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# Geothermal evidence of the Late Pleistocene-Holocene orbital forcing (example from the Urals, Russia)

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## Abstract

We use early obtained in the Middle Urals geothermal reconstruction of the ground surface temperature (GST) history to determine the surface heat flux (SHF) history over the past 35 kyr. A new algorithm of GST-SHF transformation was applied to solve this problem. The time scale of geothermal reconstructions has been corrected by comparing the estimated heat flux and annual insolation at the latitude of 60° N. The consistency of SHF and insolation changes on the interval 35–6 kyr BP (the linear correlation coefficient  $R = 0.99$ ) points to orbital factors as the main cause of climatic changes during the Pleistocene–Holocene transition. The amplitude of SHF variations is about 1.3% of the insolation changes amplitude. The increase of carbon dioxide concentrations lagged by 2–3 kyr from the SHF increase and occurred synchronously with GST changes.

## 1 Introduction

The role of orbital factors in Pleistocene climatic variations has been studied more than 100 years since Joseph Adhemar, James Croll and Milutin Milankovitch. A popular approach is comparing paleotemperatures reconstructed from proxy data (oxygen isotopes, palynological or others) with theoretically calculated insolation. Some investigators (Peixóto and Oort, 1984; Pielke, 2003; Douglass and Knox, 2012) criticized this approach. They noted that temperature field is not an optimal parameter for climate attribution, particularly for evaluation of climatic reaction on the external radiative forcing. There is a lag between external radiative flux and temperature changes, which is disappeared if we consider the heat content or the surface heat flux changes. The advantage of heat flux estimation over temperature one was not realized in full up to date. Wang and Bras (1999) proposed the integral relation to estimate surface heat flux (SHF) changes from ground surface temperature (GST) variations. A finite-difference approximation of the relation between the GST (represented by a piecewise linear

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where  $a = \frac{\lambda}{\rho C}$  is thermal diffusivity,  $\rho$  is density,  $C$  is specific heat capacity,  $i^n \operatorname{erfc}(\alpha)$  is the  $n$ th repeated integral of the error function of  $\alpha$  and  $\Gamma(\beta)$  is gamma-function of argument  $\beta$ . Differentiation of Eq. (3) yields SHF

$$q(0, t) = \frac{\Gamma\left(\frac{1}{2}n + 1\right)}{\Gamma\left(\frac{1}{2}n + \frac{1}{2}\right)} \cdot \frac{\lambda}{\sqrt{at}} \cdot T(0, t) \quad (4)$$

Note that the ratio  $E = \lambda/(a)^{-1/2}$  represents the rock's thermal effusivity (thermal inertia) characterizing the rate of heat exchange at the surface.

We approximate GST history by a sum of temperature changes corresponding to Eq. (2):

$$T_i = T_0 + \sum_{j=1}^i D_j (i - j + 1)^{\frac{n}{2}} \quad (5)$$

where  $i, j$  are positive integers related with the real time by the equations  $t = i \cdot \Delta t$ ,  $t = j \cdot \Delta t$ ,  $\Delta t$  is uniform time interval. For each addend of this sum

$$T_i = D_i i^{n/2}, \quad q_i = k_n \frac{E}{\sqrt{\Delta t}} D_i i^{\frac{n-1}{2}}, \quad k_n = \frac{\Gamma\left(\frac{1}{2}n + 1\right)}{\Gamma\left(\frac{1}{2}n + \frac{1}{2}\right)}. \quad (6)$$

Using a recurrence equation

$$D_i = (T_i - T_0) - \sum_{j=1}^{i-1} D_j (i - j + 1)^{\frac{n}{2}}, \quad i > 1 \quad (7)$$

one can estimate  $D_i$  for each interval of temperature curve and then by the equation

$$q_i = k_n \frac{E}{\sqrt{\Delta t}} \sum_{j=1}^i D_j (i - j + 1)^{\frac{n-1}{2}} \quad (8)$$

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one can calculate heat flux instantaneous values at the end of interval. The SHF history reconstruction will be more accurate if we calculate the average value of heat flux on the interval and refer it to the midpoint of the interval ( $i - 0.5$ )

$$\overline{q_{i-0.5}} = q_{i-1} + \frac{2}{n+1}(q_i - q_{i-1}). \quad (9)$$

The GST-SHF transformation algorithm was tested by applying it to harmonic function of surface temperature change. The test showed that approximation of temperature history by the Eq. (5) with  $n = 2, 3$  provides the most accurate results. When GST discretization is 6 points per period we obtain the relative error of SHF history estimation equals to 3%, and given 10 points per period the relative error is less than 1% (Gornostaeva, 2014). For comparison, the algorithm proposed by Beltrami et al. (2002) under the same discretization conditions provides relative errors equals to 8% and 3.5% respectively.

### 3 GST data and SHF reconstruction

We used temperature history (Demezhko and Shchapov, 2001) early reconstructed from temperature-depth profile logged in the Urals superdeep borehole SG-4 (58°24' N, 59°44' E, Middle Urals, Russia) as initial data. The reconstruction of the surface heat flux history was conducted using the algorithm described above with  $n = 3$  (see Fig. 1). GST and SHF curves are different in shape. The temperature increase started about 15 kyr BP and after a short break it continued to 1 kyr BP, while the heat flux increase began about 3 kyr earlier. The heat flux reached its maximum of  $0.08 \text{ W m}^{-2}$  about 8 kyr BP and then it began to decline.

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sure of climate sensitivity of the region under study to long-term orbital forcing variations.

Taking the climatically caused SHF before 35 kyr BP equals to  $0 \text{ W m}^{-2}$  and integrating it with respect to time we estimate changes in heat content. This value characterizes the additional amount of heat adsorbed in a rock column having a cross-sectional area of  $1 \text{ m}^2$  and limited by the depth of thermal anomaly penetration (i.e. by a few kilometers). Until 15 kyr BP a total heat balance was negative. A minimum value of heat content of  $-3.5 \text{ TJ m}^{-2}$  with respect to the reference value at 35 kyr BP was found about 20 kyr BP. From this moment the heat flux became positive. For the next 14 kyr (20–6 kyr BP) the heat content increased to  $22.0 \text{ TJ m}^{-2}$ . For comparison, during the period of modern warming (1765–2000), heat content of the continental lithosphere increased by  $0.1 \text{ TJ m}^{-2}$  (calculated using data from Beltrami, 2002).

## 5 The comparison of the SHF with CO<sub>2</sub> changes

Another source of the additional radiative forcing during the Pleistocene–Holocene transition could be greenhouse effect caused by the increase of carbon dioxide concentration in the atmosphere (see Shakun et al., 2012 and references therein). An additional downward heat flux necessarily would contribute to SHF changes. Figure 3 shows geothermal reconstructions of surface temperatures and heat fluxes from the borehole SG-4 (on the time scale corrected after SHF-insolation synchronization) and carbon dioxide concentration changes in Antarctic ice cores (Blunier et al., 1998; Indermühle et al., 1999a, b; Smith, 1999; Barnola et al., 2003; Pedro et al., 2012). Despite the substantial dispersion of CO<sub>2</sub> estimations, a character and a chronology of CO<sub>2</sub> concentration changes are much closer to temperature changes rather than to heat flux variations. It may mean no significant contribution of CO<sub>2</sub> forcing to climatically caused heat flux during Pleistocene–Holocene warming.

About 10 kyr BP the increase of carbon dioxide concentration was replaced by its fall which ended about 8 kyr BP. This local minimum is not consistent with either GST

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or SHF histories. It is possible that the CO<sub>2</sub> decrease was associated with a sharp increase of vegetation absorbing its excess.

## 6 Conclusions

The reconstruction of the surface heat flux history using data on the past surface temperature changes represents a new instrument for climate analysis. The reconstructed SHF variations and radiative forcing changes may be compared directly because they are expressed in the same units of energy flux ( $W m^{-2}$ ) and there is no time lag in SHF reaction on external radiative forcing changes. The ratio between surface heat flux and external forcing ( $\Delta q/\Delta I$ ) may be considered as an alternative measure of the Earth's climatic sensitivity. The ratio of heat fluxes is a non-dimensional parameter, and additionally depends less on radiative forcing duration by contrast to traditional index of climatic sensitivity representing temperature reaction on the external radiative forcing ( $\Delta T/\Delta I$ ).

The described algorithm of GST-SHF transformation is quite easy to realization and allows estimating of SHF history with high precision.

Using this algorithm, we have first estimated long-term surface heat flux changes in the Urals for the past 35 kyr. The reconstructed SHF variations are almost completely coincides with changes in insolation of Northern Hemisphere on the scale of the last glacial–interglacial cycle. The amplitude of heat flux variations was about 1.3% of the insolation changes range at the latitude of 60° N. The increase of carbon dioxide concentrations occurred 2–3 thousands of years later than the heat flux increase and synchronously with temperature response.

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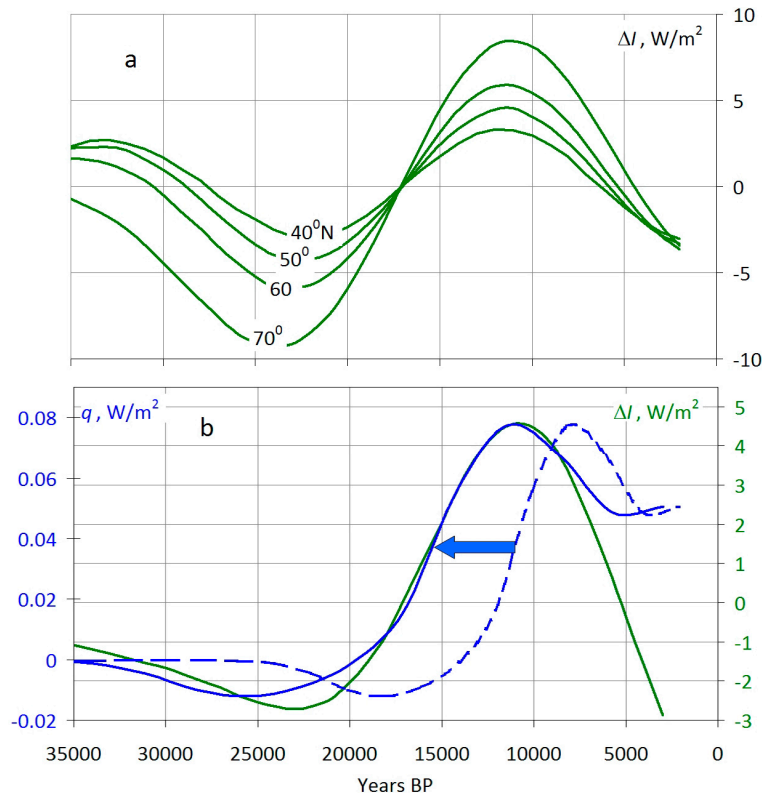
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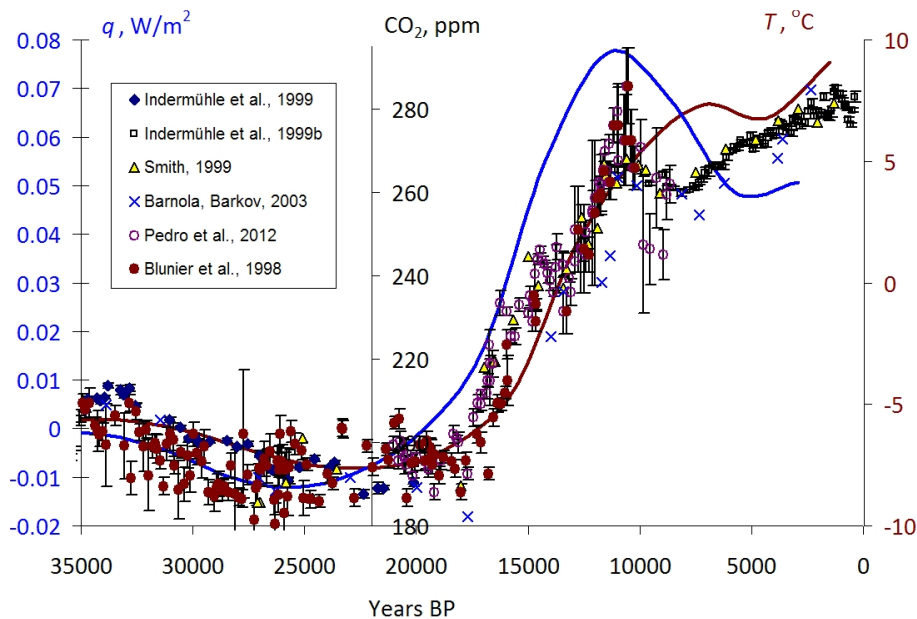


**Figure 2.** The comparison of SHF history with solar insolation changes in the Northern Hemisphere caused by changes in Earth’s orbital parameters and time scale correcting. **(a)** Annual insolation changes  $\Delta I(t)$  at the latitudes of 40–70° N (Berger, Loutre, 1991); **(b)** annual solar insolation at the latitude of 60° N smoothed in uneven running windows (green line), SHF history in the initial timescale ( $a = 1.0 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$ , blue dashed line) and SHF history in the corrected timescale ( $a = 0.71 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$ , blue solid line).

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**Figure 3.** The comparison of GST history  $T(t)$  (brown line), SHF history  $q(t)$  (blue line) and  $\text{CO}_2$  concentration in the Antarctic ice cores (multicolored markers).

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