



## Supplement of

## Statistical characteristics of extreme daily precipitation during 1501 BCE–1849 CE in the Community Earth System Model

Woon Mi Kim et al.

Correspondence to: Woon Mi Kim (woonmi.kim@climate.unibe.ch)

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Empirical Orthogonal Function analysis (EOF; Hannachi et al., 2007) is used to derive the spatial patterns and the time series associated with the modes of internal variability in ERA5, CESM in 1979 – 2008 CE, and CESM during 1501 CE – 1849 CE. The EOF is applied to the sea surface temperature (SST) to infer the Pacific Decadal Oscillation (PDO) and the geopotential height at 500 hPa for other modes. The observational SST dataset is the ERSST v5 (Huang et al., 2017). The modes that are also detected as well by Fasullo et al. (2020) which used the CMIP models including the CESM family models, and by Lim (2015) which used the reanalysis are considered.

For the Northern Annular Mode (NAM; Thompson and Wallace, 2000) and Pacific North American (PNA) pattern (Wallace and Gutzler, 1981), the EOF is applied over the region confined to  $180^{\circ}W - 180^{\circ}E$  and  $20^{\circ} - 90^{\circ}N$ ; for the Southern Annular Mode (SAM; Marshall, 2003) and the Pacific South American 1 (PSA) pattern (Mo and Paegle, 2001), the region over  $180^{\circ}W - 180^{\circ}E$  and  $20^{\circ} - 90^{\circ}S$ ; for the North Atlantic Oscillation (NAO; Wallace and Gutzler, 1981) and Eastern Atlantic-West Russian pattern (EA-WR; Barnston and Livezey, 1987; Washington et al., 2000), the region over  $70^{\circ}W - 70^{\circ}E$  and  $20^{\circ} - 85^{\circ}N$ ; and for the Pacific Decadal Oscillation (PDO; Trenberth and Hurrell, 1994), the region over  $120^{\circ}E - 75^{\circ}E$  and  $20^{\circ} - 70^{\circ}N$ . For NAM and SAM, the conventional EOF analysis is used, while for other, the rotated EOF (REOF) is applied. Among the resulting EOF patterns, those patterns whose root-mean-square-errors (RMSE) against the observational/reanalysis patterns are relatively low are chosen.

The RMSE is calculated as:

$$RMSE = \sqrt{\frac{\sum_{1}^{N} (X_i - Y_i)^2}{N}} \tag{1}$$

Where N is the total number of data,  $X_i$  is the time series of a variable from the observation, and  $Y_i$  is the time series of the same variable from the model simulation.

Unlike other indices, El Niño Southern Oscillation (ENSO) is computed as the mean SST over the Niño3.4 region in  $170^{\circ}W - 120^{\circ}W$  and  $5^{\circ}S - 5^{\circ}N$ (Trenberth and Stepaniak, 2001).



Figure S 1: Modes of internal variability from (a) ERA5, (b) CESM 1979 – 2008 CE, and (c) CESM 1501 BCE – 1849 CE.



Figure S 2: Continuation of Fig. S 1



Figure S 3: RMSE between the spatial patterns of the modes of variability of ERA5 and CESM for 1979–2008 CE (Panels a and b in Figs. S 1 and S 2)



Figure S 4: Globally and annually averaged monthly temperature anomaly from the full-forcing simulation.



Figure S 5: The external-forcing-GPD models that explains the variability of extreme precipitation better than the stationary GPD model in Fig. 9 at the 99% confidence interval in the full-forcing simulation.



Figure S 6: Same as Fig. S 5 but for the orbital-only simulation.



Figure S 7: The non-stationary GPD models with (a) the modes of variability, (b) the modes of variability and TS-G, and (c) the modes of variability and TS-R as covariates, that outperform all other GPD models (the modesof-variability-covariate, TS-G or TS-R, and stationary models) at 99% confidence interval, hence, explain best the variability of extreme precipitation in orbital-only (right) and full forcing (left) simulations.

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