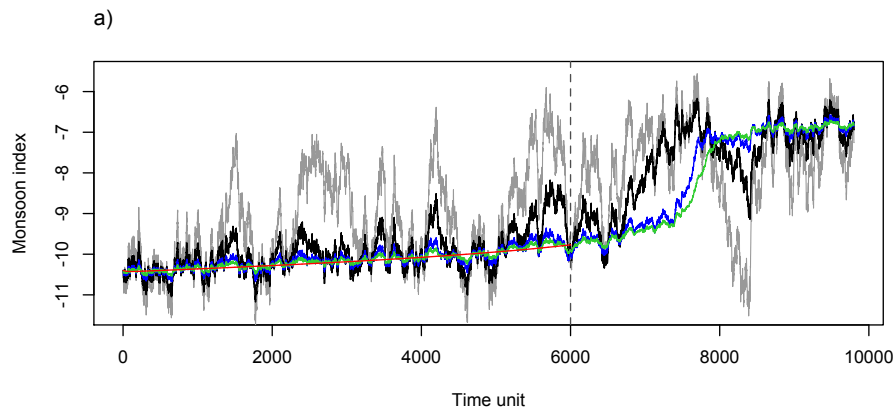


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856 Figure 10



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858 Figure 11

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