Clim. Past, 21, 1917–1931, 2025 https://doi.org/10.5194/cp-21-1917-2025 © Author(s) 2025. This work is distributed under the Creative Commons Attribution 4.0 License.





The colors of proxy noise

Mara Y. McPartland¹, Thomas Münch¹, Andrew M. Dolman¹, Raphaël Hébert¹, and Thomas Laepple^{1,2}

¹Research Unit Potsdam, Alfred-Wegener-Institut Helmholtz-Zentrum für Polar- und Meeresforschung, Potsdam, Germany ²MARUM – Center for Marine Environmental Sciences, University of Bremen, Bremen, Germany

Correspondence: Mara Y. McPartland (mara.mcpartland@awi.de)

Received: 19 November 2024 – Discussion started: 22 November 2024

Revised: 12 September 2025 – Accepted: 18 September 2025 – Published: 4 November 2025

Abstract. The complex biological and physical processes that preserve paleoclimate information over centuries or longer introduce variations in proxy time series that are unrelated to the true climate. These non-climatic variations act on different timescales and are often referred to as "noise" of a specific color, based on similarities between a time series' power spectrum and the electromagnetic spectrum of light. For example, "white noise" equally affects all timescales, where "red noise" dominates only on long timescales, similar to longwave red light. Noise spectra in proxy records have far-reaching implications in paleoclimate research, but noise characteristics are often assumed based on first principles rather than estimated directly, risking either inflating or underestimating error at particular frequencies. Here, we provide concrete definitions of the various types of timescaledependent errors that are present in proxy data, and review the literature on methods for quantifying noise terms. We then synthesize the results of several published studies that use a common empirical approach for estimating the noise spectrum in ice-core, coral, and tree-ring data. We posit that the colors of proxy noise are archive-specific, with white noise dominating in depositional archives such as ice cores and marine sediment cores, while red noise is more common in biological archives such as tree rings and corals. Our synthesis supports assigning specific colored noise terms in proxy system models, data assimilations and other experiments.

1 Introduction

Paleoclimate proxy records archive past climate information via biophysical or depositional pathways and preserve it in rings, layers or strata. The processes that create these records integrate non-climatic variability alongside the climate signal either during the archiving process, or afterwards as the physical record is modified over time (Cook, 1987; Evans et al., 2013). Recovering paleoclimate information from these archives requires sophisticated data processing and modeling techniques intended to extract climate-related variance from noisy time series (von Storch et al., 2004; Cook and Kairiukstis, 1990; Hughes and Ammann, 2009; Dee et al., 2016). Recognizing that these methods may be imperfect, the challenge lies in rigorously quantifying and minimizing the impact of non-climatic variations on the signal of past climate change.

Modification of climate signals in proxy time series can result in the addition of variance from random or unrelated fluctuations, loss of variance through smoothing, shifts in timing due to irregularities in the deposition or uncertainties in dating, or a combination of these effects (Fig. 1). We regard a process that adds variance on top of an existing climate signal as a "noise process", whereas the loss of variance through smoothing also constitutes error (i.e., any difference between the true and reconstructed climate at a given timescale), but not noise, per se. Smoothing processes are typically deterministic to some extent. For example, two colocated ice-core records with similar physical properties are both affected by same isotopic diffusion and their correlation at a certain time-scale will not be affected in the absence of additional noise (Whillans and Grootes, 1985). It is further possible to correct individual records for deterministic errors if the process is well-understood (Schiffelbein, 1985; Meko,

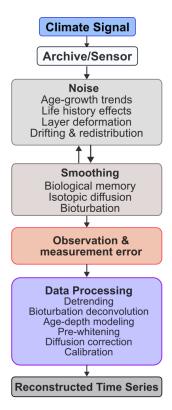


Figure 1. Conceptual diagram showing integration of different types of timescale-dependent proxy errors alongside climate signals via stochastic noise and subtractive smoothing.

1981; Dolman et al., 2021a; Shaw et al., 2024). By contrast, noise is typically independent, generating differences between nearby records as well as to the true climate signal. Observation and measurement errors are best represented by stochastic, uncorrelated noise unless they represent systematic bias, for example due to a change in the measurement apparatus. Because these types of noise are typically independent, averaging, or "stacking" individual records reduces noise while retaining the climate signal.

Both noise and smoothing processes incorporate unique timescale-dependent uncertainties alongside climate signals. For example, trees integrate multi-decadal age-growth trends alongside climate variations, such that tree-ring time series are typically "detrended" before they are used in reconstructions (Fritts, 1976; Cook and Kairiukstis, 1990; Speer, 2010). Incomplete removal of age-growth trends results in long-term biases in tree-ring data, even if interannual correlations with climate data remain reasonably strong (Melvin and Briffa, 2008, 2014a, b). By contrast, physical smoothing processes such as isotopic diffusion or bioturbation in sediments act on fast timescales by removing climate information from within deposited layers (Johnsen et al., 2000; Whillans and Grootes, 1985; Hutson, 1980; Peng and Broeker, 1984). Smoothing dampens the climate signal at annual to centennial timescales, becoming less influen-

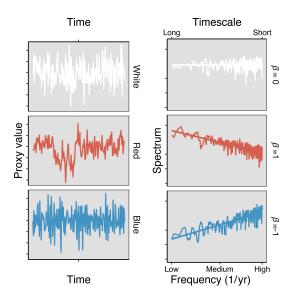


Figure 2. Spectral noise models with correlation structures referred to by analogy to colored light. Left panels show a simulated time series with the noise spectra shown in the right panels. Top: white noise with no correlation with timescale ($\beta=0$). Middle: red noise (sometimes referred to as pink noise) with a positive relationship to timescale ($\beta=1$). Bottom: blue noise with a negative relationship to timescale ($\beta=-1$). Note that β values for noise spectra are calculated as the slope of a linear model on a log-log plot, and expressed as $\beta=\operatorname{slope}\times -1$, following the convention where β describes the relationship between power and increasing timescale.

tial on longer timescales such that millennial-scale shifts in climate are retained (Schiffelbein and Hills, 1984; Laepple and Huybers, 2013; Münch and Laepple, 2018; Bothe et al., 2019).

These timescale-dependent variations can be analyzed in the spectral domain and referred to using colors by loose analogy to the frequency spectrum of light (Fig. 2). Time series with relatively more low- than high-frequency variability are considered to be "red", by analogy to long-wave red light, whereas a "white" time series implies that power spectral density is distributed evenly across the frequency space.

Low-frequency temperature variability is generally understood to exhibit increasing power with timescale, meaning that noise-free temperature proxy spectra would theoretically display a red spectrum (Pelletier, 1998; Huybers and Curry, 2006; Zhu et al., 2019). Noise, because it originates from a variety of sources may display different correlation structures. The integration of noise and climate signals may either further "redden" or "whiten" the spectrum by modifying the correlation structure of the raw time series. The relationship between power spectral density S(f) and frequency f is often summarized using a power-law scaling exponent β such that $S(f) \sim f^{-\beta}$ (Box 1) (Vautard and Ghil, 1989; Fraedrich and Blender, 2003; Hébert et al., 2021). The exponent β represents the relationship between frequency (or time period) and power spectral density, which appears as

Power-law scaling in frequency space

- The spectral exponent β summarizes the relative contribution of high- and low-frequencies to the total variance.
- The power spectral density S(f) is assumed to approximately follow a power-law with frequency f such that S(f) ~f^β
- β is typically expressed as the negative slope of a linear regression on a log-log plot of the power spectrum.

Box 1. Summarizing the timescale-dependency of proxy noise using spectral power-laws.

a linear relationship plotted on a log-log scale. By convention, the exponent is defined as the negative of the relationship with frequency such that a positive exponent represents increasing variance with timescale. Red noise processes are represented with a positive slope value ($\beta > 0$); the term "pink noise" is sometimes used specifically for $\beta = 1$ (Zhu et al., 2023). Red noise is a common noise model that implies autocorrelated errors that affect low-frequencies at a greater magnitude. (Mann et al., 2007; von Storch et al., 2009; Smerdon, 2012). By contrast, a "white" noise process implies errors uncorrelated in time such that the variance is distributed evenly across the frequency space ($\beta = 0$), similar to the spectrum of white light. White noise is the simplest and most commonly-applied noise model in paleoclimate research (Fisher et al., 1985, Ammann and Whal, 2007; von Storch et al., 2004; Mann et al., 2005; Lee et al., 2008; Smerdon, 2010, 2012). Finally, blue noise refers to processes with relatively higher variability at high frequencies ($\beta < 0$). Blue noise, which is less commonly used, is characterized by an anti-correlated structure, implying rapidly vanishing effects with increasing timescale (Mann and Rutherford, 2002; Mann et al., 2007).

Our understanding of proxy noise characteristics has evolved out of the need to reconcile diverging results in records that should, in principle, contain the same climate signal. For certain processes, such as the effects of measurement error, aliasing due to under-sampling, or depositional noise from roughness at the snow surface, the noise power spectrum can be derived from first principles and expressed in closed-form solutions (Fisher et al., 1985; Schiffelbein, 1985; Kunz et al., 2020; Dolman et al., 2021b). In cases where the physical and biological processes affecting proxies are well-understood, a more flexible approach is to use proxy system models (PSMs) (Jones et al., 2009; Vaganov et al., 2011; Evans et al., 2013; Tolwinski-Ward et al., 2011; Dee et al., 2016, 2017; Dolman and Laepple, 2018). In this case, climate data sets of temperature and precipitation from instrumental data, climate models or stochastic simulations are used as input to the PSM, and synthetic proxy time series are simulated. The spectrum of the noise can then be estimated through comparison to the climate time series (Dee et al., 2017). By omitting processes that are not well-understood, PSMs may underestimate the noise level. For example, stratigraphic noise in ice-core-based proxies can account for more than half of the isotope signal (Hirsch et al., 2023) but stratigraphic processes are not represented in current isotope PSMs (Dee et al., 2015). To account for "known unknowns" recent studies have added estimates of noise with specific spectral properties to mimic these extraneous sources of variability in PSM output, using models or reanalysis data as external validation (Dee et al., 2018; Evans et al., 2014; Zhu et al., 2023; Bothe et al., 2019).

Alternatively, empirical proxy noise spectra can be derived by relying solely on proxies by exploiting the spatial correlation of climate signals in nearby records, building on the assumption that non-climatic noise is independent between records. This approach has the advantage of being able to exploit the full length of paleoclimate time series without relying on climate models or short instrumental time series, and without the assumption that physical processes themselves are well-understood. One limitation is that this method relies on the availability of replicated or nearby records that have low time-uncertainty, such as corals, tree rings, banded ice cores or laminated sediments. If empirical noise estimates are consistent with those derived from mechanistic models this both validates the processes represented in PSMs creates a strong basis for using the resulting noise spectra in a variety of research applications.

In this study, we synthesize noise estimates derived directly from multiple proxy types and interpret their spectral characteristics in the context of known biological and physical processes. This provides a basis for evaluating signal fidelity and for refining assumptions commonly made in proxy system models and other experiments. We present noise estimates published in three studies where noise terms were derived using a simple empirical approach that partitions shared signal from independent variance on all timescales (Münch and Laepple, 2018), which we describe in the extended data section (Appendix A). We show results for published ice cores from Münch and Laepple (2018), tree rings (McPartland et al., 2024), and corals (Dolman et al., 2025). By presenting these findings alongside evidence from first principles and existing literature we aim to deepen a collective understanding of the behavior of proxy noise.

The tree-ring and coral data were sourced from global databases compiled by the Past Global Changes (PAGES) initiative (PAGES2k Consortium, 2017; Walter et al., 2023), and the ice-core data represent two large clusters of cores from Antarctica and Greenland (Graf et al., 2002; Weißbach et al., 2016; Hörhold et al., 2023) (Appendix B). Full details on each result are provided in the aforementioned studies. We focus our discussion on the noise spectra and resulting signal-to-noise ratio. Evaluating the climate signal spectra would ideally involve comparison with data and models,

which are beyond the scope of this paper. In the extended data section, we reproduce the signal spectra and sample density at each frequency to provide all information involved in the noise spectra calculations and their uncertainty estimates (Appendix C).

2 The colors of proxy noise across paleo archives

Our review of published noise estimates demonstrates that tree rings and corals exhibit clear red noise spectra with positive scaling exponent β values of 0.8 and 0.5 respectively (Fig. 3a, b) such that the power of the noise increases with timescale (McPartland et al. (2024), Dolman et al. (2025). As the noise increases more than the climate signal, this leads to a decline of the signal-to-noise ratio (SNR) (Fig. 3d, e). Treering and coral records result from the *growth* or *accretion* of layers by an individual organism over time such that life history or changes in the biological archiving system may affect proxy formation. Evidence suggests that proxy records composed of repeated measurements made on single long-lived organisms through time are susceptible to ontogenetic effects, the legacies of past disturbances, or slow changes in the behavior of the sensor.

In dendroclimatology, the pitfalls associated with tree ontogeny have been well-documented (Fritts, 1976; Cook et al., 1995; Esper and Frank, 2009). Cambial age impacts both tree-ring width and density such that detrending to remove juvenile age trends is a near universal practice (Cook and Kairiukstis 1990). Even after detrending, residual age effects could partially explain the persistent low-frequency bias observed in tree-ring records (Franke et al., 2013; Ault et al., 2013). Detrending itself can also introduce biases at medium-frequencies, particularly when fitting raw time series with negative exponential curves or rigid spline functions (Cook and Peters, 1997; Melvin and Briffa, 2008, 2014a, b; Esper, 2003; Briffa and Melvin, 2011). Techniques such as "signal-free" detrending have aimed at boosting lowfrequency variability while minimizing bias (Melvin and Briffa, 2008), but despite retaining more low-frequency variance, tests of this method indicated only minor improvements in signal strength and signal-free chronologies retained their red-noise spectra (McPartland et al., 2020, 2024). By extension, red noise is likely a feature of bivalve and sclerosponge chronologies, which contain similar age-growth trends to those found in trees and are detrended using the methods originally developed in dendrochronology (Jones, 1983; Rypel et al., 2008; Hollyman et al., 2018; McCulloch et al., 2024).

Tree rings are also smoothed on fast timescales as a result of the carryover, or "memory", of prior years' growth. Biological memory adds temporal autocorrelation to tree ring time series which has the effect of steepening the slope of the noise spectra by dampening high frequency power spectral density (Zhang et al., 2015; Lücke et al., 2019; McPart-

land et al., 2024). "Pre-whitening" chronologies by adjusting their temporal autocorrelation structure to match the climate target improves the interannual correlation between data and proxy (Meko, 1981), but by virtue of removing additional variability at high-frequencies, decreases the ratio of high to low power spectral density that defines the noise slope term β .

Coral aragonite records might similarly be affected by changes in the biology of individual or descendent polyps over time resulting in a slow drift in the temperature response of the proxy which would appear as low-frequency variability. Such changes could be growth-rate related due to reaction-kinetic effects (Goodkin et al., 2005; Hayashi et al., 2013; Maier et al., 2004; Saenger et al., 2008; Suzuki et al., 2005), result from changes in the calcification process (Lough, 2004), or persistent baseline shifts in trace element ratios following thermal stress events (D'Olivo and McCulloch, 2017; D'Olivo et al., 2019) perhaps mediated by changes in the composition of photosynthetic symbionts (Berkelmans and van Oppen, 2006; Cohen, 2002; Little et al., 2004).

The stacks of ice cores from both Greenland and Antarctica that we analyzed show a high white noise level where β is approximately equal to zero (Fig. 3e, f) (Münch and Laepple, 2018). As the climate variations become more pronounced on longer timescales, this leads to an increasing signal-to-noise ratio with time. We argue that proxies that are primarily the result of deposition, rather than growth or accretion primarily contain white noise stemming from stratigraphic processes. Precipitation intermittency and postdepositional redistribution in ice cores result in adjacent measurements that represent water from different precipitation events (Laepple et al., 2018; Casado et al., 2020; Zuhr et al., 2023). By extension, in marine sediments where foraminifera or diatoms are deposited from the water column, each sample represents a new set of individuals such that biological effects are uncorrelated between measurements. From processbased experiments, it has been demonstrated that noise in sediment records is also predominantly white with the signal level increasing as more individuals are measured (Kunz et al., 2020; Dolman et al., 2021b). In both ice and sediment core records of near-surface temperature, seasonal depositional cycles are much stronger than any interannual or even millennial climate change and the sparse subsampling of the seasonal signal leads to aliasing of independent noise within the signal of annual variation (Kunz et al., 2020). Precipitation intermittency and depositional redistribution break up the signal of the large seasonal cycle that would appear as a spike in the spectrum at annual timescales if the signal were recorded without disruption. Instead, the spike is redistributed as white noise across all frequencies (Casado et al., 2020; Münch et al., 2021).

We identified fewer examples of blue noise processes in the paleoclimate literature. Because its effects diminish quickly with time, blue noise does not introduce error past

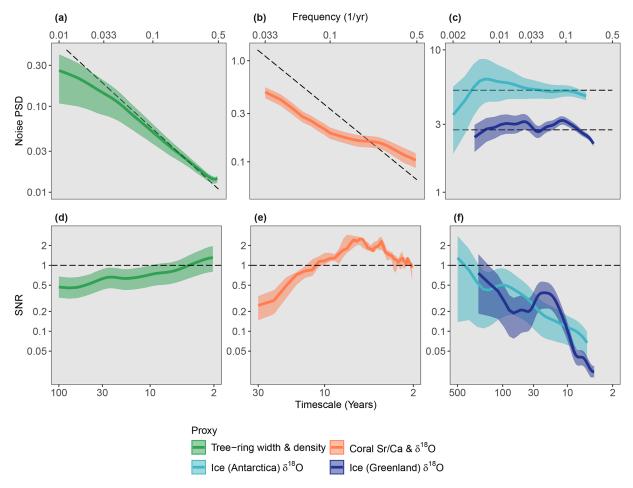


Figure 3. Estimates of proxy noise spectra (a–c) and timescale-dependent signal-to-noise ratios (d–f). Top: (a) mean noise spectra for treering width and density records from the northern hemisphere, (b) mean noise spectra for tropical coral δ^{18} O and strontium/calcium (Sr / Ca) ratios, (c) noise spectra for ice core δ^{18} O from Dronning Maud Land (light blue) in Antarctica and the North Greenland Traverse (dark blue). Dashed lines on the top row of panels represent an idealized spectral power-law with a slope $\beta=1$ for proxies containing predominantly red noise (i.e. tree rings and corals), and with $\beta=0$ for proxies (i.e. ice cores) containing predominantly white noise. Bottom: Timescale-dependent signal-to-noise ratios (SNR) for (d) tree rings, (e) corals, and (f) ice cores. Dashed lines represent an SNR of 1. Confidence intervals on all spectra represent the 10th and 90th percentiles from a parametric bootstrapping estimation method. Detailed methods for estimating proxy noise and SNR values can be found in McPartland et al. (2024) (tree rings) and Dolman et al. (2025) (corals).

fast timescales. An example of a true blue noise process is the infilling of troughs on ice sheets as wind redistributes snow causing blue noise in noise in annual layer thickness records from ice cores (Fisher et al., 1985). Blue noise models have occasionally been tested alongside red and white noise to account for a variety of potential types of error affecting high-frequencies, and to improve the fit between synthetic proxy records and climate model data (Mann et al., 2007; Mann and Rutherford, 2002).

Like blue noise, smoothing processes predominantly affect high frequencies and becomes less significant with timescale. Biological memory in trees, diffusion in ice cores, and bioturbation in sediments are all examples of smoothing processes that lead to correlated errors between the climate and the proxy signal which can theoretically be accounted for using deterministic modeling (Matalas, 1962; Berger et al., 1977; Meko, 1981; Ruddiman et al., 1980; Whillans and Grootes, 1985). Given such a model, the smoothing effect can be reversed, as we applied in this example to ice core data to reverse the effects of diffusion (Shaw et al., 2024) (see Appendix A). If, as in the case of diffusion, the smoothing process affects the signal and the noise equally, the SNR is unbiased at all timescales regardless of whether or not a correction for the smoothing effect is applied. However, when noise is introduced after smoothing (e.g. measurement noise), the attenuated climate signal on the high-frequency side will be masked by a relatively stronger noise level, biasing the SNR spectrum downwards toward high frequencies. In any case, knowledge about and accounting for smoothing processes in paleoclimate time series is critical for evaluating the short-

term effects of climate forcing events such as volcanic eruptions (Esper et al., 2015; Zhang et al., 2015; Lücke et al., 2019), but is potentially less critical for reconstructing low-frequency variations in climate.

3 Time uncertainty and noise color

Dating for all three proxy types discussed here is primarily achieved by some kind of band dating, or by counting annual cycles in geochemical tracers. If bands or cycles are missed, or double counted, this introduces time-uncertainty and an additional source of error in the reconstructed climate time series (Comboul et al., 2014). Time uncertainty has little effect on the shape of individual power spectra when the spectra are broadband, as is typical for climate time series (Rhines and Huybers, 2011). However, it reduces coherence between records, diminishing high-frequency power in stacked spectra and biasing SNR estimates downward at shorter timescales (Münch and Laepple, 2018; Fig. D1). The effect of time-uncertainty acts as a linear transfer function on the stacked spectra and can be estimated and corrected for if the time uncertainty is known, although this was not applied here (Appendix D). For the ice-core records analyzed here, the time-uncertainty is due to potential variations in the accumulation rate between volcanic tie-points and is negligible for frequencies below 1/10 years (Münch and Laepple, 2018, their Fig. B1).

For the sub-annual resolution coral records used here, age models mostly come from counting annual cycles in the geochemical tracers. However, for most coral records there are no independently dated tie-points and so it is not possible to directly estimate counting error rates and correct for time-uncertainty. Simulations with potential error rates derived from corals show that the slope of the SNR is biased in the opposite direction to the one we estimate (Fig. D1) and that even for very large error rates of 1 in 10 years' time-uncertainty cannot account for the low SNR at decadal timescales. Time uncertainty is arguably less of an issue for tree-ring records as they are considered to be precisely dated and dendrochronologists routinely employ statistical cross-dating techniques to identify and eliminate dating errors (Holmes et al., 1986). Through this process locally absent rings are identified during cross-dating and assigned a no-data value to avoid affecting the final chronology. The strength of the tree-ring SNR on sub-decadal timescales is indicative of this dating precision.

For proxy archives that are not annually resolved such as reconstructions from non-varved terrestrial and marine sediment cores, the irregular spacing of samples in time and larger dating uncertainties makes stacking unsuitable for this type of noise estimation, representing a limitation of this approach. Alternative methods, such as estimating the SNR as a function of time uncertainty (Reschke et al., 2019), or applying tuning methods that align proxy records by maximiz-

ing covariance and assess significance against surrogate data (Haam and Huybers, 2010), may still allow for empirical SNR estimation in these cases.

4 Implications of colored noise for climate reconstruction

The spectrum of temperature on local to global scales is generally accepted to be red (Huybers and Curry, 2006; Cheung et al., 2017; Hasselmann, 1976). For proxies with predominantly white-noise spectra such as ice cores and sediments, this implies that the SNR increases with timescale. This explains why ice cores are faithful recorders of millennial climate variability (e.g. EPICA community members, 2006), while they fail in many regions to reconstruct interannual to decadal changes (Stenni et al., 2017). By contrast, in proxies that contain red noise, the SNR will rise more slowly or even decline with timescale if the power of the noise rises more steeply than the signal, as we demonstrate in tree rings and corals. These proxies are better recorders of fast timescale variability where the ratio of signal to noise is highest. For example, corals can deliver unique information on tropical climate dynamics such as the El Niño Southern Oscillation (ENSO) (Fig. 3), but have challenges reproducing multidecadal trends (Scott et al., 2010). The color of the noise thus influences the timescales at which a robust climate signal can be reconstructed because it introduces a frequencydependence to the SNR.

Information about proxy noise can be used to guide future study design (e.g. what proxies can be used to answer a climatic hypothesis) and to optimize the sampling and measuring design (e.g. how many cores are needed; what is the optimal sampling resolution to minimize noise). It can also be used to estimate time scale-dependent uncertainty in climate reconstructions. For individual proxy time series where the signal increases more strongly with timescale than the noise, when the signal spectrum is "redder" than the noise, binning to a coarser timestep or by applying stronger smoothing reduces the noise. This improves the SNR, albeit at the cost of losing information at shorter timescales. The extent to which uncertainty is reduced by binning or smoothing depends on the relative spectral slopes of both the signal and noise.

Knowing the color and level of proxy noise is valuable in a variety of research contexts in paleoclimatology. For example, accurate noise models are important for pseudo-proxy experiments (PPEs) in which climate model output is transformed into pseudo-proxy time series to test the skill of reconstruction methods and evaluate models (Jones et al., 2009; Smerdon, 2012). Often PPEs rely on sensitivity tests using different noise levels or spectral colors (Riedwyl et al., 2009; Smerdon et al., 2010; Mann and Rutherford, 2002; Gómez-Navaro et al., 2017). Red noise is often tested alongside white or sometimes blue noise, but typically using a first-order autoregressive (AR(1)) process with a fixed spec-

tral slope (β = 2) (Mann et al., 2007; Riedwyl et al., 2009). However, this can lead to underestimation of the actual noise, especially at low frequencies where the spectrum of an AR(1) process levels out. More recent PPEs have integrated full PSM complexity with realistic noise estimates (Bothe et al., 2019; Zhu et al., 2023). Finally, accurate noise estimation is important in data assimilations and field reconstructions to bring reconstructed time series into better alignment with calibration datasets, and to propagate uncertainty in estimates of past climate variability (Goosse et al., 2010; King et al., 2021).

5 Conclusion

Building on prior insights from proxy system modeling, and with reference to a first-principles based understanding of proxy formation, we present here an overview of how colored noise is represented in different types of paleoclimate archives. Incorporating empirical, proxy-specific noise models as presented here into a range of paleoclimate research activities will help to move away from the assumption that noise is white or follows a first-order autoregressive process, which can lead to misinterpreting noise as signal and propagating biases into results. These noise models, or models derived using similar stacking and variance-partitioning methods, can be used account for the range of unique biological and physical processes affecting proxies in pseudo proxy experiments, data assimilation frameworks, and reconstructions efforts to improve the representation of patterns of past climate variability.

Appendix A: Estimating the spectrum of noise

We apply the method of Münch et al. (2018) of combining clustered proxy records into regional stacks and analyzing their variance in the frequency domain. This builds on the assumption that the proxy signal is a function of four main components: the climate signal, additive noise that arises during the proxy creation and archiving stages, measurement noise, and any smoothing processes that act during archiving but not on the measurement noise; i.e.

$$P = f(C, N, \Sigma; G) = G(C + N) + \Sigma \tag{A1}$$

where P, C, N, and Σ stand for the power spectral densities of the proxy signal, the climate signal, the proxy noise, and the measurement noise, respectively, and where G is a transfer function that describes a specific smoothing process such as biological memory, diffusion, or bioturbation.

Given a regional cluster of n proxy records with a similar climate between sites, the mean power spectrum, M, averaged across all individual records' spectra, will yield a precise estimate of the proxy spectrum P. By contrast, the power spectrum, S, of the stacked record from averaging all records in the time domain, will also contain the full climate signal,

but with the noise proportions reduced by a factor of n. By combining both quantities one can derive expressions for the climate and noise spectra (Münch and Laepple, 2018),

$$C = \frac{n}{n-1}G^{-1}\left(S - \frac{M}{n}\right);$$

$$N = \frac{n}{n-1}G^{-1}\left(M - S - \frac{n-1}{n}\Sigma\right)$$
(A2)

with the ratio of C:N yielding the frequency-resolved signal-to-noise ratio (SNR). A common smoothing process equally biases the signal and the noise spectrum, if not corrected for by means of the inverse transfer function G^{-1} , and hence its effect cancels out in the SNR spectrum. We note that time uncertainty between individual proxy records can be another source of smoothing in the stacked record, but it is less straightforward to include into our methodology (Münch and Laepple, 2018) and is neglected here.

Appendix B: Data

B1 Tree Rings

For the tree-ring data we analyzed the tree-ring records contained within the Past Global Changes 2k (PAGES2k) database, a large database compiled to reconstruct global temperature variations during the last two millennia. This network of 647 unique paleoclimate records from around the globe includes 450 tree-ring time series, of which we used 421 records of tree-ring width and density located across the Northern hemisphere (PAGES 2k Consortium et al., 2013, 2017; Neukom et al., 2019). Spatial clusters were defined using 250 km radii, such that no two sites were more than 500 km apart. Tree-ring width and density records were clustered separately so that the proxies weren't mixed within clusters. This resulted in 253 clusters containing a minimum of 3, and a maximum of 30 sites per cluster. The average number of sites per cluster was 8. There were 18 density and 235 ring width clusters. The average length of the overlapping period was around 450 years. The results of all clusters of both proxy types were averaged at the end to derive the signal, noise and SNR. Uncertainty was calculated using a parametric bootstrapping approach. (McPartland et al., 2024).

B2 Corals

We used the coral records contained within the PAGES Coral Hydro 2k database to obtain coral SNR estimates (Walter et al., 2023). The Coral Hydro2k database contains 54 oxygen ($\delta^{18}\text{O}$) and strontium calcium (Sr / Ca) records from the global tropics. The database was compiled to reconstruct sea surface temperature and ocean hydroclimate variability for the past two centuries. Due to fewer records, 1000 km spatial clusters were used, resulting in 64 clusters. $\delta^{18}\text{O}$ and Sr / Ca

records were clustered separately and the results were averaged. More information on the coral data curation is contained in Dolman et al. (2025).

B3 Ice Cores

As an example in ice-core derived temperature proxies, we use stable isotope records from the Dronning Maud Land region in Antarctica ("DML data" in the following; Graf et al., 2002) and from central-north Greenland ("NGT data" in the following; Weißbach et al., 2016; Hörhold et al., 2023).

The DML data consist of 15 records, 12 of which cover the time period from 1800 to 1998 CE and 3 records cover 1000–1998 CE. We combine both datasets by using the individual spectral results (Münch and Laepple, 2018) of the shorter records on timescales below decadal and of the longer records on the supra-decadal timescales. We apply the diffusion correction as in Münch and Laepple (2018) but do not use their time-uncertainty correction.

The NGT data comprise 14 cores covering the time span from 1505 to 1979 CE, including original records from the North Greenland Traverse published in Weißbach et al. (2016) as well as the extended NGT records from exploiting new drillings as presented in Hörhold et al. (2023). The corresponding NGT spectra shown in Hörhold et al. (2023) were not diffusion-corrected; here, to be able to compare the NGT spectra to those from the DML data, we apply a diffusion correction to the NGT spectra following the method given in Münch and Laepple (2018) with diffusion length estimates calculated as described in Hörhold et al. (2023). Note that the SNR spectrum shown in Hörhold et al. (2023) used the ratio of the integrated signal and noise spectra, which is related to the correlation with the climate signal (Münch and Laepple, 2018), whereas here we show the direct ratio of the spectra.

Appendix C: Signal, noise and signal-to-noise ratio estimation

Full results for the uncorrected signal, noise and SNR estimates for tree rings, corals and ice-core data (Fig. C1a-d). Spectra in Fig. 3 represent truncated versions which have been cut off where sample density in corals and tree rings drop off (shaded regions), as seen in the spectral density plots (Fig. C1 bottom panels). In both corals and tree rings, the SNR rises again due to the reduction in replication and dominance by single or a small number of records with higher SNR than average (Fig. C1a, b) (see McPartland et al., 2024; Fig. 2e, f). Confidence intervals on all spectra represent the 10th and 90th percentiles from a parametric bootstrapping estimation method. In addition to the truncation due to low sample size, the lowest two spectral estimates on all spectra are removed during SNR calculation and confidence interval estimation a the multitaper approach introduces a small bias at the lowest frequencies (Percival and Walden, 1993).

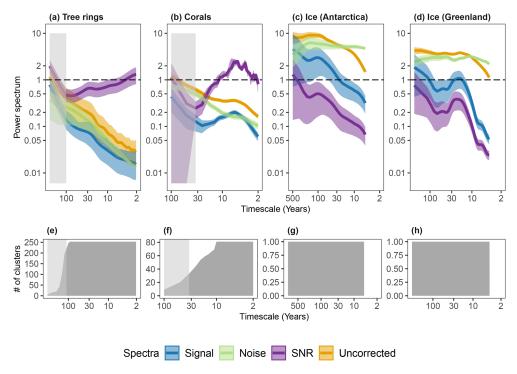


Figure C1. Timescale-dependent signal, noise and SNR estimates with sample density plots for tree rings (\mathbf{a} , \mathbf{e}), corals (\mathbf{b} , \mathbf{f}), and ice-core δ^{18} O data from Dronning Maud Land in Antarctica (\mathbf{c} , \mathbf{g}) and the North Greenland Traverse (\mathbf{d} , \mathbf{h}). Panels (\mathbf{a})–(\mathbf{d}) show signal (blue), noise (green) and SNR (purple) curves, with the uncorrected "proxy" spectra (yellow). Confidence intervals on all spectra represent the 10th and 90th percentiles from a parametric bootstrapping estimation method. The light grey shading indicates the cut-off point for spectral estimates presented in Fig. 3 when sample density decreases and the results become more uncertain. Detailed methods for estimating proxy noise and SNR values can be found in McPartland et al. (2024) (tree rings), Münch et al. (2018) (ice cores) and Dolman et al. (2025) (corals).

Appendix D: Simulated effects of time uncertainty on timescale-dependent signal-to-noise ratios

To illustrate the potential effects of time uncertainty on estimates of signal-to-noise ratio we used the approach of Comboul et al. (2014) as implemented by Münch and Laepple (2018). Münch and Laepple (2018) show that relative time-uncertainty between records in a stack acts as a linear transfer function, reducing power in the stack at high frequencies. The precise shape of the transfer function depends on the counting error rate, and on the lengths of the time series, as longer time series allow larger relative errors to accumulate. It does not depend on the power spectrum of the initial "true" signal. Here we show the effect on SNR for 100-year time series with band counting error rates of 1 in 10, 50 and 100 years, with equal probability of missing or double counting a band. The effect on estimated SNR is shown relative to a hypothetical true SNR of 1.

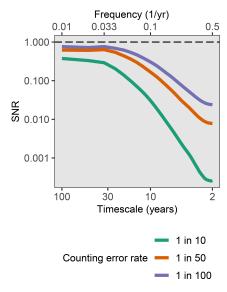


Figure D1. The influence of time-uncertainty on SNR estimated by the stacking method. Here time uncertainty is simulated for a set of 100-year depositional records with band counting error rates of 1 in 10, 50 and 100, and a true SNR of 10 at all frequencies. The simulation was carried out following Münch and Laepple (2018) which implements the counting error model of Comboul et al. (2014).

Code availability. The general software to conduct the separation of signal and noise in the spectral domain and to perform the signal-to-noise ratio analysis is available as the R package proxysnr from the open research data repository Zenodo (https://doi.org/10.5281/zenodo.17098991, Münch et al., 2025). Additionally, specific code to reproduce the tree-ring, coral, and ice-core analyses, respectively, are also available via Zenodo (https://doi.org/10.5281/zenodo.10822165, McPartland and Dolman, 2024; https://doi.org/10.5281/zenodo.14025394, Dolman,

2024; https://doi.org/10.5281/zenodo.17098991, Münch, 2025a; https://doi.org/10.5281/zenodo.17102273, Münch, 2025b).

Data availability. This work represents a synthesis of multiple independent research projects. The data needed to reproduce the tree-ring and coral data are publicly available through the NOAA National Centers for Environmental Information (https://doi.org/10.25921/YCR3-7588, Emile-Geay et al., 2017; Walter et al., 2023). The original Antarctic icecore isotope data are archived at the PANGAEA database (https://doi.org/10.1594/PANGAEA.728240, Graf et al., 2002) as well as the Greenland data except for core NGRIP whose data is available from the Centre for Ice and Climate of Copenhagen University (https://doi.org/10.1594/PANGAEA.849161, Weißbach et al., 2016; Hörhold et al., 2023). PANGAEA is hosted by the Alfred Wegener Institute Helmholtz Centre for Polar and Marine Research (AWI), Bremerhaven and the Center for Marine Environmental Sciences (MARUM), Bremen, Germany.

Author contributions. MYM wrote the manuscript, created figures, and contributed the analysis of tree-ring data. TM developed the signal-to-noise ratio analysis, contributed the analysis of the ice-core data, and helped write and edit the manuscript. AMD contributed analysis of coral data and the simulations of colored noise spectra and time uncertainty simulations, and helped write and edit the manuscript. RH helped write and edit the manuscript. TL developed the signal-to-noise ratio analysis, helped to write and edit the manuscript, and supervised analysis of all proxy data.

Competing interests. The contact author has declared that none of the authors has any competing interests.

Disclaimer. Publisher's note: Copernicus Publications remains neutral with regard to jurisdictional claims made in the text, published maps, institutional affiliations, or any other geographical representation in this paper. While Copernicus Publications makes every effort to include appropriate place names, the final responsibility lies with the authors. Views expressed in the text are those of the authors and do not necessarily reflect the views of the publisher.

Acknowledgements. This work profited from discussions at the Climate Variability Across Scales (CVAS) working group of the Past Global Changes (PAGES) program. We acknowledge the contributions of Nora Hirsch, Jannis Viola and Vanessa Skiba, along with members of the AWI-Earth System Diagnostics Group.

Financial support. This is a contribution to the SPACE ERC project; this project has received funding from the European Research Council (ERC) under the European Union's Horizon 2020 Research and Innovation program (grant no. 716092). A. Dolman was supported by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) – project number 468685498

(A.M.D.) – SPP 2299/project number 441832482. T. Münch was supported by the Informationsinfrastrukturen grant of the Helmholtz Association as part of the DataHub of the Research Field Earth and Environment.

The article processing charges for this open-access publication were covered by the Alfred-Wegener-Institut Helmholtz-Zentrum für Polar- und Meeresforschung.

Review statement. This paper was edited by Stephen Obrochta and reviewed by three anonymous referees.

References

- Ammann, C. M. and Wahl, E. R.: The importance of the geophysical context in statistical evaluations of climate reconstruction procedures, Climatic Change, 85, 71–88, https://doi.org/10.1007/s10584-007-9276-x, 2007.
- Ault, T. R., Cole, J. E., Overpeck, J. T., Pederson, G. T., St. George, S., Otto-Bliesner, B., Woodhouse, C. A., and Deser, C.: The Continuum of Hydroclimate Variability in Western North America during the Last Millennium, J. Climate, 26, 5863–5878, https://doi.org/10.1175/JCLI-D-11-00732.1, 2013.
- Berger, W. H., Johnson, R. F., and Killingley, J. S.: "Unmixing" of the deep-sea record and the deglacial meltwater spike, Nature, 269, 661–663, https://doi.org/10.1038/269661a0, 1977.
- Berkelmans, R. and van Oppen, M. J. H.: The role of zooxanthellae in the thermal tolerance of corals: a "nugget of hope" for coral reefs in an era of climate change, Proceedings of the Royal Society B: Biological Sciences, 273, 2305–2312, https://doi.org/10.1098/rspb.2006.3567, 2006.
- Bothe, O., Wagner, S., and Zorita, E.: Simple noise estimates and pseudoproxies for the last 21 000 years, Earth Syst. Sci. Data, 11, 1129–1152, https://doi.org/10.5194/essd-11-1129-2019, 2019.
- Briffa, K. R. and Melvin, T. M.: A Closer Look at Regional Curve Standardization of Tree-Ring Records: Justification of the Need, a Warning of Some Pitfalls, and Suggested Improvements in Its Application, in: Dendroclimatology, Springer, Dordrecht, 113–145, https://doi.org/10.1007/978-1-4020-5725-0_5, 2011.
- Casado, M., Münch, T., and Laepple, T.: Climatic information archived in ice cores: impact of intermittency and diffusion on the recorded isotopic signal in Antarctica, Clim. Past, 16, 1581–1598, https://doi.org/10.5194/cp-16-1581-2020, 2020.
- Cheung, A. H., Mann, M. E., Steinman, B. A., Frankcombe, L. M., England, M. H., and Miller, S. K.: Comparison of Low-Frequency Internal Climate Variability in CMIP5 Models and Observations, J. Climate, 30, 4763–4776, https://doi.org/10.1175/JCLI-D-16-0712.1, 2017.
- Cohen, A. L.: The Effect of Algal Symbionts on the Accuracy of Sr / Ca Paleotemperatures from Coral, Science, 296, 331–333, https://doi.org/10.1126/science.1069330, 2002.
- Comboul, M., Emile-Geay, J., Evans, M. N., Mirnateghi, N., Cobb, K. M., and Thompson, D. M.: A probabilistic model of chronological errors in layer-counted climate proxies: applications to annually banded coral archives, Clim. Past, 10, 825–841, https://doi.org/10.5194/cp-10-825-2014, 2014.

- Cook, E. R.: The decomposition of tree-ring series for environmental studies, Tree-Ring Bulletin (USA), 47, 37–59 http://hdl. handle.net/10150/261788 (last access: 4 February 2019), 1987.
- Cook, E. R. and Kairiukstis, L. A.: Methods of Dendrochronology: Applications in the Environmental Sciences, Springer Science & Business Media, 403 pp., ISBN: 978-94-015-7879-0, 1990.
- Cook, E. R. and Peters, K.: Calculating unbiased tree-ring indices for the study of climatic and environmental change, The Holocene, 7, 361–370, https://doi.org/10.1177/095968369700700314, 1997.
- Cook, E. R., Briffa, K. R., Meko, D. M., Graybill, D. A., and Funkhouser, G.: The "segment length curse" in long tree-ring chronology development for palaeoclimatic studies, The Holocene, 5, 229–237, https://doi.org/10.1177/095968369500500211, 1995.
- Dee, S., Emile-Geay, J., Evans, M. N., Allam, A., Steig, E. J., and Thompson, D. M.: PRYSM: An open-source framework for PRoxY System Modeling, with applications to oxygen-isotope systems, Journal of Advances in Modeling Earth Systems, 7, 1220–1247, https://doi.org/10.1002/2015MS000447, 2015.
- Dee, S. G., Steiger, N. J., Emile-Geay, J., and Hakim, G. J.: On the utility of proxy system models for estimating climate states over the common era, J. Adv. Model. Earth Syst., 8, 1164–1179, https://doi.org/10.1002/2016MS000677, 2016.
- Dee, S. G., Parsons, L. A., Loope, G. R., Overpeck, J. T., Ault, T. R., and Emile-Geay, J.: Improved spectral comparisons of paleoclimate models and observations via proxy system modeling: Implications for multi-decadal variability, Earth and Planetary Science Letters, 476, 34–46, https://doi.org/10.1016/j.epsl.2017.07.036, 2017.
- Dee, S. G., Russell, J. M., Morrill, C., Chen, Z., and Neary, A.: PRYSM v2.0: A Proxy System Model for Lacustrine Archives, Paleoceanography and Paleoclimatology, 33, 1250–1269, https://doi.org/10.1029/2018PA003413, 2018.
- D'Olivo, J. P. and McCulloch, M. T.: Response of coral calcification and calcifying fluid composition to thermally induced bleaching stress, Sci. Rep., 7, 2207, https://doi.org/10.1038/s41598-017-02306-x, 2017.
- D'Olivo, J. P., Georgiou, L., Falter, J., DeCarlo, T. M., Irigoien, X., Voolstra, C. R., Roder, C., Trotter, J., and McCulloch, M. T.: Long-Term Impacts of the 1997–1998 Bleaching Event on the Growth and Resilience of Massive Porites Corals From the Central Red Sea, Geochemistry, Geophysics, Geosystems, 20, 2936–2954, https://doi.org/10.1029/2019GC008312, 2019.
- Dolman, A.: EarthSystemDiagnostics/Dolman-et-al-2024-corals-exaggerate: Code for second submission of paper, Zenodo [code], https://doi.org/10.5281/zenodo.14025394, 2024.
- Dolman, A., McPartland, M., Felis, T., and Laepple, T.: Coral records exaggerate past decadal tropical climate variability, Research Square [preprint], https://doi.org/10.21203/rs.3.rs-3924954/v1, 9 January 2025.
- Dolman, A. M. and Laepple, T.: Sedproxy: a forward model for sediment-archived climate proxies, Clim. Past, 14, 1851–1868, https://doi.org/10.5194/cp-14-1851-2018, 2018.
- Dolman, A. M., Kunz, T., Groeneveld, J., and Laepple, T.: A spectral approach to estimating the timescale-dependent uncertainty of paleoclimate records Part 2: Application and interpretation, Clim. Past, 17, 825–841, https://doi.org/10.5194/cp-17-825-2021, 2021a.

- Dolman, A. M., Groeneveld, J., Mollenhauer, G., Ho, S. L., and Laepple, T.: Estimating Bioturbation From Replicated Small-Sample Radiocarbon Ages, Paleoceanography and Paleoclimatology, 36, e2020PA004142, https://doi.org/10.1029/2020PA004142, 2021b.
- Emile-Geay, J., McKay, N. P., Kaufman, D. S., von Gunten, L., Wang, J., Anchukaitis, K. J., Abram, N. J., Addison, J. A., Curran, M. A. J., Evans, M. N., Henley, B. J., Hao, Z., Martrat, B., McGregor, H. V., Neukom, R., Pederson, G. T., Stenni, B., Thirumalai, K., Werner, J. P., Xu, C., Divine, D. V., Dixon, B., Gergis, J., Mundo, I. A., Nakatsuka, T., Phipps, S. J., Routson, C., Steig, E. J., Tierney, J. E., Tyler, J. J., Allen, K. J., Bertler, N. A. N., Björklund, J., Chase, B. M., Chen, M.-T., Cook, E. R., de Jong, R., DeLong, K. L., Dixon, D. A., Ekavkin, A. A., Ersek, V., Filipsson, H. L., Francus, P., Freund, M. B., Frezzotti, M., Gaire, N. P., Gajewski, K. J., Ge, Q., Goosse, H., Gornostaeva, A., Grosjean, M., Horiuchi, K., Hormes, A., Husum, K., Isaksson, E., Kandasamy, K., Kawamura, K., Kilbourne, K. H., Koç, N., Leduc, G., Linderholm, H. W., Lorrey, A., Mikhalenko, V. N., Mortyn, P. G., Motoyama, H., Moy, A. D., Mulvaney, R., Munz, P. M., Nash, D. J., Oerter, H., Opel, T., Orsi, A. J., Ovchinnikov, D. V., Porter, T. J., Roop, H. A., Saenger, C. P., Sano, M., Sauchyn, D. J., Saunders, K. M., Seidenkrantz, M.-S., Severi, M., Shao, X., Sicre, M.-A., Sigl, M., Sinclair, K., St. George, S., St. Jacques, J.-M., Meloth, T., Thapa, U. K., Thomas, E. R., Turney, C. S. M., Uemura, R., Viau, A. E., Vladimirova, D. O., Wahl, E. R., White, J. W. C., Yu, Z., and Zinke, J.: NOAA/WDS Paleoclimatology – PAGES2k Global 2,000 Year Multiproxy Database, NOAA National Centers for Environmental Information [data set], https://doi.org/10.25921/YCR3-7588, 2017.
- EPICA community members: One-to-one coupling of glacial climate variability in Greenland and Antarctica, Nature, 444, 195–198, https://doi.org/10.1038/nature05301, 2006.
- Esper, J. and Frank, D.: Divergence pitfalls in tree-ring research, Climatic Change, 94, 261–266, https://doi.org/10.1007/s10584-009-9594-2, 2009.
- Esper, J., Cook, E. R., Krusic, P. J., Peters, K., and Schweingruber, F. H.: Tests of the RCS Method for Preserving Low-Frequency Variability in Long Tree-Ring Chronologies, Tree Ring Res., 59, 81–98, https://repository.arizona.edu/handle/10150/262573 (last access: 12 July 2023), 2003.
- Esper, J., Schneider, L., Smerdon, J. E., Schöne, B. R., and Büntgen, U.: Signals and memory in tree-ring width and density data, Dendrochronologia, 35, 62–70, https://doi.org/10.1016/j.dendro.2015.07.001, 2015.
- Evans, M. N., Tolwinski-Ward, S. E., Thompson, D. M., and Anchukaitis, K. J.: Applications of proxy system modeling in high resolution paleoclimatology, Quaternary Science Reviews, 76, 16–28, https://doi.org/10.1016/j.quascirev.2013.05.024, 2013.
- Evans, M. N., Smerdon, J. E., Kaplan, A., Tolwinski-Ward, S. E., and González-Rouco, J. F.: Climate field reconstruction uncertainty arising from multivariate and nonlinear properties of predictors, Geophysical Research Letters, 41, 9127–9134, https://doi.org/10.1002/2014GL062063, 2014.
- Fisher, D. A., Reeh, N., and Clausen, H. B.: Stratigraphic Noise in Time Series Derived from Ice Cores, Annals of Glaciology, 7, 76–83, https://doi.org/10.3189/S0260305500005942, 1985.
- Fraedrich, K. and Blender, R.: Scaling of Atmosphere and Ocean Temperature Correlations in Observations

- and Climate Models, Phys. Rev. Lett., 90, 108501, https://doi.org/10.1103/PhysRevLett.90.108501, 2003.
- Franke, J., Frank, D., Raible, C. C., Esper, J., and Brönnimann, S.: Spectral biases in tree-ring climate proxies, Nature Clim. Change, 3, 360–364, https://doi.org/10.1038/nclimate1816, 2013.
- Fritts, H.: Tree Rings and Climate, Elsevier, 583 pp., ISBN: 978-0-323-14528-2, 1976.
- Gómez-Navarro, J. J., Zorita, E., Raible, C. C., and Neukom, R.: Pseudo-proxy tests of the analogue method to reconstruct spatially resolved global temperature during the Common Era, Clim. Past, 13, 629–648, https://doi.org/10.5194/cp-13-629-2017, 2017.
- Goodkin, N. F., Hughen, K. A., Cohen, A. L., and Smith, S. R.: Record of Little Ice Age sea surface temperatures at Bermuda using a growth-dependent calibration of coral Sr/Ca, Paleoceanography, 20, https://doi.org/10.1029/2005PA001140, 2005.
- Goosse, H., Crespin, E., de Montety, A., Mann, M. E., Renssen, H., and Timmermann, A.: Reconstructing surface temperature changes over the past 600 years using climate model simulations with data assimilation, Journal of Geophysical Research: Atmospheres, 115, https://doi.org/10.1029/2009JD012737, 2010.
- Graf, W., Oerter, H., Reinwarth, O., Stichler, W., Wilhelms, F., Miller, H., and Mulvaney, R.: Stable-isotope records from Dronning Maud Land, Antarctica, PANGAEA [data set], https://doi.org/10.1594/PANGAEA.728240, 2002.
- Haam, E. and Huybers, P.: A test for the presence of covariance between time-uncertain series of data with application to the Dongge Cave speleothem and atmospheric radiocarbon records, Paleoceanography, 25, 14 pp., https://doi.org/10.1029/2008PA001713, 2010.
- Hasselmann, K.: Stochastic climate models Part I. Theory, Tellus, 28, 473–485, https://doi.org/10.3402/tellusa.v28i6.11316, 1976.
- Hayashi, E., Suzuki, A., Nakamura, T., Iwase, A., Ishimura, T., Iguchi, A., Sakai, K., Okai, T., Inoue, M., Araoka, D., Murayama, S., and Kawahata, H.: Growth-rate influences on coral climate proxies tested by a multiple colony culture experiment, Earth and Planetary Science Letters, 362, 198–206, https://doi.org/10.1016/j.epsl.2012.11.046, 2013.
- Hébert, R., Rehfeld, K., and Laepple, T.: Comparing estimation techniques for temporal scaling in palaeoclimate time series, Nonlin. Processes Geophys., 28, 311–328, https://doi.org/10.5194/npg-28-311-2021, 2021.
- Hirsch, N., Zuhr, A., Münch, T., Hörhold, M., Freitag, J., Dallmayr, R., and Laepple, T.: Stratigraphic noise and its potential drivers across the plateau of Dronning Maud Land, East Antarctica, The Cryosphere, 17, 4207–4221, https://doi.org/10.5194/tc-17-4207-2023, 2023.
- Hollyman, P. R., Laptikhovsky, V. V., and Richardson, C. A.: Techniques for Estimating the Age and Growth of Molluscs: Gastropoda, SHRE, 37, 773–782, https://doi.org/10.2983/035.037.0408, 2018.
- Holmes, R. L., Adams, R. K., and Fritts, H. C.: Tree-Ring Chronologies of Western North America: California, Eastern Oregon and Northern Great Basin with Procedures Used in the Chronology Development Work Including Users Manuals for Computer Programs COFECHA and ARSTAN, Laboratory of Tree-Ring Research Archives, The University of Arizona, https://repository.

- arizona.edu/handle/10150/304672 (last access: 22 May 2025), 1986
- Hörhold, M., Münch, T., Weißbach, S., Kipfstuhl, S., Freitag, J., Sasgen, I., Lohmann, G., Vinther, B., and Laepple, T.: Modern temperatures in central–north Greenland warmest in past millennium, Nature, 613, 503–507, https://doi.org/10.1038/s41586-022-05517-z, 2023.
- Hughes, M. K. and Ammann, C. M.: The future of the past an earth system framework for high resolution paleoclimatology: editorial essay, Climatic Change, 94, 247–259, https://doi.org/10.1007/s10584-009-9588-0, 2009.
- Hutson, W. H.: Bioturbation of deep-sea sediments: Oxygen isotopes and stratigraphic uncertainty, Geology, 8, 127–130, https://doi.org/10.1130/0091-7613(1980)8<127:BODSOI>2.0.CO;2, 1980.
- Huybers, P. and Curry, W.: Links between annual, Milankovitch and continuum temperature variability, Nature, 441, 329–332, https://doi.org/10.1038/nature04745, 2006.
- Johnsen, S. J., Clausen, H. B., Cuffey, K. M., Hoffmann, G., Schwander, J., and Creyts, T.: Diffusion of stable isotopes in polar firn and ice: the isotope effect in firn diffusion, in: Physics of Ice Core Records, vol. 159, edited by: Hondoh, T., Hokkaido University Press, Sapporo, Japan, 121–140, http://hdl.handle.net/ 2115/32465 (last access: 17 December 2019), 2000.
- Jones, D. S.: Sclerochronology: Reading the Record of the Molluscan Shell: Annual growth increments in the shells of bivalve molluscs record marine climatic changes and reveal surprising longevity, American Scientist, 71, 384–391, 1983.
- Jones, P. D., Briffa, K. R., Osborn, T. J., Lough, J. M., van Ommen, T. D., Vinther, B. M., Luterbacher, J., Wahl, E. R., Zwiers, F. W., Mann, M. E., Schmidt, G. A., Ammann, C. M., Buckley, B. M., Cobb, K. M., Esper, J., Goosse, H., Graham, N., Jansen, E., Kiefer, T., Kull, C., Küttel, M., Mosley-Thompson, E., Overpeck, J. T., Riedwyl, N., Schulz, M., Tudhope, A. W., Villalba, R., Wanner, H., Wolff, E., and Xoplaki, E.: Highresolution palaeoclimatology of the last millennium: a review of current status and future prospects, The Holocene, 19, 3–49, https://doi.org/10.1177/0959683608098952, 2009.
- King, J. M., Anchukaitis, K. J., Tierney, J. E., Hakim, G. J., Emile-Geay, J., Zhu, F., and Wilson, R.: A Data Assimilation Approach to Last Millennium Temperature Field Reconstruction Using a Limited High-Sensitivity Proxy Network, Journal of Climate, https://doi.org/10.1175/JCLI-D-20-0661.1, 2021.
- Kunz, T., Dolman, A. M., and Laepple, T.: A spectral approach to estimating the timescale-dependent uncertainty of paleoclimate records – Part 1: Theoretical concept, Clim. Past, 16, 1469–1492, https://doi.org/10.5194/cp-16-1469-2020, 2020.
- Laepple, T. and Huybers, P.: Reconciling discrepancies between Uk37 and Mg / Ca reconstructions of Holocene marine temperature variability, Earth and Planetary Science Letters, 375, 418– 429, https://doi.org/10.1016/j.epsl.2013.06.006, 2013.
- Laepple, T., Münch, T., Casado, M., Hoerhold, M., Landais, A., and Kipfstuhl, S.: On the similarity and apparent cycles of isotopic variations in East Antarctic snow pits, The Cryosphere, 12, 169– 187, https://doi.org/10.5194/tc-12-169-2018, 2018.
- Lee, T. C. K., Zwiers, F. W., and Tsao, M.: Evaluation of proxybased millennial reconstruction methods, Clim. Dyn., 31, 263–281, https://doi.org/10.1007/s00382-007-0351-9, 2008.

- Little, A. F., van Oppen, M. J. H., and Willis, B. L.: Flexibility in Algal Endosymbioses Shapes Growth in Reef Corals, Science, 304, 1492–1494, https://doi.org/10.1126/science.1095733, 2004.
- Lough, J. M.: A strategy to improve the contribution of coral data to high-resolution paleoclimatology, Palaeogeography, Palaeoclimatology, Palaeoecology, 204, 115–143, https://doi.org/10.1016/S0031-0182(03)00727-2, 2004.
- Lücke, L. J., Hegerl, G. C., Schurer, A. P., and Wilson, R.: Effects of Memory Biases on Variability of Temperature Reconstructions, Journal of Climate, 32, 8713–8731, https://doi.org/10.1175/JCLI-D-19-0184.1, 2019.
- Maier, C., Felis, T., Pätzold, J., and Bak, R. P. M.: Effect of skeletal growth and lack of species effects in the skeletal oxygen isotope climate signal within the coral genus Porites, Marine Geology, 207, 193–208, https://doi.org/10.1016/j.margeo.2004.03.008, 2004.
- Mann, M. E. and Rutherford, S.: Climate reconstruction using "Pseudoproxies", Geophysical Research Letters, 29, 139-1–139-4, https://doi.org/10.1029/2001GL014554, 2002.
- Mann, M. E., Rutherford, S., Wahl, E., and Ammann, C.: Testing the Fidelity of Methods Used in Proxy-Based Reconstructions of Past Climate, Journal of Climate, 18, 4097–4107, https://doi.org/10.1175/JCLI3564.1, 2005.
- Mann, M. E., Rutherford, S., Wahl, E., and Ammann, C.: Robustness of proxy-based climate field reconstruction methods, Journal of Geophysical Research: Atmospheres, 112, https://doi.org/10.1029/2006JD008272, 2007.
- Matalas, N. C.: Statistical Properties of Tree Ring Data, International Association of Scientific Hydrology, Bulletin, 7, 39–47, https://doi.org/10.1080/02626666209493254, 1962.
- McCulloch, M. T., Winter, A., Sherman, C. E., and Trotter, J. A.: 300 years of sclerosponge thermometry shows global warming has exceeded 1.5 °C, Nat. Clim. Chang., 14, 171–177, https://doi.org/10.1038/s41558-023-01919-7, 2024.
- McPartland, M. Y. and Dolman, A.: EarthSystemDiagnostics/M-cPartland_etal_2024_DendroSNR: v1.1 (v1.1), Zenodo [code], https://doi.org/10.5281/zenodo.10822165, 2024.
- McPartland, M. Y., St. George, S., Pederson, G. T., and Anchukaitis, K. J.: Does signal-free detrending increase chronology coherence in large tree-ring networks?, Dendrochronologia, 125755, https://doi.org/10.1016/j.dendro.2020.125755, 2020.
- McPartland, M. Y., Dolman, A. M., and Laepple, T.: Separating Common Signal From Proxy Noise in Tree Rings, Geophysical Research Letters, 51, e2024GL109282, https://doi.org/10.1029/2024GL109282, 2024.
- Meko, D. M.: Applications of Box-Jenkins methods of time series analysis to the reconstruction of drought from tree rings, PhD thesis, University of Arizona, Tucson, Arizona, USA. 149 pp., https://repository.arizona.edu/handle/10150/191062 (last access: 19 April 2019), 1981.
- Melvin, T. M. and Briffa, K. R.: A "signal-free" approach to dendroclimatic standardisation, Dendrochronologia, 26, 71–86, https://doi.org/10.1016/j.dendro.2007.12.001, 2008.
- Melvin, T. M. and Briffa, K. R.: CRUST: Software for the implementation of Regional Chronology Standardisation: Part 1. Signal-Free RCS, Dendrochronologia, 32, 7–20, https://doi.org/10.1016/j.dendro.2013.06.002, 2014a.
- Melvin, T. M. and Briffa, K. R.: CRUST: Software for the implementation of Regional Chronology Standardisation: Part 2. Fur-

- ther RCS options and recommendations, Dendrochronologia, 32, 343–356, https://doi.org/10.1016/j.dendro.2014.07.008, 2014b.
- Münch, T., McPartland M. Y., Dolman, A., and Laepple, T.: proxysnr: An R package to separate the common signal from local noise in climate proxy records using spectral analyses, Zenodo [code], https://doi.org/10.5281/zenodo.17098991, 2025.
- Münch, T.: proxysnr: An R package to separate the common signal from local noise in climate proxy records using spectral analyses (v1.0.1), Zenodo [code], https://doi.org/10.5281/zenodo.17098991, 2025a.
- Münch, T.: ice-colors-of-noise: R software to perform signal-to-noise ratio analyses for Greenland and Antarctic ice-core data (v0.1.0), Zenodo [code], https://doi.org/10.5281/zenodo.17102273, 2025b.
- Münch, T. and Laepple, T.: What climate signal is contained in decadal- to centennial-scale isotope variations from Antarctic ice cores?, Clim. Past, 14, 2053–2070, https://doi.org/10.5194/cp-14-2053-2018, 2018.
- Münch, T., Werner, M., and Laepple, T.: How precipitation intermittency sets an optimal sampling distance for temperature reconstructions from Antarctic ice cores, Clim. Past, 17, 1587–1605, https://doi.org/10.5194/cp-17-1587-2021, 2021.
- Neukom, R., Steiger, N., Gómez-Navarro, J. J., Wang, J., and Werner, J. P.: No evidence for globally coherent warm and cold periods over the preindustrial Common Era, Nature, 571, 550–554, https://doi.org/10.1038/s41586-019-1401-2, 2019.
- PAGES 2k Consortium, Ahmed, M., Anchukaitis, K. J., Asrat, A., Borgaonkar, H. P., Braida, M., Buckley, B. M., Büntgen, U., Chase, B. M., Christie, D. A., Cook, E. R., Curran, M. A. J., Diaz, H. F., Esper, J., Fan, Z.-X., Gaire, N. P., Ge, Q., Gergis, J., González-Rouco, J. F., Goosse, H., Grab, S. W., Graham, N., Graham, R., Grosjean, M., Hanhijärvi, S. T., Kaufman, D. S., Kiefer, T., Kimura, K., Korhola, A. A., Krusic, P. J., Lara, A., Lézine, A.-M., Ljungqvist, F. C., Lorrey, A. M., Luterbacher, J., Masson-Delmotte, V., McCarroll, D., McConnell, J. R., McKay, N. P., Morales, M. S., Moy, A. D., Mulvaney, R., Mundo, I. A., Nakatsuka, T., Nash, D. J., Neukom, R., Nicholson, S. E., Oerter, H., Palmer, J. G., Phipps, S. J., Prieto, M. R., Rivera, A., Sano, M., Severi, M., Shanahan, T. M., Shao, X., Shi, F., Sigl, M., Smerdon, J. E., Solomina, O. N., Steig, E. J., Stenni, B., Thamban, M., Trouet, V., Turney, C. S. M., Umer, M., Ommen, T. van, Verschuren, D., Viau, A. E., Villalba, R., Vinther, B. M., Gunten, L. von, Wagner, S., Wahl, E. R., Wanner, H., Werner, J. P., White, J. W. C., Yasue, K., and Zorita, E.: Continental-scale temperature variability during the past two millennia, Nature Geoscience, 6, 339—346, https://doi.org/10.1038/ngeo1797, 2013.
- PAGES2k Consortium, Emile-Geay, J., McKay, N. P., Kaufman, D. S., Gunten, L. von, Wang, J., Anchukaitis, K. J., Abram, N. J., Addison, J. A., Curran, M. A. J., Evans, M. N., Henley, B. J., Hao, Z., Martrat, B., McGregor, H. V., Neukom, R., Pederson, G. T., Stenni, B., Thirumalai, K., Werner, J. P., Xu, C., Divine, D. V., Dixon, B. C., Gergis, J., Mundo, I. A., Nakatsuka, T., Phipps, S. J., Routson, C. C., Steig, E. J., Tierney, J. E., Tyler, J. J., Allen, K. J., Bertler, N. A. N., Björklund, J., Chase, B. M., Chen, M.-T., Cook, E., Jong, R. de, DeLong, K. L., Dixon, D. A., Ekaykin, A. A., Ersek, V., Filipsson, H. L., Francus, P., Freund, M. B., Frezzotti, M., Gaire, N. P., Gajewski, K., Ge, Q., Goosse, H., Gornostaeva, A., Grosjean, M., Horiuchi, K., Hormes, A., Husum, K., Isaksson, E., Kandasamy, S.,

- Kawamura, K., Kilbourne, K. H., Koç, N., Leduc, G., Linderholm, H. W., Lorrey, A. M., Mikhalenko, V., Mortyn, P. G., Motoyama, H., Moy, A. D., Mulvaney, R., Munz, P. M., Nash, D. J., Oerter, H., Opel, T., Orsi, A. J., Ovchinnikov, D. V., Porter, T. J., Roop, H. A., Saenger, C., Sano, M., Sauchyn, D., Saunders, K. M., Seidenkrantz, M.-S., Severi, M., Shao, X., Sicre, M.-A., Sigl, M., Sinclair, K., George, S. S., Jacques, J.-M. S., Thamban, M., Thapa, U. K., Thomas, E. R., Turney, C., Uemura, R., Viau, A. E., Vladimirova, D. O., Wahl, E. R., White, J. W. C., Yu, Z., and Zinke, J.: A global multiproxy database for temperature reconstructions of the Common Era, Scientific Data, 4, 170088, https://doi.org/10.1038/sdata.2017.88, 2017.
- Pelletier, J. D.: The power spectral density of atmospheric temperature from time scales of 10⁻² to 10⁶ yr, Earth and Planetary Science Letters, 158, 157–164, https://doi.org/10.1016/S0012-821X(98)00051-X, 1998.
- Peng, T.-H. and Broecker, W. S.: The impacts of bioturbation on the age difference between benthic and planktonic foraminifera in deep sea sediments, Nuclear Instruments and Methods in Physics Research Section B: Beam Interactions with Materials and Atoms, 5, 346–352, https://doi.org/10.1016/0168-583X(84)90540-8, 1984.
- Percival, D. B. and Walden, A. T.: Spectral Analysis for Physical Applications, Cambridge University Press, 616 pp., ISBN: 978-0-521-43541-3, 1993.
- Reschke, M., Rehfeld, K., and Laepple, T.: Empirical estimate of the signal content of Holocene temperature proxy records, Clim. Past, 15, 521–537, https://doi.org/10.5194/cp-15-521-2019, 2019.
- Rhines, A. and Huybers, P.: Estimation of spectral power laws in time uncertain series of data with application to the Greenland Ice Sheet Project 2 δ^{18} O record, Journal of Geophysical Research: Atmospheres, 116, https://doi.org/10.1029/2010JD014764, 2011.
- Riedwyl, N., Küttel, M., Luterbacher, J., and Wanner, H.: Comparison of climate field reconstruction techniques: application to Europe, Clim. Dyn., 32, 381–395, https://doi.org/10.1007/s00382-008-0395-5, 2009.
- Ruddiman, W. F., Jones, G. A., Peng, T.-H., Glover, L. K., Glass, B. P., and Liebertz, P. J.: Tests for size and shape dependency in deep-sea mixing, Sedimentary Geology, 25, 257–276, https://doi.org/10.1016/0037-0738(80)90064-0, 1980.
- Rypel, A. L., Haag, W. R., and Findlay, R. H.: Validation of annual growth rings in freshwater mussel shells using cross dating, Can. J. Fish. Aquat. Sci., 65, 2224–2232, https://doi.org/10.1139/F08-129, 2008.
- Saenger, C., Cohen, A. L., Oppo, D. W., and Hubbard, D.: Interpreting sea surface temperature from strontium/calcium ratios in Montastrea corals: Link with growth rate and implications for proxy reconstructions, Paleoceanography, 23, https://doi.org/10.1029/2007PA001572, 2008.
- Schiffelbein, P.: Calculation of error measures for deconvolved deep-sea stratigraphic records, Marine Geology, 65, 333–342, https://doi.org/10.1016/0025-3227(85)90063-5, 1985.
- Schiffelbein, P. and Hills, S.: Direct assessment of stable isotope variability in planktonic foraminifera populations, Palaeogeography, Palaeoclimatology, Palaeoecology, 48, 197–213, https://doi.org/10.1016/0031-0182(84)90044-0, 1984.

- Scott, R. B., Holland, C. L., and Quinn, T. M.: Multi-decadal Trends in Instrumental SST and Coral Proxy Sr/Ca Records, Journal of Climate, 23, 1017–1033, https://doi.org/10.1175/2009JCLI2386.1, 2010.
- Shaw, F., Dolman, A. M., Kunz, T., Gkinis, V., and Laepple, T.: Novel approach to estimate the water isotope diffusion length in deep ice cores with an application to Marine Isotope Stage 19 in the Dome C ice core, The Cryosphere, 18, 3685–3698, https://doi.org/10.5194/tc-18-3685-2024, 2024.
- Smerdon, J. E.: Climate models as a test bed for climate reconstruction methods: pseudoproxy experiments, WIREs Climate Change, 3, 63–77, https://doi.org/10.1002/wcc.149, 2012.
- Smerdon, J. E., Kaplan, A., Chang, D., and Evans, M. N.: A Pseudoproxy Evaluation of the CCA and RegEM Methods for Reconstructing Climate Fields of the Last Millennium, Journal of Climate, https://doi.org/10.1175/2010JCLI3328.1, 2010.
- Speer, J. H.: Fundamentals of Tree-ring Research, University of Arizona Press, 370 pp., ISBN: 978-0-8165-2684-0, 2010.
- Stenni, B., Curran, M. A. J., Abram, N. J., Orsi, A., Goursaud, S., Masson-Delmotte, V., Neukom, R., Goosse, H., Divine, D., van Ommen, T., Steig, E. J., Dixon, D. A., Thomas, E. R., Bertler, N. A. N., Isaksson, E., Ekaykin, A., Werner, M., and Frezzotti, M.: Antarctic climate variability on regional and continental scales over the last 2000 years, Clim. Past, 13, 1609–1634, https://doi.org/10.5194/cp-13-1609-2017, 2017.
- Suzuki, A., Hibino, K., Iwase, A., and Kawahata, H.: Intercolony variability of skeletal oxygen and carbon isotope signatures of cultured Porites corals: Temperature-controlled experiments, Geochimica et Cosmochimica Acta, 69, 4453–4462, https://doi.org/10.1016/j.gca.2005.05.018, 2005.
- Tolwinski-Ward, S. E., Evans, M. N., Hughes, M. K., and Anchukaitis, K. J.: An efficient forward model of the climate controls on interannual variation in tree-ring width, Clim. Dyn., 36, 2419–2439, https://doi.org/10.1007/s00382-010-0945-5, 2011.
- Vaganov, E. A., Anchukaitis, K. J., and Evans, M. N.: How Well Understood Are the Processes that Create Dendroclimatic Records? A Mechanistic Model of the Climatic Control on Conifer Tree-Ring Growth Dynamics, in: Dendroclimatology: Progress and Prospects, edited by: Hughes, M. K., Swetnam, T. W., and Diaz, H. F., Springer Netherlands, Dordrecht, 37–75, https://doi.org/10.1007/978-1-4020-5725-0_3, 2011.
- Vautard, R. and Ghil, M.: Singular spectrum analysis in non-linear dynamics, with applications to paleoclimatic time series, Physica D: Nonlinear Phenomena, 35, 395–424, https://doi.org/10.1016/0167-2789(89)90077-8, 1989.
- von Storch, H., Zorita, E., Jones, J. M., Dimitriev, Y., González-Rouco, F., and Tett, S. F. B.: Reconstructing Past Climate from Noisy Data, Science, 306, 679–682, https://doi.org/10.1126/science.1096109, 2004.

- von Storch, H., Zorita, E., and González-Rouco, F.: Assessment of three temperature reconstruction methods in the virtual reality of a climate simulation, Int. J. Earth Sci. (Geol. Rundsch.), 98, 67– 82, https://doi.org/10.1007/s00531-008-0349-5, 2009.
- Walter, R. M., Sayani, H. R., Felis, T., Cobb, K. M., Abram, N. J., Arzey, A. K., Atwood, A. R., Brenner, L. D., Dassié, É. P., DeLong, K. L., Ellis, B., Emile-Geay, J., Fischer, M. J., Goodkin, N. F., Hargreaves, J. A., Kilbourne, K. H., Krawczyk, H., McKay, N. P., Moore, A. L., Murty, S. A., Ong, M. R., Ramos, R. D., Reed, E. V., Samanta, D., Sanchez, S. C., Zinke, J., and the PAGES CoralHydro2k Project Members: The CoralHydro2k database: a global, actively curated compilation of coral δ^{18} O and Sr / Ca proxy records of tropical ocean hydrology and temperature for the Common Era, Earth Syst. Sci. Data, 15, 2081–2116, https://doi.org/10.5194/essd-15-2081-2023, 2023.
- Weißbach, S., Wegner, A., Opel, T., Oerter, H., Vinther, B. M., and Kipfstuhl, S.: Spatial and temporal oxygen isotope variability in northern Greenland – implications for a new climate record over the past millennium, Clim. Past, 12, 171–188, https://doi.org/10.5194/cp-12-171-2016, 2016.
- Whillans, I. M. and Grootes, P. M.: Isotopic diffusion in cold snow and firn, Journal of Geophysical Research: Atmospheres, 90, 3910–3918, https://doi.org/10.1029/JD090iD02p03910, 1985.
- Zhang, H., Yuan, N., Esper, J., Werner, J. P., Xoplaki, E., Büntgen, U., Treydte, K., and Luterbacher, J.: Modified climate with long term memory in tree ring proxies, Environ. Res. Lett., 10, 084020, https://doi.org/10.1088/1748-9326/10/8/084020, 2015.
- Zhu, F., Emile-Geay, J., McKay, N. P., Hakim, G. J., Khider, D., Ault, T. R., Steig, E. J., Dee, S., and Kirchner, J. W.: Climate models can correctly simulate the continuum of global-average temperature variability, Proceedings of the National Academy of Sciences, 116, 8728–8733, https://doi.org/10.1073/pnas.1809959116, 2019.
- Zhu, F., Emile-Geay, J., McKay, N. P., Stevenson, S., and Meng, Z.: A pseudoproxy emulation of the PAGES 2k database using a hierarchy of proxy system models, Sci. Data, 10, 624, https://doi.org/10.1038/s41597-023-02489-1, 2023.
- Zuhr, A. M., Wahl, S., Steen-Larsen, H. C., Hörhold, M., Meyer, H., and Laepple, T.: A Snapshot on the Buildup of the Stable Water Isotopic Signal in the Upper Snowpack at EastGRIP on the Greenland Ice Sheet, Journal of Geophysical Research: Earth Surface, 128, e2022JF006767, https://doi.org/10.1029/2022JF006767, 2023.