



Supplement of

Oligocene-early Miocene paradox of $p\text{CO}_2$ inferred from alkenone carbon isotopic fractionation and sea surface temperature trends

José Guitián et al.

Correspondence to: José Guitián (jguitian@iim.csic.es) and Heather M. Stoll (heather.stoll@eaps.ethz.ch)

The copyright of individual parts of the supplement might differ from the article licence.

Table S1.**Differences between SST proxy between ZB-1 column
and RTX-200 column measurement**

Proxy		av. diff. (°C)	Stdv.
IODP 1406 (subset)	$U_{37}^{k'}$	-0.6	0.4
	$U_{38ME}^{k'}$	-0.8	1.9
ODP 1168 <22.4 Ma	$U_{37}^{k'}$	-0.5	1.2
	$U_{38ME}^{k'}$	-1	0.7
ODP 1168 >22.4 Ma	$U_{37}^{k'}$	-1.8	1.7
	$U_{38ME}^{k'}$	-2.8	1.8

**Differences between $\delta^{13}C$ alkenone between ZB-1 column
and RTX-200 column measurement**

		av. diff. (‰)	Stdv.
IODP 1406 (subset)	$\delta^{13}C$ alk	-0.2	0.9
ODP 1168 <22.4 Ma	$\delta^{13}C$ alk	-1.1	1
ODP 1168 >22.4 Ma	$\delta^{13}C$ alk	-3.7	1.6

Figure S1. High resolution IODP 1406 subset of measured $\delta^{13}\text{C}$ benthic foraminifera (red crosses), bulk carbonate (green circles), $\text{C}_{37:2}$ alkenone, calculated ϵ_p (where DIC $\delta^{13}\text{C}$ derived from bulk carbonate is solid line and circles, from benthic foraminifera transparent line and crosses), and SST.

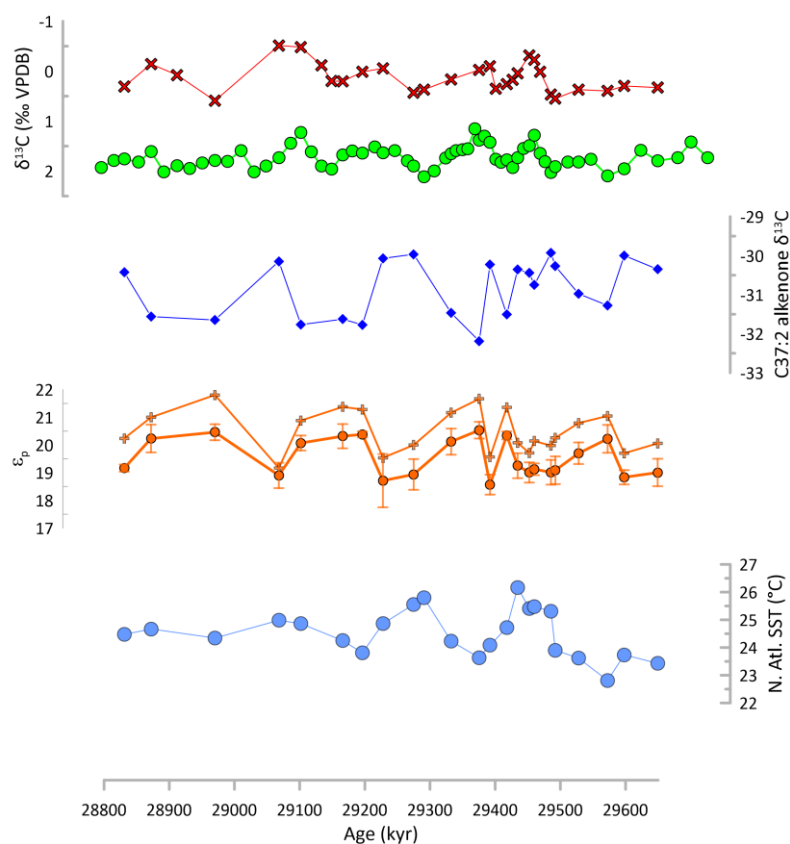


Table S2

Site	Source age model	Source SST	Source $\delta^{13}\text{C}_{\text{alk}}$	Source $\delta^{13}\text{C}_{\text{DIC}}$
ODP 1168	Stoll <i>et al.</i> , (2024)	Miocene = $U_{37}^{k'}$ This study Oligocene = $U_{38ME}^{k'}$ This study	This study	Bulk sed. -0.05 ‰
IODP 1406	Stoll <i>et al.</i> , (2024)	$U_{37}^{k'}$ This study	This study	Bulk sed. -0.05 ‰
DSDP 516	Guitian <i>et al.</i> , (2020)	TEX_{86} Auderset <i>et al.</i> , (2022)	Pagani <i>et al.</i> , (2005)	Miocene = Planktic foram. Oligocene = Benthic foram. + 2 ‰
ODP 608	CenCO2PIP Consortium, (2023)	TEX_{86} Super <i>et al.</i> , (2018)	Super <i>et al.</i> , (2018)	Planktic foram.
ODP 925	Guitian <i>et al.</i> , (2020)	TEX_{86} Zhang <i>et al.</i> , (2013) and this study	Zhang <i>et al.</i> , (2013) and this study	Bulk sed. -0.05 ‰

Figure S2. Measured biogenic silica vs SST from the same samples of IODP 1406 and ODP 1168. Dashed black line shows overall relation.

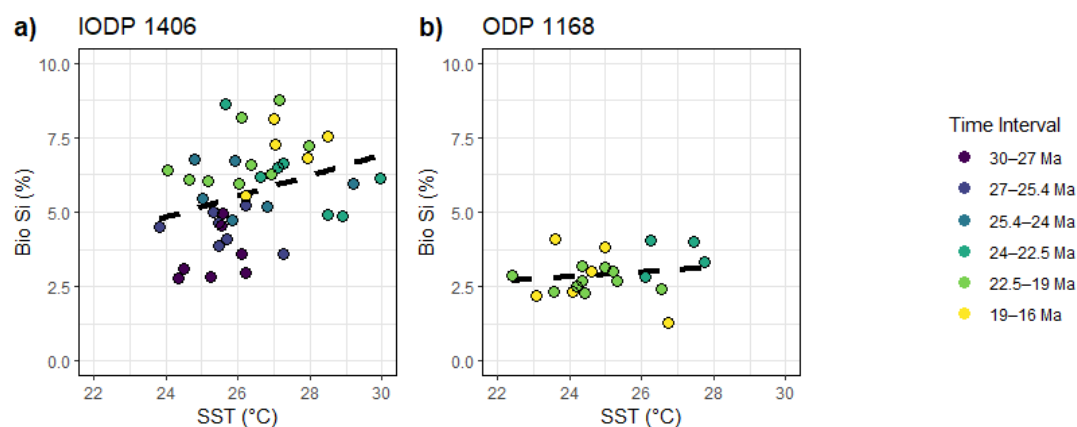


Table S3

Slopes	IODP 1406							
	SST				Benthic			
Interval (Ma)	ϵ_p measured	ϵ_p temp	ϵ_p size	ϵ_p sum	ϵ_p measured	ϵ_p temp	ϵ_p size	ϵ_p sum
30 to 27	0.5	1	0.2	0.7	-0.5	-1	2	1.49
27 to 25.4	0.7	1.1	1	1.5	-2.8	-3.1	-3.7	-4.03
25.4 to 24	-0.2	0.3	-0.1	0.4	0.1	-0.9	1.8	0.70
24 to 22.5	-0.3	0.2	-0.7	-0.2	0.5	-1.2	1.9	0.14
22.5 to 19	0	0.5	-0.2	0.3	0.4	0.1	2.7	1.82
19 to 16	0.2	0.7	0.9	1.4	0.8	1.6	6.3	7.21
All	-0.75	-0.25	-0.71	-0.21	2.16	0.98	2.53	1.24

Slopes	ODP 1168							
	SST				Benthic			
Interval (Ma)	ϵ_p measured	ϵ_p temp	ϵ_p size	ϵ_p sum	ϵ_p measured	ϵ_p temp	ϵ_p size	ϵ_p sum
30 to 27	0.5	1	0.5	1				
27 to 25.4								
25.4 to 24	0.6	1.1	1.5	2				
24 to 22.5	-0.3	0.3	-1	-0.5				
22.5 to 19	-0.4	0.1	-0.9	-0.4				
19 to 16	-0.3	0.2	-0.3	0.2	-0.7	-0.2	-0.9	-0.4
All	0.6	1.1	0.7	1.2				

Figure S3. Entire studied period correlation regression lines, for the measured ϵ_p (solid), ϵ_p without the theoretical temperature effect (transparent), and ϵ_p without the temperature and size effect (dashed). R2-values: a (0.43**, 0.16, 0.09); b (0.58**, 0.78**, 0.73**); c (0.25, 0.13, 0.15); d (0.29, 0.25, 0.48). ** p value < 0.05.

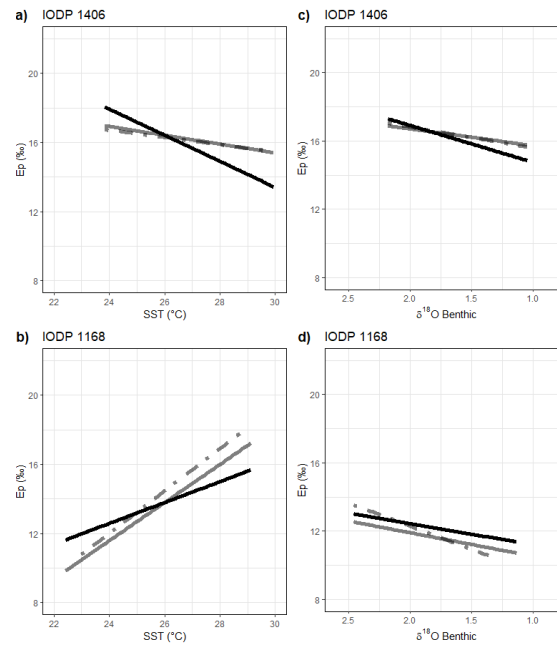


Figure S4. Relation between published ϵ_p estimates recalculated as described in text, and existing GDGTs-derived temperature reconstructions for same or nearby samples.

